Great Ideas in Computer Architecture

Memory Hierarchy, Fully Associative Caches

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Genius Annotation 2 contributors

‘Clear the cache’ is a way for Kanye to express that he plans to wipe the slate clean and diverge from his aforementioned ‘bad traits’. Cache — which ‘Ye pronounces incorrectly in order to keep the ‘-ay’ rhyme scheme — is synonymous with collection or stash and in modern times most often refers to the cache of a web browser which stores, among other things, saved usernames and passwords and pre-loaded parts of the websites a user visits. Clearing your browsers cache regularly can help your browser run properly and potentially increase your online security.
Review

• Hazards reduce effectiveness of pipelining
  – Cause stalls/bubbles

• Structural Hazards
  – Conflict in use of datapath component

• Data Hazards
  – Need to wait for result of a previous instruction

• Control Hazards
  – Address of next instruction uncertain/unknown
  – Use branch prediction to avoid hazards
Great Idea #3: Principle of Locality/Memory Hierarchy
Agenda

• Memory Hierarchy Overview
• Fully Associative Caches
• Hits, Misses, and Replacement Policies
• FA Cache Example
• Cache Reads and Writes
Storage in a Computer

• Processor
  – Holds data in register files (~ 100 B)
  – Registers accessed on sub-nanosecond timescale

• Memory (“main memory”)
  – More capacity than registers (~ GiB)
  – Access time ~ 50-100 ns

• Hundreds of clock cycles per memory access?!
Processor-Memory Gap

1989 first Intel CPU with cache on chip
1998 Pentium III has two cache levels on chip

μProc 55%/year (2X/1.5yr)

Processor-Memory Performance Gap (grows 50%/year)

“Moore’s Law”

DRAM 7%/year (2X/10yrs)
Library Analogy

• Writing a report on a specific topic
  – e.g. history of the computer (your internet is out)
• While at library, take books from shelves and put them on shelf above your desk
• If need more, go get them and bring back to shelf
  – Don’t return earlier books since might still need them
  – Limited space on shelf; which books do we keep?
• You hope these ~10 books on shelf enough to write report
  – Only 0.00001% of the books in UC Berkeley libraries!
Principle of Locality (1/3)

- **Principle of Locality**: Programs access only a small portion of the full address space at any instant of time
  - **Recall**: Address space holds both code and data
  - Loops and sequential instruction execution mean generally localized code access
  - Stack and Heap try to keep your data together
  - Arrays and structs naturally group data you would access together
Principle of Locality (2/3)

• **Temporal Locality** (locality in time)
  – Go back to the same book on desk multiple times
  – If a memory location is referenced then it will tend to be referenced again soon

• **Spatial Locality** (locality in space)
  – When go to shelves, grab many books on computers since related books are stored together
  – If a memory location is referenced, the locations with nearby addresses will tend to be referenced soon
Principle of Locality (3/3)

• We exploit the principle of locality in hardware via a *memory hierarchy* where:
  – Levels closer to processor are faster (and more expensive per bit so smaller)
  – Levels farther from processor are larger (and less expensive per bit so slower)

• **Goal:** Create the illusion of memory being almost as fast as fastest memory and almost as large as biggest memory of the hierarchy
Memory Hierarchy Schematic

Processor

Level 1
Level 2
Level 3
...
Level n

Smaller, Faster, More expensive

Bigger, Slower, Cheaper

Higher
Lower
Cache Concept

• Memory *Cache*—holds a copy of a subset of main memory
  – We often use $ (“cash”) to abbreviate cache (e.g. D$ = Data Cache, L1$ = Level 1 Cache)

• Modern processors have separate caches for instructions and data, as well as several levels of caches implemented in different sizes

• Implemented with same IC processing technology as CPU and integrated on-chip – faster but more expensive than main memory
Memory Transfer in the Hierarchy

Inclusive: data in L1\$ ⊂ data in L2\$ ⊂ data in MM ⊂ data in SM

Block: Unit of transfer between memory and cache

- Processor
- L1\$ : 4-8 bytes (word)
- L2\$: 8-32 bytes (block)
- Main Memory: 16-128 bytes (block)
- Secondary Memory: 4,096+ bytes (page)
Managing the Hierarchy

- registers ↔ memory
  - By compiler (or assembly level programmer)

- cache ↔ main memory
  - By the cache controller hardware

- main memory ↔ disks (secondary storage)
  - By the OS (virtual memory, which is a later topic)
  - Virtual to physical address mapping assisted by the hardware (TLB)
  - By the programmer (files)
Typical Memory Hierarchy

On-Chip Components

- Control
- Datapath
  - RegFile
- Instr Cache
- Data Cache
- Second Level Cache (SRAM)

Secondary Memory (Disk or Flash)
- Main Memory (DRAM)

Cost/bit: highest to lowest

Speed: (cycles)
- ½’s
- 1’s
- 10’s
- 100’s
- 1,000,000’s

Size: (bytes)
- 100’s
- 10K’s
- M’s
- G’s
- T’s
Jim Gray’s Storage Latency Analogy: How Far Away is the Data?

