

1 Flynn's Taxonomy

- 1.1 Explain SISD and give an example if available

Single Instruction Single Data; each instruction is executed in order, acting on a single stream of data. For example, traditional computer programs.

- 1.2 Explain SIMD and give an example if available

Single Instruction Multiple Data; each instruction is executed in order, acting on multiple streams of data. For example, the SSE Ininsics.

- 1.3 Explain MISD and give an example if available

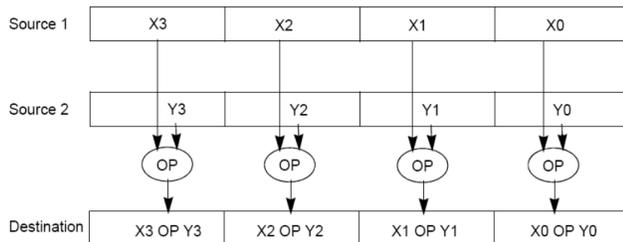
Multiple Instruction Single Data; multiple instructions are executed simultaneously, acting on a single stream of data. There are no good modern examples.

- 1.4 Explain MIMD and give an example if available

Multiple Instruction Multiple Data; multiple instructions are executed simultaneously, acting on multiple streams of data. For example, map reduce or multithreaded programs.

2 Data-Level Parallelism

The idea central to data level parallelism is vectorized calculation: applying operations to multiple items (which are part of a single vector) at the same time.



Some machines with x86 architectures have special, wider registers, that can hold 128, 256, or even 512 bits. Intel intrinsics (Intel proprietary technology) allow us to use these wider registers to harness the power of DLP in C code.

Below is a small selection of the available Intel intrinsic instructions. All of them perform operations using 128-bit registers. The type `_m128i` is used when these registers hold 4 ints, 8 shorts or 16 chars; `_m128d` is used for 2 double precision floats, and `_m128` is used for 4 single precision floats. Where you see “epiXX”, epi stands for extended packed integer, and XX is the number of bits in the integer.

“epi32” for example indicates that we are treating the 128-bit register as a pack of 4 32-bit integers.

- `__m128i _mm_set1_epi32(int i)`:
Set the four signed 32-bit integers within the vector to `i`.
- `__m128i _mm_loadu_si128(__m128i *p)`:
Return the 128-bit vector stored at pointer `p`.
- `__m128i _mm_mullo_epi32(__m128i a, __m128i b)`:
Return vector $(a_0 \cdot b_0, a_1 \cdot b_1, a_2 \cdot b_2, a_3 \cdot b_3)$.
- `__m128i _mm_add_epi32(__m128i a, __m128i b)`:
Return vector $(a_0 + b_0, a_1 + b_1, a_2 + b_2, a_3 + b_3)$
- `void _mm_storeu_si128(__m128i *p, __m128i a)`:
Store 128-bit vector `a` at pointer `p`.
- `__m128i _mm_and_si128(__m128i a, __m128i b)`:
Perform a bitwise AND of 128 bits in `a` and `b`, and return the result.
- `__m128i _mm_cmpeq_epi32(__m128i a, __m128i b)`:
Compare packed 32-bit integers in `a` and `b` for equality, set return vector to `0xFFFFFFFF` if equal and `0` if not.

2.1 You have an array of 32-bit integers and a 128-bit vector as follows:

```
1 int arr[8] = {1, 2, 3, 4, 5, 6, 7, 8};
2 __m128i vector = _mm_loadu_si128((__m128i *) arr);
```

For each of the following tasks, fill in the correct arguments for each SIMD instruction, and where necessary, fill in the appropriate SIMD function. Assume they happen independently, i.e. the results of Part (a) do not at all affect Part (b).

(a) Multiply `vector` by itself, and set `vector` to the result.

```
1 vector = _mm_mullo_epi32(vector, vector);
```

(b) Add 1 to each of the first 4 elements of the `arr`, resulting in `arr = {2, 3, 4, 5, 5, 6, 7, 8}`

```
1 __m128i vector_ones = _mm_set1_epi32(1);
2 __m128i result = _mm_add_epi32(vector, vector_ones);
3 _mm_storeu_si128((__m128i *) arr, result);
```

Notice: In this and the following solutions, we are using the *unaligned* versions of the commands that interface with memory (i.e. `storeu/loadu` vs. `store/load`). This is because the `store/load` commands require that the address we are loading at is aligned at some byte boundary (and not necessarily just word-aligned), whereas the unaligned versions have no such requirements. For instance, `_mm_store_si128` needs the address to be aligned on a 16-byte boundary (i.e. is a multiple of 16). There is extra work that needs to be done to achieve these alignment requirements, so for this class, we just use the unaligned variants.

(c) Add the second half of the array to the first half of the array, resulting

in $\text{arr} = \{1 + 5, 2 + 6, 3 + 7, 4 + 8, 5, 6, 7, 8\} = \{6, 8, 10, 12, 5, 6, 7, 8\}$

```
1 __m128i result = _mm_add_epi32(_mm_loadu_si128((__m128i *) (arr + 4)), vector);
2 _mm_storeu_si128((__m128i*) arr, result);
```

(d) Set every element of the array that is not equal to 5 to 0, resulting in $\text{arr} = \{0, 0, 0, 0, 5, 0, 0, 0\}$. Remember that the first half of the array has already been loaded into vector.

```
1 __m128i fives = _mm_set1_epi32(5);
2 __m128i mask = _mm_cmpeq_epi32(vector, fives);
3 __m128i result = _mm_and_si128(mask, vector);
4 _mm_storeu_si128((__m128i *) arr, result);
5 vector = _mm_loadu_si128((__m128i *) (arr + 4));
6 mask = _mm_cmpeq_epi32(vector, fives);
7 result = _mm_and_si128(mask, vector);
8 _mm_storeu_si128((__m128i *) (arr + 4), result);
```

2.2 Implement the following function, which returns the product of all of the elements in an array.

```
static int product_naive(int n, int *a) {
    int product = 1;
    for (int i = 0; i < n; i++) {
        product *= a[i];
    }
    return product;
}

static int product_vectorized(int n, int *a) {
    int result[4];
    __m128i prod_v = _mm_set1_epi32(1);
    for (int i = 0; i < n/4 * 4; i += 4) { // Vectorized loop
        prod_v = _mm_mullo_epi32(prod_v, _mm_loadu_si128((__m128i *) (a + i)));
    }
    _mm_storeu_si128((__m128i *) result, prod_v);
    for (int i = n/4 * 4; i < n; i++) { // Handle tail case
        result[0] *= a[i];
    }
    return result[0] * result[1] * result[2] * result[3];
}
```