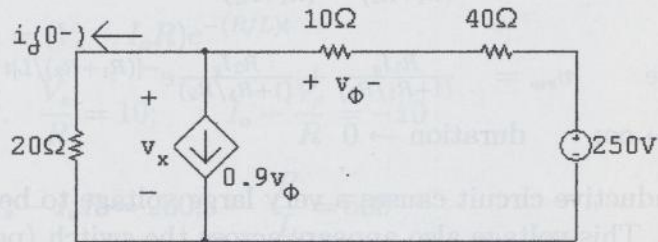


P 7.41 For  $t < 0$



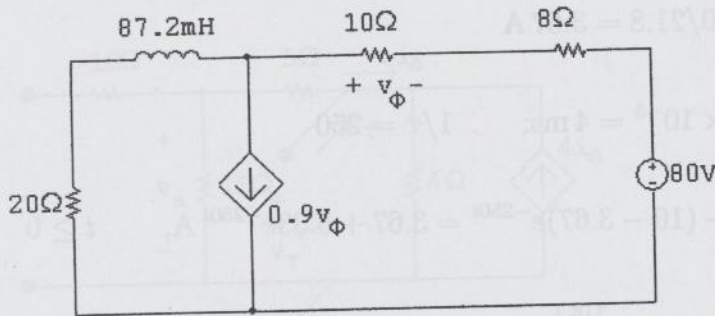
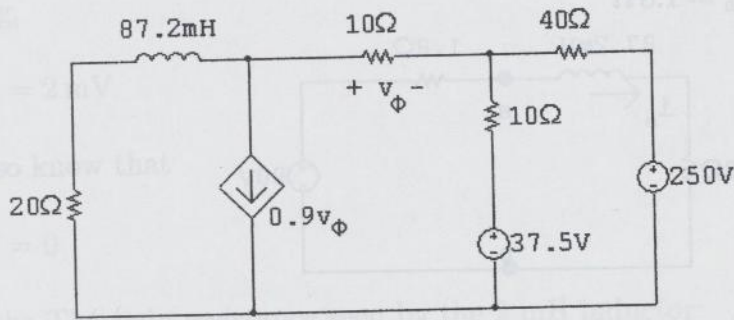
$$\frac{v_x}{20} + 9 \left[ \frac{v_x - 250}{50} \right] + \left[ \frac{v_x - 250}{50} \right] = 0$$

$$\frac{v_x}{20} + 10 \frac{(v_x - 250)}{50} = 0$$

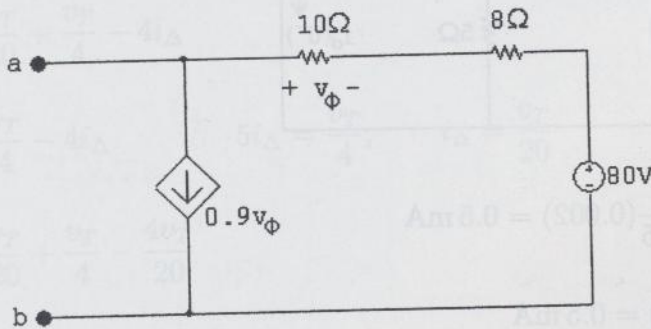
$$5v_x - 5000 + 20v_x = 0; \quad v_x = 200 \text{ V}$$

$$i_o(0^-) = 200/20 = 10 \text{ A}$$

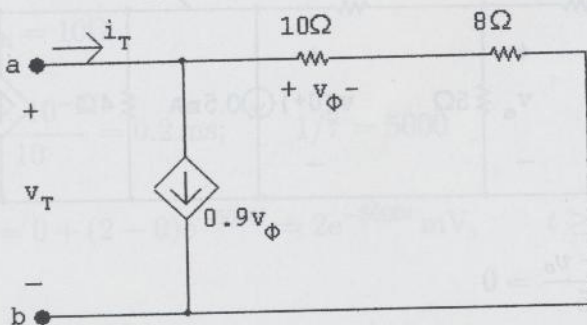
$t > 0$



Find Thévenin equivalent with respect to a, b



$$\frac{V_{Th} - 80}{18} + 9 \frac{(V_{Th} - 80)}{18} = 0 \quad V_{Th} = 80 \text{ V}$$

