

Virtual Memory Overview

Virtual address (VA): What your program uses

| | |
|---------------------|-------------|
| Virtual Page Number | Page Offset |
|---------------------|-------------|

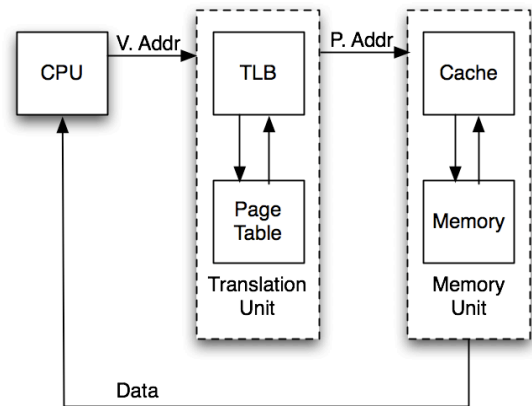
Physical address (PA): What actually determines where in memory to go

| | |
|----------------------|-------------|
| Physical Page Number | Page Offset |
|----------------------|-------------|

With 4 KiB pages and byte addresses, $2^{(page\ offset\ bits)} = 4096$, so page offset bits = 12.

The Big Picture: Logical Flow

Translate VA to PA using the TLB and Page Table. Then use PA to access memory as the program intended.



Pages

A chunk of memory or disk with a set size. Addresses in the same virtual page get mapped to addresses in the same physical page. The page table determines the mapping.

The Page Table

| Index = Virtual Page Number (not stored) | Page Valid | Page Dirty | Permission Bits (read, write, ...) | Physical Page Number |
|---|------------|------------|---------------------------------------|----------------------|
| 0 | | | | |
| 1 | | | | |
| 2 | | | | |
| ... | | | | |
| (Max virtual page number) | | | | |

Each stored row of the page table is called a **page table entry** (the grayed section is the first page table entry). The page table is stored *in memory*; the OS sets a register telling the hardware the address of the first entry of the page table. The processor updates the “page dirty” in the page table: “page dirty” bits are used by the OS to know whether updating a page on disk is necessary. Each process gets its own page table.

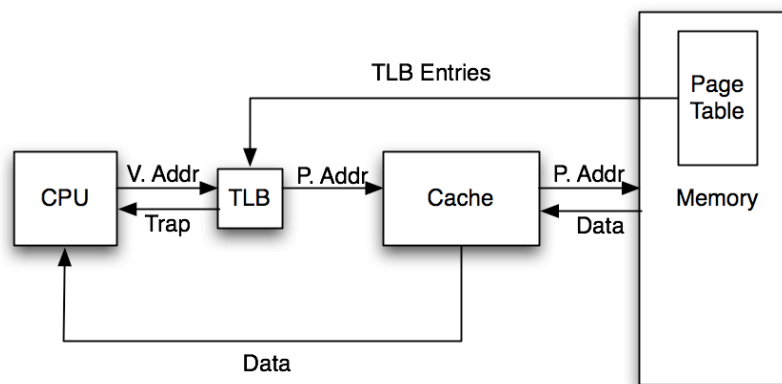
- **Protection Fault**--The page table entry for a virtual page has permission bits that prohibit the requested operation
- **Page Fault**--The page table entry for a virtual page has its valid bit set to false. The entry is not in memory.

The Translation Lookaside Buffer (TLB)

A cache for the page table. Each block is a single page table entry. If an entry is not in the TLB, it's a TLB miss. Assuming *fully associative*:

| TLB Entry Valid | Tag = Virtual Page Number | Page Table Entry | | |
|-----------------|---------------------------|------------------|-----------------|----------------------|
| | | Page Dirty | Permission Bits | Physical Page Number |
| ... | ... | ... | ... | ... |

The Big Picture Revisited



Exercises

1) What are three specific benefits of using virtual memory?

Bridges memory and disk in memory hierarchy.
 Simulates full address space for each process.
 Enforces protection between processes.

2) What should happen to the TLB when a new value is loaded into the page table address register?

The valid bits of the TLB should all be set to 0. The page table entries in the TLB corresponded to the old page table, so none of them are valid once the page table address register points to a different page table.

3) x86 has an "accessed" bit in each page table entry, which is like the dirty bit but set whenever a page is used (load *or* store). Why is this helpful when using memory as a cache for disk?

It allows smarter replacements. We naturally want fewer misses (page faults), so if possible, we would want to replace a page table entry that hasn't been used. The "accessed" bit is one way of giving us enough information to implement this.

4) Fill this table out!

| Virtual Address Bits | Physical Address Bits | Page Size | VPN Bits | PPN Bits | Bits per row of PT (4 extra bits) |
|----------------------|-----------------------|-----------|----------|----------|-----------------------------------|
| 32 | 32 | 16KiB | 18 | 18 | 22 |
| 32 | 26 | 8KiB | 19 | 13 | 17 |
| 36 | 32 | 32KiB | 21 | 17 | 21 |
| 40 | 36 | 32KiB | 25 | 21 | 25 |
| 64 | 40 | 64KiB | 48 | 24 | 28 |

5) A processor has 16-bit addresses, 256 byte pages, and an 8-entry fully associative TLB with LRU replacement (the LRU field is 3 bits and encodes the order in which pages were accessed, 0 being the most recent). At some time instant, the TLB for the current process is the initial state given in the table below. Assume that all current page table entries are in the initial TLB. Assume also that all pages can be read from and written to. Fill in the final state of the TLB according to the access pattern below.

Free physical pages: 0x17, 0x18, 0x19

Access pattern:

Read 0x11f0, Write 0x1301, Write 0x20ae, Write 0x2332, Read 0x20ff, Write 0x3415

Initial

| VPN | PPN | Valid | Dirty | LRU |
|------|------|-------|-------|-----|
| 0x01 | 0x11 | 1 | 1 | 0 |
| 0x00 | 0x00 | 0 | 0 | 7 |
| 0x10 | 0x13 | 1 | 1 | 1 |
| 0x20 | 0x12 | 1 | 0 | 5 |
| 0x00 | 0x00 | 0 | 0 | 7 |
| 0x11 | 0x14 | 1 | 0 | 4 |
| 0xac | 0x15 | 1 | 1 | 2 |
| 0xff | 0x16 | 1 | 0 | 3 |

Read 0x11f0: hit, LRUs: 1,7,2,5,7,0,3,4

Write 0x1301: miss, map VPN 0x13 to PPN 0x17, valid and dirty, LRUs: 2,0,3,6,7,1,4,5

Write 0x20ae: hit, dirty, LRUs: 3,1,4,0,7,2,5,6

Write 0x2332: miss, map VPN 0x23 to PPN 0x18, valid and dirty, LRUs: 4,2,5,1,0,3,6,7

Read 0x20ff: hit, LRUs: 4,2,5,0,1,3,6,7

Write 0x3415: miss and replace last entry, map VPN 0x34 to 0x19, dirty, LRUs: 5,3,6,1,2,4,7,0

Final

| VPN | PPN | Valid | Dirty | LRU |
|------|------|-------|-------|-----|
| 0x01 | 0x11 | 1 | 1 | 5 |

| | | | | |
|------|------|---|---|---|
| 0x13 | 0x17 | 1 | 1 | 3 |
| 0x10 | 0x13 | 1 | 1 | 6 |
| 0x20 | 0x12 | 1 | 1 | 1 |
| 0x23 | 0x18 | 1 | 1 | 2 |
| 0x11 | 0x14 | 1 | 0 | 4 |
| 0xac | 0x15 | 1 | 1 | 7 |
| 0x34 | 0x19 | 1 | 1 | 0 |