CS 61C Fall 2023

Caches, AMAT

 $Discussion \ 9$

1 Pre-Check

This section is designed as a conceptual check for you to determine if you conceptually understand and have any misconceptions about this topic. Please answer true/false to the following questions, and include an explanation:

- 1.1 We cannot use a 1KB cache in a 32-bit system because it's too small and cannot contain all possible addresses.
- 1.2 If a piece of data is both in the cache and in memory, reading it from cache is faster than reading from memory.

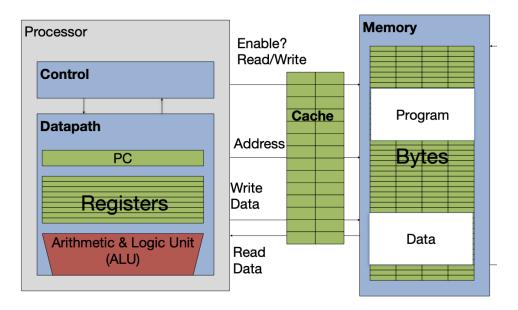
1.3 Caches see an immediate improvement in memory access time at program execution.

1.4 Increasing cache size by adding more blocks always improves (increases) hit rate for all programs.

1.5 Decreasing block size to increase the **number** of blocks held by the cache improves the program speed for all programs.

2 Understanding T/I/O

We use caches to make our access to data faster. When working with main memory (RAM), the main problem faced is the fact that access to the main memory is very slow. In fact, modern processors take about 100 instructions cycles or more to access the main memory, meaning memory accesses become the bottleneck of our programs. Caches help fix this problem for us - they hold a portion of the data in main memory, that we might access again later on. They are closer to the processor in the memory hierarchy, and thus accessing a cache is much faster than accessing the main memory.



As seen above, the access to cache is the middle step between the CPU asking for a memory bit, and the actual main memory access - if the data is not found in the cache, only then is main memory accessed. This way unnecessary trips to main memory are avoided. One important detail is that caches are much smaller in size than main memory - this is why we have to be efficient in what we hold in caches. When we are saving data in caches, we need to be as efficient as possible. In order to do this, we make use of locality. We have two different kinds of locality to consider.

- **Temporal Locality:** If we have accessed a piece of information recently, it is possible that we will access it again. So, we hold this data in the cache.
- Spatial Locality: If we have accessed a memory location recently, it is probable that we will access the neighbouring addresses as well. So, we also keep the neighbouring addresses within the cache. An example is array accesses if we access the 0th element of an array, it is probable we will also access the 1st one.

Note that caches hold the data in blocks that have a size equal to the block size of the cache.

When working with caches, we have to be able to break down the memory addresses we work with to understand where they fit into our caches. There are three fields:

- Tag Used to distinguish different blocks that use the same index. Number of bits: (# of bits in memory address) Index Bits Offset Bits
- Index The set that this piece of memory will be placed in. Number of bits: $\log_2(\# \text{ of indices})$
- Offset The location of the byte in the block. Number of bits: log₂(size of block)

Given these definitions, the following is true:

 $\log_2(\text{memory size}) = \# \text{ memory address bits} = \# \text{ tag bits} + \# \text{ index bits} + \# \text{ offset bits}$

Another useful equality to remember is:

cache size = block size * num blocks

One thing to consider when calculating index, offset, and tag bits is their order within an address:

Tag	Index	Offset

As seen above, the tag bits are to the left (most significant), the index bits are in the middle, and the offset bits are the to the right (least significant).

2.1 Assume we have a direct-mapped byte-addressed cache with capacity 32B and block size of 8B. Of the 32 bits in each address, which bits do we use to find the tag, index, and offset of the cache?

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2.2 Assume that we have the same cache scheme as the previous part (direct-mapped byte-addressed cache with capacity 32B and block size of 8B). Classify each of the following byte memory accesses as a cache hit (H), cache miss (M), or cache miss with replacement (R). Tip: Drawing out the cache can help you see the replacements more clearly.

Address	T/I/O	Hit, Miss, Replace
0x00000004		
0x00000005		
0x0000068		
0x000000C8		
0×0000068		
0x000000DD		
0x00000045		
0x000000CF		
0x000000F3		

(Feel free to use the space below to draw your cache.)

