

# EE 105 | Discussion 3

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# Discussion Outline

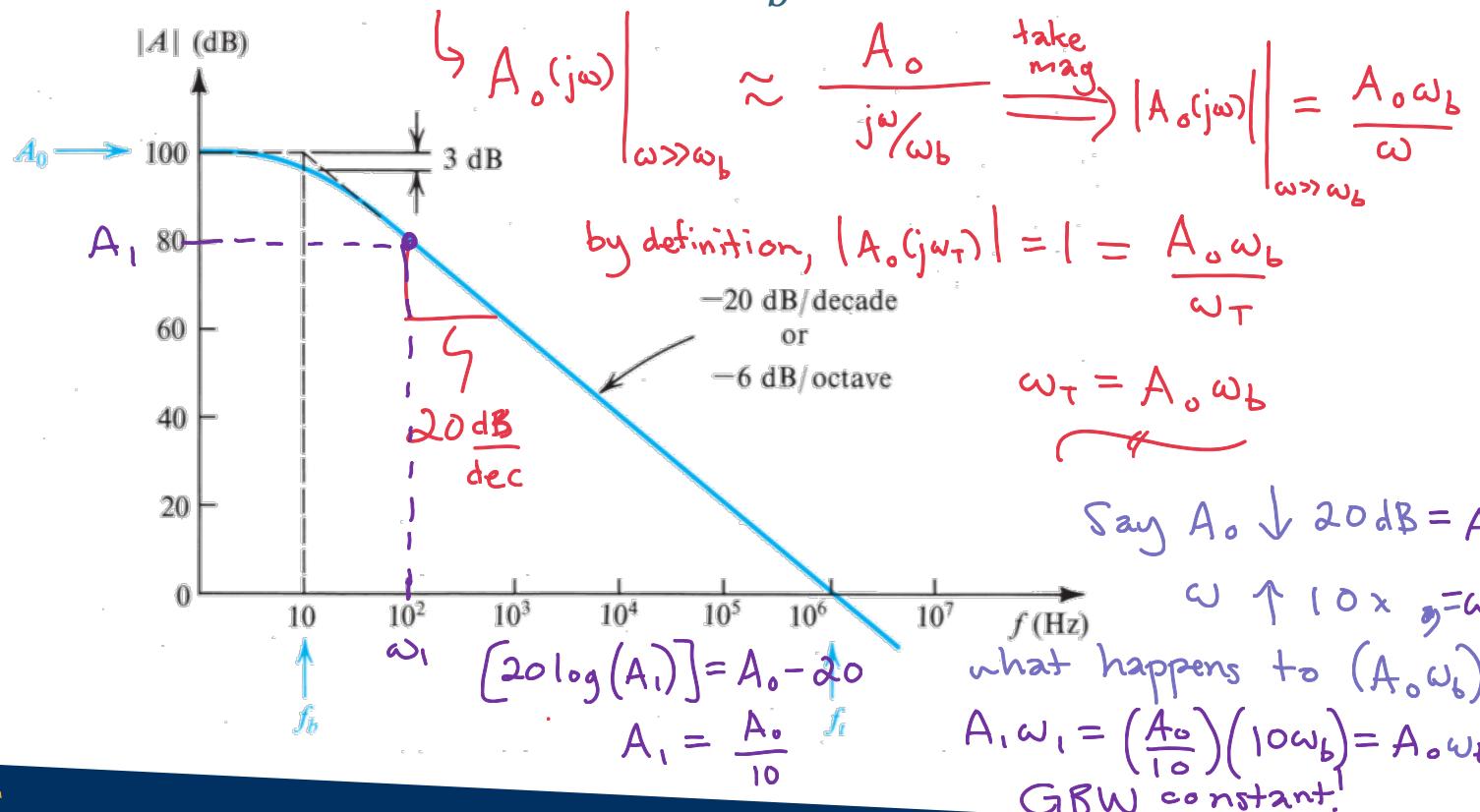
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- Finite gain & bandwidth
- Gain error
- Introduce slew rate, offset voltage & input bias nonidealities

# Nonideal Op Amps | Finite Gain & Bandwidth

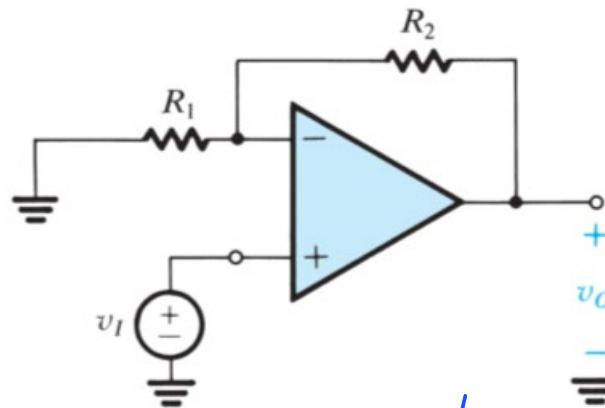
- Op amps without any feedback have open-loop gain  $A_o(s)$

