1 Pre-Check

This section is designed as a conceptual check for you to determine if you conceptually understand and have any misconceptions about this topic. Please answer true/false to the following questions, and include an explanation:

1.1 If a page table entry can not be found in the TLB, then a page fault has occurred.

1.2 The local miss rate of one level of a cache is always greater than or equal to the global miss rate of that cache.

1.3 SIMD is a form of instruction-level parallelism.

2 VM Access Patterns

A processor has 16-bit addresses, 256 byte pages, and an 8-entry fully associative TLB with LRU replacement (the LRU field is 3 bits and encodes the order in which pages were accessed, 0 being the most recent). At some time instant, the TLB for the current process is the initial state given in the table below. Assume that all current page table entries are in the initial TLB. Assume also that all pages can be read from and written to. Fill in the final state of the TLB according to the access pattern below.
Free Physical Pages 0x17, 0x18, 0x19

Access Pattern

1. 0x11f0 (Read)
2. 0x1301 (Write)
3. 0x20ae (Write)
4. 0x2332 (Write)
5. 0x20ff (Read)
6. 0x3415 (Write)

Initial TLB

<table>
<thead>
<tr>
<th>VPN</th>
<th>PPN</th>
<th>Valid</th>
<th>Dirty</th>
<th>LRU</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x01</td>
<td>0x11</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>0x00</td>
<td>0x00</td>
<td>0</td>
<td>0</td>
<td>7</td>
</tr>
<tr>
<td>0x10</td>
<td>0x13</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>0x20</td>
<td>0x12</td>
<td>1</td>
<td>0</td>
<td>5</td>
</tr>
<tr>
<td>0x00</td>
<td>0x00</td>
<td>0</td>
<td>0</td>
<td>7</td>
</tr>
<tr>
<td>0x11</td>
<td>0x14</td>
<td>1</td>
<td>0</td>
<td>4</td>
</tr>
<tr>
<td>0xac</td>
<td>0x15</td>
<td>1</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>0xff</td>
<td>0xff</td>
<td>1</td>
<td>0</td>
<td>3</td>
</tr>
</tbody>
</table>

Final TLB

<table>
<thead>
<tr>
<th>VPN</th>
<th>PPN</th>
<th>Valid</th>
<th>Dirty</th>
<th>LRU</th>
</tr>
</thead>
</table>

3 AMAT

Recall that AMAT stands for Average Memory Access Time. The main formula for it is:

\[ \text{AMAT} = \text{Hit Time} + \text{Miss Rate} \times \text{Miss Penalty} \]

In a multi-level cache, there are two types of miss rates that we consider for each level. **Global:** Calculated as the number of accesses that missed at that level divided by the total number of accesses to the cache system. **Local:** Calculated as the number of accesses that missed at that level divided by the total number of accesses to that cache level.

3.1 An L2$, out of 100 total accesses to the cache system, missed 20 times. What is the global miss rate of L2$?
3.2 If L1$ had a miss rate of 50%, what is the local miss rate of L2$?

Suppose your system consists of:

1. An L1$ that has a hit time of 2 cycles and has a local miss rate of 20%
2. An L2$ that has a hit time of 15 cycles and has a global miss rate of 5%
3. Main memory where accesses take 100 cycles

3.3 What is the local miss rate of L2$?

3.4 What is the AMAT of the system?

3.5 Suppose we want to reduce the AMAT of the system to 8 cycles or lower by adding in a L3$. If the L3$ has a local miss rate of 30%, what is the largest hit time that the L3$ can have?

4 Flynn’s Taxonomy

4.1 Explain SISD and give an example if available.

4.2 Explain SIMD and give an example if available.
4.3 Explain MISD and give an example if available.

4.4 Explain MIMD and give an example if available.

5 Data-Level Parallelism

The idea central to data level parallelism is vectorized calculation: applying operations to multiple items (which are part of a single vector) at the same time.
Some machines with x86 architectures have special, wider registers, that can hold 128, 256, or even 512 bits. Intel intrinsics (Intel proprietary technology) allow us to use these wider registers to harness the power of DLP in C code.

Below is a small selection of the available Intel intrinsic instructions. All of them perform operations using 128-bit registers. The type _m128i is used when these registers hold 4 ints, 8 shorts or 16 chars; _m128d is used for 2 double precision floats, and _m128 is used for 4 single precision floats. Where you see “epiXX”, epi stands for extended packed integer, and XX is the number of bits in the integer. “epi32” for example indicates that we are treating the 128-bit register as a pack of 4 32-bit integers.