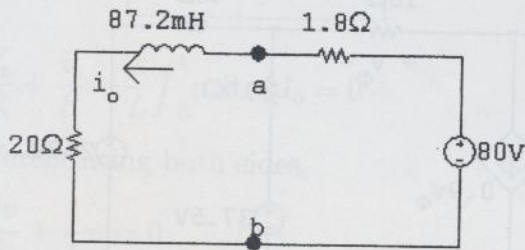


$$v_T = (i_T - 0.9v_\phi)18 = \left[ i_T - 0.9 \left( \frac{10v_T}{18} \right) \right] 18$$

7-42 CHAPTER 7. Response of First-Order RL and RC Circuits

$$v_T = 18i_T - 9v_T \quad \therefore 10v_T = 18i_T$$

$$\frac{v_T}{i_T} = R_{Th} = 1.8 \Omega$$



$$i_o(\infty) = 80/21.8 = 3.67 \text{ A}$$

$$\tau = \frac{87.2}{21.8} \times 10^{-3} = 4 \text{ ms}; \quad 1/\tau = 250$$

$$i_o = 3.67 + (10 - 3.67)e^{-250t} = 3.67 + 6.33e^{-250t} \text{ A}, \quad t \geq 0$$

P 7.91 [a]  $\frac{Cdv_p}{dt} + \frac{v_p - v_b}{R} = 0$ ; therefore  $\frac{dv_p}{dt} + \frac{1}{RC}v_p = \frac{v_b}{RC}$

$$\frac{v_n - v_a}{R} + C \frac{d(v_n - v_o)}{dt} = 0;$$

$$\text{therefore } \frac{dv_o}{dt} = \frac{dv_n}{dt} + \frac{v_n}{RC} - \frac{v_a}{RC}$$

But  $v_n = v_p$

$$\text{Therefore } \frac{dv_n}{dt} + \frac{v_n}{RC} = \frac{dv_p}{dt} + \frac{v_p}{RC} = \frac{v_b}{RC}$$

$$\text{Therefore } \frac{dv_o}{dt} = \frac{1}{RC}(v_b - v_a); \quad v_o = \frac{1}{RC} \int_0^t (v_b - v_a) dy$$

[b] The output is the integral of the difference between  $v_b$  and  $v_a$  and then scaled by a factor of  $1/RC$ .

[c]  $v_o = \frac{1}{RC} \int_0^t (v_b - v_a) dx$

$$RC = (40) \times 10^3 (25) \times 10^{-9} = 1 \text{ ms}$$

$$v_b - v_a = 50 \text{ mV}$$

$$v_o = 50 \int_0^t dx = 50t; \quad 50t_{\text{sat}} = 12; \quad t_{\text{sat}} = 240 \text{ ms}$$

P 9.20 [a]  $Y_2 = \frac{1}{R_2} - \frac{j}{\omega L_2}$

$$Y_1 = \frac{1}{R_1 + j\omega L_1} = \frac{R_1 - j\omega L_1}{R_1^2 + \omega^2 L_1^2}$$

Therefore  $Y_2 = Y_1$  when

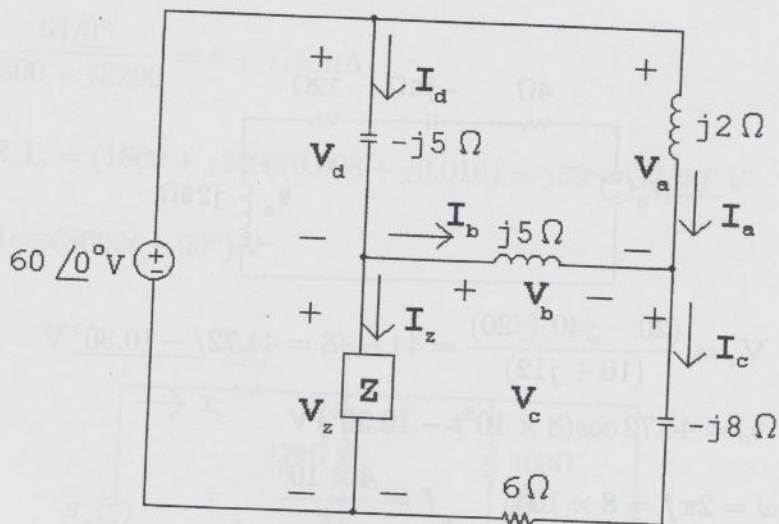
$$R_2 = \frac{R_1^2 + \omega^2 L_1^2}{R_1} \quad \text{and} \quad L_2 = \frac{R_1^2 + \omega^2 L_1^2}{\omega^2 L_1}$$