$$A_o(s) = \frac{A_o}{1 + \frac{s}{\omega_b}} \quad (\text{Low pass STC})$$



# Nonideal Op Amps | Finite Gain & Bandwidth

- At DC,  $|A_o(s)| = A_o$ , which is finite in real op amps
- When we close the loop, this results in a deviation from the expected gain



$$\text{RECALL: } A_{v, \text{ideal}} = \frac{v_o}{v_i} \left|_{A_o=\infty} \right. = 1 + \frac{R_2}{R_1}$$

$$v_o = A_o (v^+ - v^-)$$

$$= A_o \left( v_i - \frac{R_1}{R_1 + R_2} v_o \right)$$

$$v_o \left( 1 + \frac{R_1}{R_1 + R_2} A_o \right) = A_o v_i$$

$$A_{v, \text{actual}} = \frac{v_o}{v_i} = \frac{A_o}{1 + \frac{R_1}{R_1 + R_2} A_o} = \frac{1 + R_2/R_1}{1 + \frac{1 + R_2/R_1}{A_o}}$$

$$v^+ = v_i$$

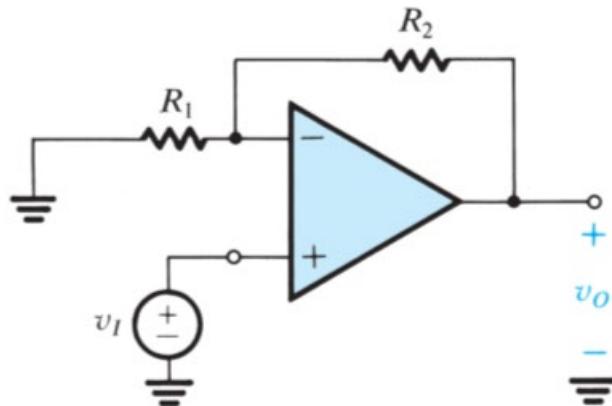
$$v^- = \frac{R_1}{R_1 + R_2} v_o$$

equal when  $A_o \rightarrow \infty$

$$A_{v, \text{actual}} = \frac{A_{v, \text{ideal}}}{1 + A_{v, \text{ideal}}/A_o}$$

$$\text{Define gain error, } \epsilon = \frac{|A_{v, \text{actual}} - A_{v, \text{ideal}}|}{A_{v, \text{ideal}}} \times 100$$

# Nonideal Op Amps | Finite Gain & Bandwidth



can swap & remove abs. val. b/c  $A_{v,ideal} > A_{v,act.}$

$$\epsilon = \frac{|A_{v,actual} - A_{v,ideal}|}{A_{v,ideal}} \times 100$$

$$\epsilon = \left( A_{v,id.} - \frac{A_{v,id.}}{1 + A_{v,id.}/A_o} \right) \left( \frac{1}{A_{v,id.}} \right) \times 100$$

$$= \frac{(1 + A_{v,id.}/A_o) - 1}{1 + A_{v,id.}/A_o} \times 100$$

$$= \frac{A_{v,id.}}{A_o + A_{v,id.}} \times 100$$

$$\% \epsilon_{gain} = \frac{(1 + R_2/R_1)}{A_o + (1 + R_2/R_1)} \times 100$$

X

# Nonideal Op Amps | Slew Rate

Slew rate (SR) refers to the max rate of change of an amplifier's output voltage

$$SR \triangleq \left. \frac{dv_o}{dt} \right|_{max}$$

This imposes two limitations on the output

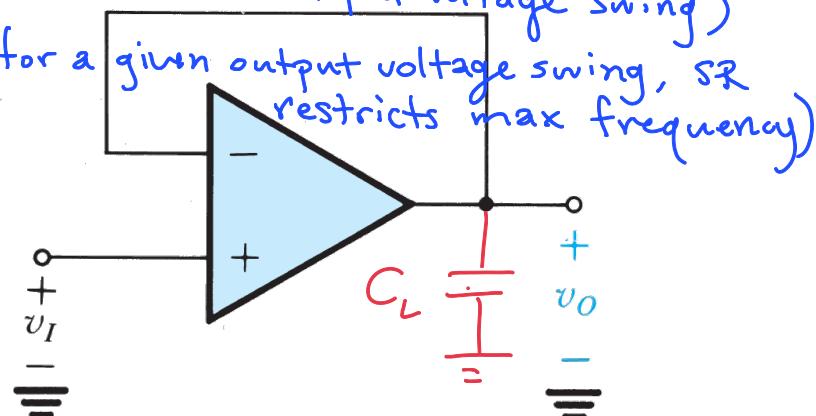
1. Amplitude (i.e.  $\Delta V_o$ )  $\rightarrow \Delta V_o \leq SR \cdot \Delta t$  (for a given frequency, SR restricts max output voltage swing)
2. Frequency (i.e.  $\Delta t$ )  $\rightarrow \Delta t \geq \frac{\Delta V_o}{SR}$  (for a given output voltage swing, SR restricts max frequency)

Say op amp has max output current

$i_{o,max}$ . For a given  $C_L$ :

$$i_{o,max} = C_L \left( \frac{dv_o}{dt} \right)_{max}$$

$$\therefore SR = \frac{i_{o,max}}{C_L}$$



Note that this  $i_{o,max}$  is usually dictated by your amplifier's bias current

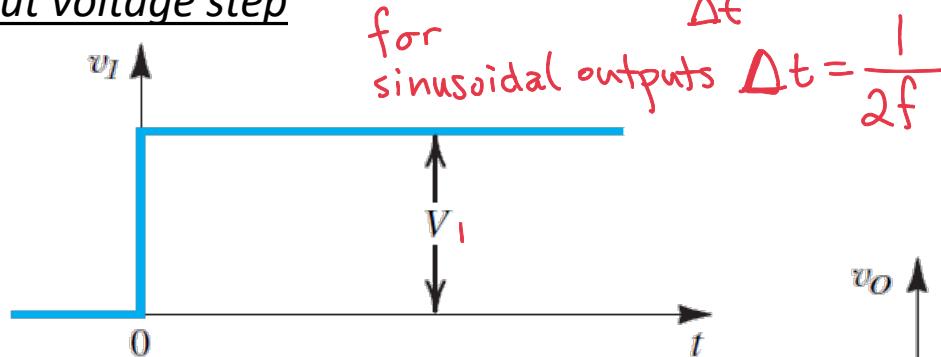
# Nonideal Op Amps | Slew Rate

Limitation #1: Amplitude (i.e.,  $\Delta V_o$ )

