1 Pre-Check

This section is designed as a conceptual check for you to determine if you conceptually understand and have any misconceptions about this topic. Please answer true/false to the following questions, and include an explanation:

MapReduce is more general than Spark since it is lower level.

False. Spark is higher level, but you can also do basic map reduce. It is easier to express more complex computations in Spark.

The higher the PUE the more efficient the datacenter is.

False. The ideal PUE is 1.0.

Hamming codes can detect any type of data corruption.

False. They cannot detect all three bit errors.

All RAID levels improve reliability.

False. Raid 0 actually decreases reliability.

2 MapReduce

For each problem below, write pseudocode to complete the implementations. Tips:

- The input to each MapReduce job is given by the signature of map().
- `emit(key k, value v)` outputs the key-value pair (k, v).
- `for var in list` can be used to iterate through Iterables or you can call the `hasNext()` and `next()` functions.
- Usable data types: `int`, `float`, `String`. You may also use lists and custom data types composed of the aforementioned types.
- `intersection(list1, list2)` returns a list of the common elements of `list1`, `list2`. 
Given a set of coins and each coin’s owner in the form of a list of CoinPairs, compute the number of coins of each denomination that a person has.

CoinPair:
  String person
  String coinType

map(CoinPair pair):
  emit(pair, 1)

reduce(CoinPair pair, Iterable<
  int count>):
  total = 0
  for num in count:
    total += num
  emit(pair, total)

Using the output of the first MapReduce, compute each person’s amount of money.

valueOfCoin(String coinType) returns a float corresponding to the dollar value of the coin.

map(tuple<CoinPair, int> output):
  pair, amount = output
  emit(pair.person, 
      valueOfCoin(pair.coinType) * amount)

reduce(String person, Iterable<float> values):
  total = 0
  for amount in values:
    total += amount
  emit(person, total)

3 Spark

Resilient Distributed Datasets (RDD) are the primary abstraction of a distributed collection of items

Transforms RDD → RDD

map(f) Return a new transformed item formed by calling f on a source element.

flatMap(f) Similar to map, but each input item can be mapped to 0 or more output items (so f should return a sequence rather than a single item).

reduceByKey(f) When called on a dataset of (K, V) pairs, returns a dataset of (K, V) pairs where the values for each key are aggregated using the given reduce function f, which must be of type (V, V) → V.

Actions RDD → Value

reduce(f) Aggregate the elements of the dataset regardless of keys using a function f.

Call sc.parallelize(data) to parallelize a Python collection, data.
Given a set of coins and each coin’s owner, compute the number of coins of each denomination that a person has. Then, using the output of the first result, compute each person’s amount of money. Assume \( \text{valueOfCoin}(\text{coinType}) \) is defined and returns the dollar value of the coin.

The type of \( \text{coinPairs} \) is a tuple of (person, coinType) pairs.

1. \( \text{coinData} = \text{sc.parallelize(coinPairs)} \)

\[
\begin{align*}
\text{out1} &= \text{coinData.map}(\lambda (k1, k2): ((k1, k2), 1)) \\
&\quad \quad .\text{reduceByKey}(\lambda v1, v2: v1 + v2)
\end{align*}
\]

\[
\begin{align*}
\text{out2} &= \text{out1.map}(\lambda (k, v): (k[0], v * \text{valueOfCoin}(k[1]))) \\
&\quad \quad .\text{reduceByKey}(\lambda v1, v2: v1 + v2)
\end{align*}
\]

3.2 Given a student’s name and course taken, output their name and total GPA.

\[
\begin{align*}
\text{CourseData:} \\
\quad \text{int courseID} \\
\quad \text{float studentGrade} // a number from 0-4
\end{align*}
\]

The type of \( \text{students} \) is a list of (studentName, courseData) pairs.

1. \( \text{studentsData} = \text{sc.parallelize(students)} \)

\[
\begin{align*}
\text{out} &= \text{studentsData.map}(\lambda (k, v): (k, (v.\text{studentGrade}, 1))) \\
&\quad \quad .\text{reduceByKey}(\lambda v1, v2: (v1[0] + v2[0], v1[1] + v2[1])) \\
&\quad \quad .\text{map}(\lambda (k, v): (k, v[0] / v[1]))
\end{align*}
\]

4 Warehouse-Scale Computing

Sources speculate Google has over 1 million servers. Assume each of the 1 million servers draw an average of 200W, the PUE is 1.5, and that Google pays an average of 6 cents per kilowatt-hour for datacenter electricity.