$$[\mathbf{b}] \quad R_2 = \frac{25 \times 10^6 + 10^8(0.25)}{5 \times 10^3} = 10 \times 10^3$$

$$\therefore R_2 = 10 \text{ k}\Omega$$

$$L_2 = \frac{50 \times 10^6}{10^8(0.5)} = 1 \text{ H}$$

P 9.32



$$\mathbf{V}_a = j2\mathbf{I}_a = j2(-j5) = 10\angle 0^\circ \text{ V}$$

$$\mathbf{V}_c = 60\angle 0^\circ - \mathbf{V}_a = 50\angle 0^\circ \text{ V}$$

$$\mathbf{I}_c = \frac{\mathbf{V}_c}{6 - j8} = \frac{50\angle 0^\circ}{10\angle -53.13^\circ} = 5\angle 53.13^\circ = 3 + j4 \text{ A}$$

$$\mathbf{I}_b = \mathbf{I}_c - \mathbf{I}_a = 3 + j4 - (-j5) = 3 + j9 \text{ A} = 9.49\angle 71.57^\circ \text{ A}$$

$$\mathbf{V}_b = \mathbf{I}_b(j5) = (3 + j9)(j5) = -45 + j15 \text{ V}$$

$$\mathbf{V}_z = \mathbf{V}_b + \mathbf{V}_c = -45 + j15 + 50 + j0 = 5 + j15 \text{ V}$$

$$\mathbf{V}_d + \mathbf{V}_z = 60\angle 0^\circ; \quad \therefore \mathbf{V}_d = 60 - 5 - j15 = 55 - j15 \text{ V}$$

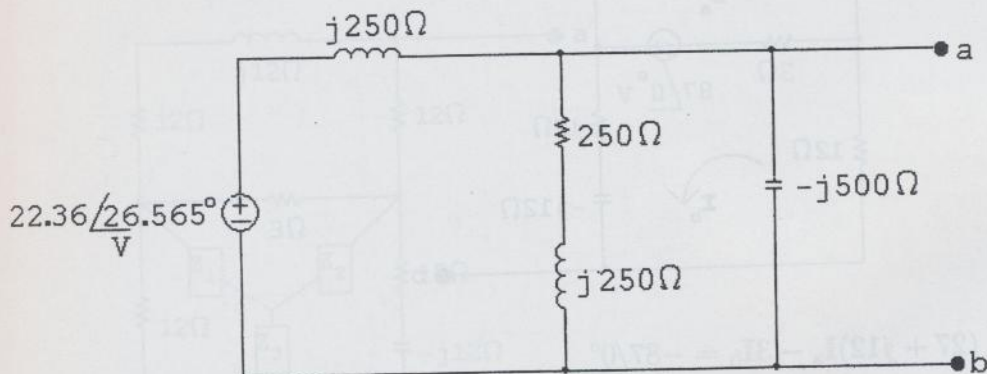
$$\mathbf{I}_d = \frac{\mathbf{V}_d}{-j5} = 3 + j11 \text{ A}$$

$$\mathbf{I}_z = \mathbf{I}_d - \mathbf{I}_b = 3 + j11 - 3 - j9 = j2 \text{ A}$$

$$\mathbf{Z} = \frac{\mathbf{V}_z}{\mathbf{I}_z} = \frac{5 + j15}{j2} = 7.5 - j2.5 \Omega$$

P 9.42 [a]  $j\omega L = j(5000)(50) \times 10^{-3} = j250 \Omega$

$$\frac{1}{j\omega C} = -j \frac{1}{(5000)(400 \times 10^{-9})} = -j500 \Omega$$



Using voltage division,

$$V_{ab} = \frac{(250 + j250) \parallel (-j500)}{j250 + (250 + j250) \parallel (-j500)} (22.36 \angle 26.565^\circ) = 20 \angle 0^\circ$$

$$V_{Th} = V_{ab} = 20 \angle 0^\circ \text{ V}$$

[b] Remove the voltage source and combine impedances in parallel to find

$$Z_{Th} = Z_{ab}:$$

$$Y_{ab} = \frac{1}{j250} + \frac{1}{250 + j250} + \frac{1}{-j500} = 2 - j4 \text{ mS}$$

$$Z_{Th} = Z_{ab} = \frac{1}{Y_{ab}} = 100 + j200 \Omega$$

[c]