• __m128i _mm_set1_epi32(int i):
  Set the four signed 32-bit integers within the vector to i.
• __m128i _mm_loadu_si128(__m128i *p):
  Load the 4 successive ints pointed to by p into a 128-bit vector.
• __m128i _mm_mullo_epi32(__m128i a, __m128i b):
  Return vector \((a_0 \cdot b_0, a_1 \cdot b_1, a_2 \cdot b_2, a_3 \cdot b_3)\).
• __m128i _mm_add_epi32(__m128i a, __m128i b):
  Return vector \((a_0 + b_0, a_1 + b_1, a_2 + b_2, a_3 + b_3)\).
• void _mm_storeu_si128(__m128i *p, __m128i a):
  Store 128-bit vector a at pointer p.
• __m128i _mm_and_si128(__m128i a, __m128i b):
  Perform a bitwise AND of 128 bits in a and b, and return the result.
• __m128i _mm_cmpeq_epi32(__m128i a, __m128i b):
  The ith element of the return vector will be set to 0xFFFFFFFF if the ith elements of a and b are equal, otherwise it'll be set to 0.

Notice: On this worksheet, we are using the unaligned versions of the commands that interface with memory (i.e. storeu/loadu vs. store/load). This is because the store/load commands require that the address we are loading at is aligned at some byte boundary (and not necessarily just word-aligned), whereas the unaligned versions have no such requirements. For instance, _mm_store_si128 needs the address to be aligned on a 16-byte boundary (i.e. is a multiple of 16). There is extra work that needs to be done to achieve these alignment requirements, so for this class, we just use the unaligned variants.

5.1

You have an array of 32-bit integers and a 128-bit vector as follows:

```c
int arr[8] = {1, 2, 3, 4, 5, 6, 7, 8};
__m128i vector = _mm_loadu_si128((__m128i *) arr);
```

For each of the following tasks, fill in the correct arguments for each SIMD instruction, and where necessary, fill in the appropriate SIMD function. Assume they happen independently, i.e. the results of Part (a) do not at all affect Part (b).

(a) Multiply vector by itself, and set vector to the result.

```c
vector = ________________(__________________, ________________);
```
(b) Add 1 to each of the first 4 elements of the \(arr\), resulting in \(arr = \{2, 3, 4, 5, 5, 6, 7, 8\}\)

```cpp
__m128i vector.ones = _mm_set1_epi32(1);
__m128i result = _mm_add_epi32(vector.ones, arr);
_mm_storeu_si128(arr, result);
```

(c) Add the second half of the array to the first half of the array, resulting in \(arr = \{1 + 5, 2 + 6, 3 + 7, 4 + 8, 5, 6, 7, 8\} = \{6, 8, 10, 12, 5, 6, 7, 8\}\)

```cpp
__m128i result = _mm_add_epi32(_mm_loadu_si128(arr), arr);
_mm_storeu_si128(arr, result);
```

(d) Set every element of the array that is not equal to 5 to 0, resulting in \(arr = \{0, 0, 0, 0, 0, 6, 7, 8\}\). Remember that the first half of the array has already been loaded into vector.

```cpp
__m128i fives = _mm_set1_epi32(5);
__m128i mask = _mm_or_si128(_mm_setzero_si128(), _mm_cmpl_epi32(arr, fives));
__m128i result = _mm_andnot_si128(mask, arr);
_mm_storeu_si128(arr, result);
```

5.2 SIMD-ize the following function, which returns the product of all of the elements in an array. Things to think about: When iterating through a loop and grabbing elements 4 at a time, how should we update our index for the next iteration? What if our array has a length that isn’t a multiple of 4? Can we always SIMD-ize an entire array? What can we do to handle this tail case?

```
static int product_naive(int n, int *a) {
    int product = 1;
    for (int i = 0; i < n; i++) {
        product *= a[i];
    }
    return product;
}
```

```
static int product_vectorized(int n, int *a) {
    int result[4];
    __m128i prod_v = _mm_loadu_si128(a);
```
for (int i = 0; i < _____; i += ___) { // Vectorized loop
    prod_v = ________________________________________________________________________;
}
__mm_storeu_si128(__________________________, __________________________);
for (int i = ______________; i < ____________; i++) { // Handle tail case
    result[0] *= ________________________;
}
return ______________________________________________________________________________;