4.1 Estimate Google’s annual power bill for its datacenters.

\[
1.5 \cdot 10^6 \text{ servers} \cdot 0.2\text{kW/server} \cdot $0.06/\text{kW-hr} \cdot 8760 \text{ hrs/yr} \approx $157.68 \text{ M/year}
\]

4.2 Google reduced the PUE of a 50,000-machine datacenter from 1.5 to 1.25 without decreasing the power supplied to the servers. What’s the cost savings per year?

\[
PUE = \frac{\text{Total building power}}{\text{IT equipment power}} \implies \text{Savings} \propto (PUE_{\text{old}} - PUE_{\text{new}}) \cdot \text{IT equipment power} \\
(1.5 - 1.25) \cdot 50000 \text{ servers} \cdot 0.2\text{kW/server} \cdot $0.06/\text{kW-hr} \cdot 8760\text{hrs/yr} \approx $1.314 \text{ M/year}
\]
5 Hamming ECC

Recall the basic structure of a Hamming code. We start out with some bitstring, and then add parity bits at the indices that are powers of two (1, 2, 8, etc.). We don’t assign values to these parity bits yet. **Note that the indexing convention used for Hamming ECC is different from what you are familiar with.** In particular, the 1 index represents the MSB, and we index from left-to-right. The \( i \)th parity bit \( P_i \) covers the bits in the new bitstring where the *index* of the bit under the aforementioned convention, \( j \), has a 1 at the same position as \( i \) when represented as binary. For instance, 4 is \( \text{0b100} \) in binary. The integers \( j \) that have a 1 in the same position when represented in binary are 4, 5, 6, 7, 12, 13, etc. Therefore, \( P_4 \) covers the bits at indices 4, 5, 6, 7, 12, 13, etc. A visual representation of this is:

![Hamming Code Diagram](https://en.wikipedia.org/wiki/Hamming_code)

5.1 How many bits do we need to add to \( 0011_2 \) to allow single error correction?

3 parity bits

5.2 Which locations in \( 0011_2 \) would parity bits be included?

Using \( P \) to represent parity bits: \( PP0P011_2 \)

5.3 Which bits does each parity bit cover in \( 0011_2 \)?

Parity bit 1: 1, 3, 5, 7
Parity bit 2: 2, 3, 6, 7
Parity bit 3: 4, 5, 6, 7

5.4 Write the completed coded representation for \( 0011_2 \) to enable single error correction. Assume that we set the parity bits so that the bits they cover have even parity.

\( 100011_2 \)

5.5 How can we enable an additional double error detection on top of this?

Add an additional parity bit over the entire sequence.

5.6 Find the original bits given the following SEC Hamming Code: \( 0110111_2 \). Again, assume that the parity bits are set so that the bits they cover have even parity.

Parity group 1: error
Parity group 2: okay
Parity group 4: error
Incorrect bit: \( 1 + 4 = 5 \), change bit 5 from 1 to 0: \( 0110011_2 \) → \( 1011_2 \)

Find the original bits given the following SEC Hamming Code: \( 1001000_2 \)

- Parity group 1: error
- Parity group 2: okay
- Parity group 4: error

Incorrect bit: \( 1 + 4 = 5 \), change bit 5 from 1 to 0: \( 1001100_2 \) → \( 0100_2 \)

6 RAID

Fill out the following table:

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Pro/Good for</th>
<th>Con/Bad for</th>
</tr>
</thead>
<tbody>
<tr>
<td>RAID 0</td>
<td>Split data across multiple disks</td>
<td>No overhead, fast read / write</td>
</tr>
<tr>
<td>RAID 1</td>
<td>Mirrored Disks: Extra copy of data</td>
<td>Fast read / write, Fast recovery</td>
</tr>
<tr>
<td>RAID 2</td>
<td>Hamming ECC: Bit-level striping, one disk per parity group</td>
<td>Smaller overhead</td>
</tr>
<tr>
<td>RAID 3</td>
<td>Byte-level striping with single parity disk.</td>
<td>Smallest overhead to check parity</td>
</tr>
<tr>
<td>RAID 4</td>
<td>Block-level striping with single parity disk.</td>
<td>Higher throughput for small reads</td>
</tr>
<tr>
<td>RAID 5</td>
<td>Block-level striping, parity distributed across disks.</td>
<td>Higher throughput of small writes</td>
</tr>
</tbody>
</table>