<table>
<thead>
<tr>
<th>Distance</th>
<th>Storage</th>
<th>Location</th>
<th>Time</th>
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</thead>
<tbody>
<tr>
<td>1 million</td>
<td>Disk</td>
<td>Pluto</td>
<td>2 Years</td>
</tr>
<tr>
<td>100</td>
<td>Memory</td>
<td>Sacramento</td>
<td>1.5 hr</td>
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<tr>
<td>2</td>
<td>On-Chip Cache</td>
<td>This Room</td>
<td>2 min</td>
</tr>
<tr>
<td>1 ns</td>
<td>Registers</td>
<td>My Head</td>
<td>1 min</td>
</tr>
</tbody>
</table>

Jim Gray
Turing Award
B.S. Cal 1966
Ph.D. Cal 1969
Memory Hierarchy Technologies

• Caches use static RAM (SRAM)
  + Fast (typical access times of 0.5 to 2.5 ns)
  + Higher power, expensive
    ($2000 to $4000 per GB in 2011)
  + Static: content will last as long as power is on

• Main memory uses dynamic RAM (DRAM)
  + Lower power, cheaper
    ($20 to $40 per GB in 2011)
  + Slower (typical access times of 50 to 70 ns)
  + Dynamic: needs to be “refreshed” regularly (~ every 8 ms)
Review So Far

• **Goal:** present the programmer with $\approx$ as much memory as the *largest* memory at $\approx$ the speed of the *fastest* memory

• **Approach:** Memory Hierarchy
  – Successively higher levels contain “most used” data from lower levels
  – Exploits *temporal and spatial locality*
  – We will start by studying caches
Agenda

• Memory Hierarchy Overview
• Fully Associative Caches
• Hits, Misses, and Replacement Policies
• FA Cache Example
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Cache Management

• What is the overall organization of blocks we impose on our cache?
  – Where do we put a block of data from memory?
  – How do we know if a block is already in cache?
  – How do we quickly find a block when we need it?
  – When do we replace something in the cache?
General Notes on Caches (1/4)

• **Recall:** Memory is *byte-addressed*

• We haven’t specified the size of our “blocks,” but will usually be multiple of word size (32-bits)
  – How do we access individual words or bytes within a block? OFFSET

• Cache is smaller than memory
  – Can’t fit all blocks at once, so multiple blocks in memory must map to the same “set” in cache INDEX
  – Need some way of identifying which memory block is currently in each cache slot TAG
General Notes on Caches (2/4)

• **Recall:** hold subset of memory in a place that’s faster to access
  – Return data to you when you request it
  – If cache doesn’t have it, then fetches it for you

• Cache must be able to check/identify its current contents

• What does cache initially hold?
  – Garbage! Cache considered “cold”
  – Keep track with **Valid bit**
General Notes on Caches (3/4)

- Effect of block size (K Bytes):
  - Spatial locality dictates our blocks consist of adjacent bytes, which differ in address by 1
  - Offset field: Lowest bits of memory address can be used to index to specific bytes within a block
    - Block size needs to be a power of two (in bytes)
    - # of offset bits = \( \log_2(\text{block size}) \)
General Notes on Caches (4/4)

• Effect of cache size (C Bytes):
  – “Cache Size” refers to total stored data
  – Determines number of blocks the cache can hold (C/K blocks)
  – **Tag field**: Leftover upper bits of memory address determine *which portion of memory* the block came from (identifier)

![Diagram of Tag and Offset fields](image)

- 8 byte block:
  - xx...x000
  - xx...x001
  - ...
  - xx...x111

Same for all bytes in block!
You are given a 256 B cache that holds 8 data blocks. We are working on a 10-bit byte-addressed machine. Which statement is false?

(A) Each data block holds 32 bytes of data

(B) Our tag can be more than 5 bits

(C) All of main memory could fit into four caches

(D) Only one valid copy of a block can be in the cache at any point in time

Always true

# blocks = cache size / block size

# offset bits = \log_2(32) = 5

# tag bits = 10 – 5 = 5

10-bit addresses = 2^{10} bytes of memory

256 B = 2^8 * 2^2 (4 caches) = 2^{10}
Fully Associative Caches

• Each memory block can map *anywhere* in the cache (*fully associative*)
  – Most efficient use of space
  – Least efficient to check

• To check a fully associative cache:
  1) Look at ALL cache slots in sequence
  2) If Valid bit is 0, then ignore
  3) If Valid bit is 1 and Tag matches, then return that data

(In FA cache, Tag is unique to entire cache since 1 large “bucket”, not the case in other designs)

Cache must store valid and tag bits!
Fully Associative Cache
Address Breakdown

- Memory address fields:

- Meaning of the field sizes:
  - Offset bits $\leftrightarrow$ $2^{\text{Offset}}$ bytes per block
    $= 2^{\text{Offset} - 2}$ words per block
  - Tag bits = $A - \text{Offset}$, where $A$ = # of address bits
    ($A = 32$ here)
Question

You are given a 32 bit byte addressed machine. The offset field is 5 bits, but you decide to use only 26 bits to represent the tag. Which of the following statements is true?