3 The 3 C's of Cache Misses

In order to evaluate cache performance and hit rate, especially with determining how effective our current cache structure is, it is useful to analyze the misses that do occur, and adjust accordingly. Below, we categorize cache misses into three types:

- **Compulsory**: A miss that must occur when you bring in a certain block for a first time, hence "compulsory". Compulsory misses occur when a program is first started, and the cache does not contain any of that program's data.
- **Conflict**: A miss that occurs if the block was fetched before and in our cache, but was evicted while the cache was not full. Increasing the associativity of the cache may help avoid conflict misses.
- **Capacity**: A miss that occurs if the block was fetched before and in our cache, but evicted while the cache was full. Capacity misses may be resolved by increasing the size of the cache.

Go back to question 2 and classify each miss (M) and replacement (R) as one of the 3 types of misses described above.

3.1

4 Cache Associativity

In the previous question, we focused on Direct-Mapped caches, in which each block of memory maps to specifically one slot in our cache. This is good for quick replacement and finding our block in the cache, but not good for spatial efficiency!

This is where we bring associativity into the matter. We define associativity as the number of slots a block can potentially map to in our cache. Thus, a Fully-Associative cache has the most associativity, meaning every block can go anywhere in the cache. Our Direct-Mapped cache, on the other hand, has the least, being only 1-way set associative.

For an N-way associative cache, the following are true:

N * # sets = # blocks, Index bits = $log_2(# sets)$

4.1 Here's some practice involving a 2-way set associative cache. This time we have an 8-bit address space, 8 B blocks, and a cache size of 32 B. Classify each of the following accesses as a cache hit (H), cache miss (M) or cache miss with replacement (R). For any misses, list out which type of miss it is (Compulsory, Conflict, or Capacity). Assume that we have an LRU replacement policy (in general, this is not always the case).

Address	T/I/O	Hit, Miss, Replace
0b0000 0100		
0b0000 0101		
0b0110 1000		
0b1100 1000		
0b0110 1000		
0b1101 1101		
0b0100 0101		
0b0000 0100		
0b0011 0000		
0b1100 1011		
0b0100 0010		

[4.2] What is the hit rate of our above accesses?

5 Cache Performance

Recall that AMAT stands for Average Memory Access Time. The main formula for it is:

AMAT = Hit Time + Miss Rate * Miss Penalty

In a multi-level cache structure, we can separate miss rates into two types that we consider for each level.

- **Global:** Calculated as the number of accesses that missed at that level divided by the total number of accesses to the cache system.
- Local: Calculated as the number of accesses that missed at that level divided by the total number of accesses to that cache level.
- 5.1 In a 2-level cache system, after 100 total accesses to the cache system, we find that the L2\$ (L2 cache) ended up missing 20 times. What is the global miss rate of L2\$?
- 5.2 Given the system from the previous subpart, if L1\$ had a local miss rate of 50%, what is the local miss rate of L2\$?

Suppose your system consists of:

- 1. An L1\$ that has a hit time of 2 cycles and has a local miss rate of 20%
- 2. An L2\$ that has a hit time of 15 cycles and has a global miss rate of 5%
- 3. Main memory where accesses take 100 cycles
- 5.3 What is the local miss rate of L2\$?
- 5.4 What is the AMAT of the system?
- 5.5 Suppose we want to reduce the AMAT of the system to 8 cycles or lower by adding in a L3\$. If the L3\$ has a local miss rate of 30%, what is the largest hit time that the L3\$ can have?

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6 Code Analysis

Given the follow chunk of code, analyze the hit rate given that we have a byteaddressed computer with a total memory of **1** MiB. It also features a **16** KiB Direct-Mapped cache with **1** KiB blocks. Assume that your cache begins cold.

```
#define NUM_INTS 8192 // 2^13
int A[NUM_INTS]; // A lives at 0x10000
int i, total = 0;
for (i = 0; i < NUM_INTS; i += 128) {
    A[i] = i; // Line 1
}
for (i = 0; i < NUM_INTS; i += 128) {
    total += A[i]; // Line 2
}</pre>
```

[6.1] How many bits make up a memory address on this computer?

[6.2] What is the T:I:O breakdown?

[6.3] Calculate the cache hit rate for the line marked Line 1:

[6.4] Calculate the cache hit rate for the line marked Line 2: