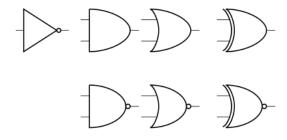
## CS61c Summer 2014 Discussion 10 – Synchronous Digital Systems and Boolean Algebra

July 23, 2014

## 1 Logic Gates

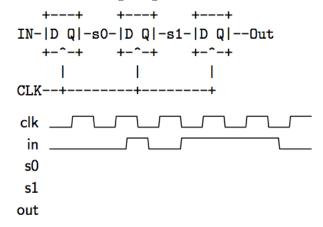
1. Label the following logic gates:



- 2. Convert the following to boolean expressions:
  - (a) NAND
  - (b) XOR
  - (c) XNOR
- 3. Create an AND gate using only NAND gates.
- 4. How many different two-input logic gates can there be? How many n-input logic gates?

## 2 State

1. Fill out the timing diagram for the circuit below:



2. Fill out the timing diagram for the circuit below:

## 3 Boolean Logic

• 
$$A + \bar{A} = 1$$

• 
$$0B = 0$$

$$\bullet \ (A+B)(A+C) = A+BC$$

• 
$$1 + A = 1$$

• 
$$B\bar{B}=0$$

• 
$$\overline{AB} = \overline{A} + \overline{B}$$

$$\bullet \ A + AB = A$$

$$\bullet \ A + \bar{A}B = A + B$$

$$\bullet \ \overline{\mathbf{A} + \mathbf{B}} = \bar{A}\bar{B}$$

1. Minimize the following boolean expressions:

(a) Standard: 
$$(A+B)(A+\bar{B})C$$

(b) Grouping & Extra Terms: 
$$\bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}\bar{C} + A\bar{B}\bar{C} + A\bar{B}\bar{C} + A\bar{B}\bar{C}$$

(c) DeMorgan's: 
$$\overline{{\bf A}(\bar{B}\bar{C}+BC)}$$