(A) Each block can contain more data than if you used all 27 bits.
(B) More bits will need to be stored by the cache
(C) Fewer blocks can be stored in the cache than if you used all 27 bits.
(D) You cannot properly identify what is data block is in the cache.

If I ignore the last tag bit, how can I tell xx...1000 and xx...0000 apart?
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Caching Terminology (1/2)

• When reading memory, 2 things can happen:
  – Cache hit:
    Cache holds a valid copy of the block, so return the desired data
  – Cache miss:
    Cache does not have desired block, so fetch from memory and put in empty (invalid) slot
      • If cache is full you must discard one valid block and replace it with desired data
Block Replacement Policies

• Which block do you replace?
  – Use a cache block replacement policy
  – There are many (most are intuitively named), but we will just cover a few in this class
    http://en.wikipedia.org/wiki/Cache_algorithms#Examples

• Of note:
  – Random Replacement
  – Least Recently Used (LRU): requires some “management bits”
Understanding LRU

• The BEST replacement policy we could have is to replace data we will use farthest in the future
  – Either never use again or use later than everything else
• Unfortunately this isn’t possible
• Instead we approximate using LRU
  – Replace block we used least recently first in the hopes we will use it again later than all other blocks
Caching Terminology (2/2)

• How effective is your cache?
  – Want to max cache hits and min cache misses
  – Hit rate (HR): Percentage of memory accesses in a program or set of instructions that result in a cache hit
  – Miss rate (MR): Like hit rate, but for cache misses
    \[ MR = 1 - HR \]

• How fast is your cache?
  – Hit time (HT): Time to access cache (including Tag comparison)
  – Miss penalty (MP): Time to replace a block in the cache from a lower level in the memory hierarchy
Fully Associative Cache Implementation

• What’s actually in the cache?
  – Each cache slot contains the actual data block (1 block/slot in FA)
    \((8 \times K = 8 \times 2^{\text{Offset}}\) bits)
  – Tag field of address as identifier (Tag bits)
  – Valid bit (1 bit): Whether cache slot was filled in
  – Any necessary replacement management bits (“LRU bits” – variable # of bits stored in each row)

• Total bits in cache
  \[= # \text{ slots} \times (8 \times K + \text{Tag} + 1 + ?)\]
  \[= \left(\frac{C}{K}\right) \times (8 \times 2^{\text{Offset}} + \text{Tag} + 1 + ?) \text{ bits}\]
What does a cache look like?

**Fully Associative Cache**

![Diagram of a Fully Associative Cache]

- **V Tag**
- **Data Block**
- **Tag**
- **Block Offset**
- **HIT**
- **Data Word or Byte**
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FA Cache Examples (1/4)

• Cache parameters:
  – Fully associative, address space of 64B, block size of 1 word, cache size of 4 words, LRU (2 bits)

• Address Breakdown:
  – 1 word = 4 bytes, so Offset = \(\log_2(4) = 2\)
  – \(A = \log_2(64) = 6\) bits, so Tag = 6 – 2 = 4

• Bits in cache
  \[= (4/1) \times (8 \times 2^2 + 4 + 1 + 2) = 156 \text{ bits}\]
FA Cache Examples (1/4)

• Cache parameters:
  – Fully associative, address space of 64B, block size of 1 word, cache size of 4 words, LRU (2 bits)
  – Offset – 2 bits, Tag – 4 bits

- 39 bits per slot, 156 bits to implement with LRU
1) Consider the sequence of memory address accesses

Starting with a cold cache: 0 2 4 10 20 16 0 2

<table>
<thead>
<tr>
<th>Address</th>
<th>Cache State</th>
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<tbody>
<tr>
<td>000000</td>
<td>Miss</td>
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<tr>
<td>000001</td>
<td>Hit</td>
</tr>
<tr>
<td>000010</td>
<td>Miss</td>
</tr>
<tr>
<td>001010</td>
<td>Miss</td>
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</tbody>
</table>

I bring in the memory from the beginning offset of the block.
1) Consider the sequence of memory address accesses:

Starting with a cold cache:

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</table>

- 8 requests, 6 misses – HR of 25%
2) Same requests, but reordered

Starting with a cold cache:

<table>
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# FA Cache Examples (3/4)

2) Same requests, but reordered

Starting with a cold cache:

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### Example 1

**010000**

**16** miss

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### Example 2

**010100**

**20** miss

<table>
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<tbody>
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### Example 3

**001010**

**10** miss

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</table>

### Example 4

**000100**

**04** miss

<table>
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</tr>
</tbody>
</table>

- 8 requests, 5 misses – ordering matters!
3) Original sequence, but double block size

Starting with a cold cache:

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<tr>
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<th></th>
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</tr>
</thead>
<tbody>
<tr>
<td>0 miss</td>
<td>0 000</td>
<td>0x??</td>
<td>0x??</td>
<td>0x??</td>
<td>0x??</td>
<td>0x??</td>
<td>0x??</td>
<td>0x??</td>
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</tbody>
</table>

<table>
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</thead>
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<tr>
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<td>0x??</td>
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<td>0x??</td>
<td>0x??</td>
<td>0x??</td>
<td>0x??</td>
</tr>
</tbody>
</table>

<table>
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<tbody>
<tr>
<td>4 hit</td>
<td>0 000</td>
<td>0x??</td>
<td>0x??</td>
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<td>0x??</td>
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<td>0x??</td>
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</tr>
</tbody>
</table>

|--------|-------|------|------|------|------|------|------|------|------|
3) Original sequence, but double block size

Starting with a cold cache:

```
<p>| | | | | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
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<th></th>
</tr>
</thead>
<tbody>
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<td>8</td>
<td>20</td>
<td>16</td>
<td>0</td>
<td>2</td>
</tr>
</tbody>
</table>
```

- **Miss**
  - 010100
  - 20
  - 000
  - 001

- **Hit**
  - 010000
  - 16
  - 010
  - 001

- 000000
  - 0
  - 010
  - 001

- 000010
  - 2
  - 010
  - 000

• 8 requests, 4 misses – cache parameters matter!
Agenda

• Memory Hierarchy Overview
• Fully Associative Caches
• Hits, Misses, and Replacement Policies
• FA Cache Example
• Cache Reads and Writes
Memory Accesses

• The picture so far:

  ![Diagram of memory access](image)

  - CPU
  - Cache
  - Main Memory

  - Addr
  - hit
  - miss
  - data

• Cache is separate from memory
  - Possible to hold different data? **No, but it can hold a different version**
Cache Reads and Writes

• Want to handle reads and writes quickly while maintaining consistency between cache and memory (i.e. both know about all updates)
  – Policies for cache hits and misses are independent

• Here we assume the use of separate instruction and data caches (I$ and D$)
  – Read from both
  – Write only to D$ (assume no self-modifying code)
Handling Cache Hits

• Read hits (I$ and D$)
  – Fastest possible scenario, so want more of these

• Write hits (D$)
  1) Write-Through Policy: Always write data to cache and to memory (through cache)
     • Forces cache and memory to always be consistent
     • Slow! (every memory access is long)
     • Include a Write Buffer that updates memory in parallel with processor

Assume present in all schemes when writing to memory
Handling Cache Hits

- **Read hits (I$ and D$)**
  - Fastest possible scenario, so want more of these

- **Write hits (D$)**
  
  2) **Write-Back Policy**: Write data only to cache, then update memory when block is removed

  - Allows cache and memory to be inconsistent
  - Multiple writes collected in cache; single write to memory per block
  - **Dirty bit**: Extra bit per cache row that is set if block was written to (is “dirty”) and needs to be written back
Handling Cache Misses

• Miss penalty grows as block size does
• Read misses (I$ and D$)
  – Stall execution, fetch block from memory, put in cache, send requested data to processor, resume
• Write misses (D$)
  – Always have to update block from memory
  – We have to make a choice:
    • Carry the updated block into cache or not?
Write Allocate

- **Write Allocate** policy: when we bring the block into the cache after a write miss
- **No Write Allocate** policy: only change main memory after a write miss
  - Write allocate almost always paired with write-back
    - Eg: Accessing same address many times -> cache it
  - No write allocate typically paired with write-through
    - Eg: Infrequent/random writes -> don’t bother caching it
Updated Cache Picture

- Fully associative, write through
  - Same as previously shown
- Fully associative, write back

<table>
<thead>
<tr>
<th>Slot</th>
<th>V</th>
<th>D</th>
<th>Tag</th>
<th>00</th>
<th>01</th>
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</tr>
</tbody>
</table>

- Write miss procedure (write allocate or not) only affects behavior, not design
Summary

• Memory hierarchy exploits principle of locality to deliver lots of memory at fast speeds
• Fully Associative Cache: Every block in memory maps to any cache slot
  – Offset to determine which byte within block
  – Tag to identify if it’s the block you want
• Replacement policies: random and LRU
• Cache params: block size (K), cache size (C)
• Cache write policies:
  – Write-back (need dirty bit) and write-through