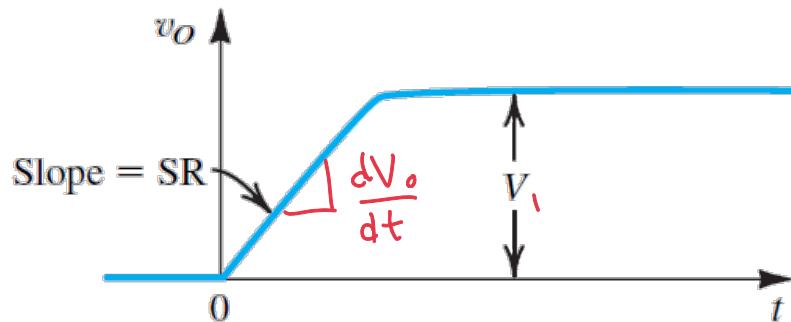
$$\Delta V_o \leq SR \cdot \Delta t$$



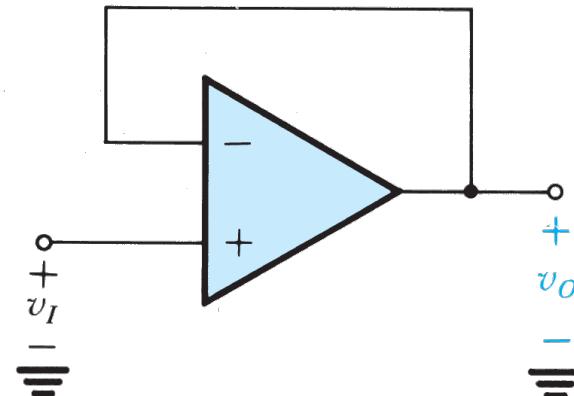
Input voltage step



Output voltage waveform, SR-limited

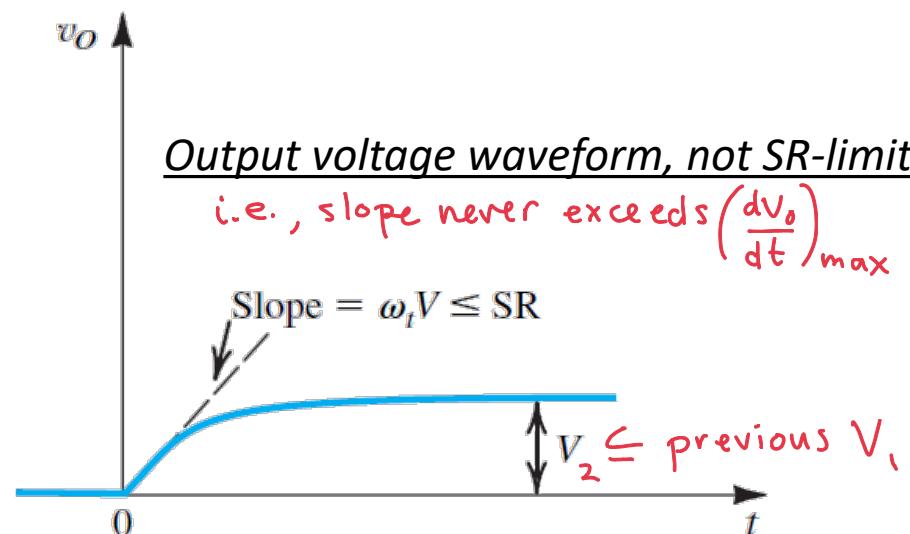


**Unity-gain buffer**



Output voltage waveform, not SR-limited

i.e., slope never exceeds  $\left(\frac{dV_o}{dt}\right)_{\max}$

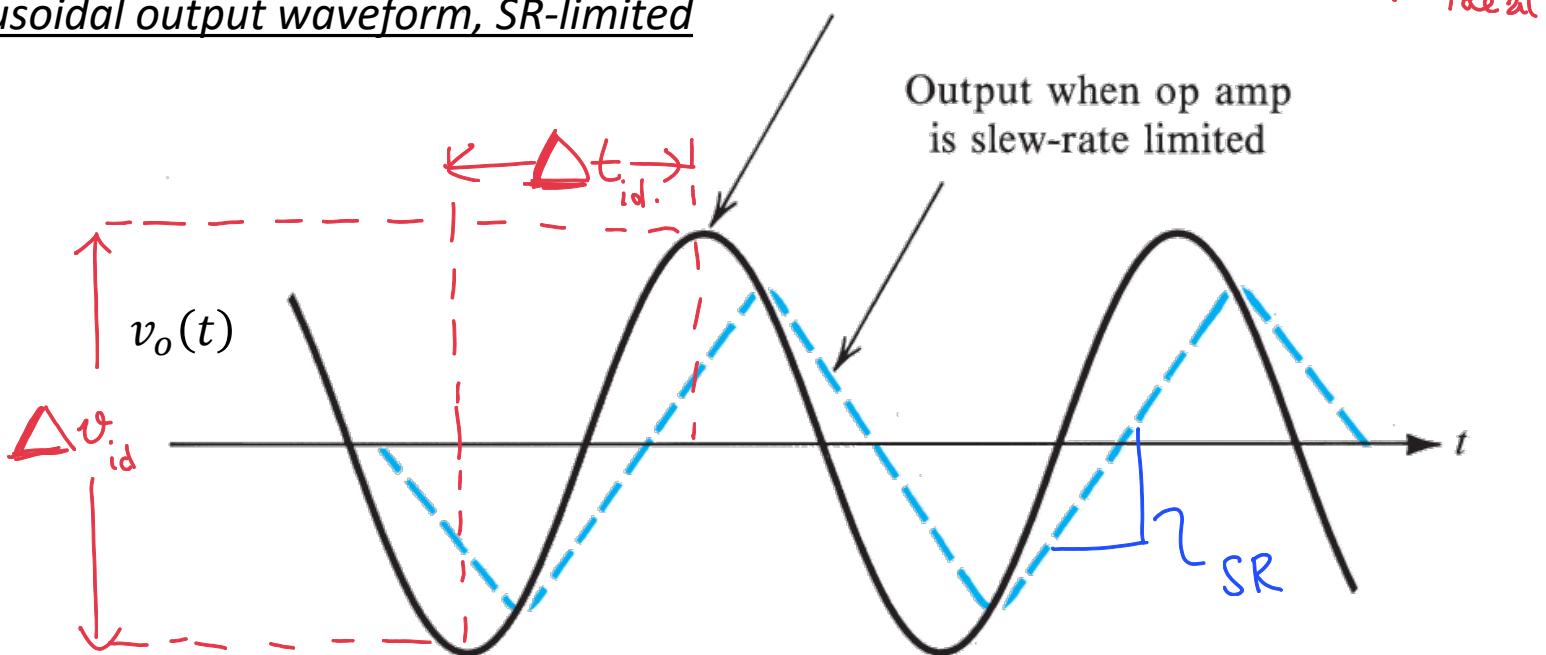


# Nonideal Op Amps | Slew Rate

Limitation #2: Frequency (i.e.  $\Delta t$ )  $\rightarrow \Delta t \geq \frac{\Delta V_o}{SR}$

$$\Delta t_{\text{ideal}} = \frac{1}{2f}$$

Sinusoidal output waveform, SR-limited



$$SR < \frac{\Delta v_{o,\text{id}}}{\Delta t_{\text{id}}}$$

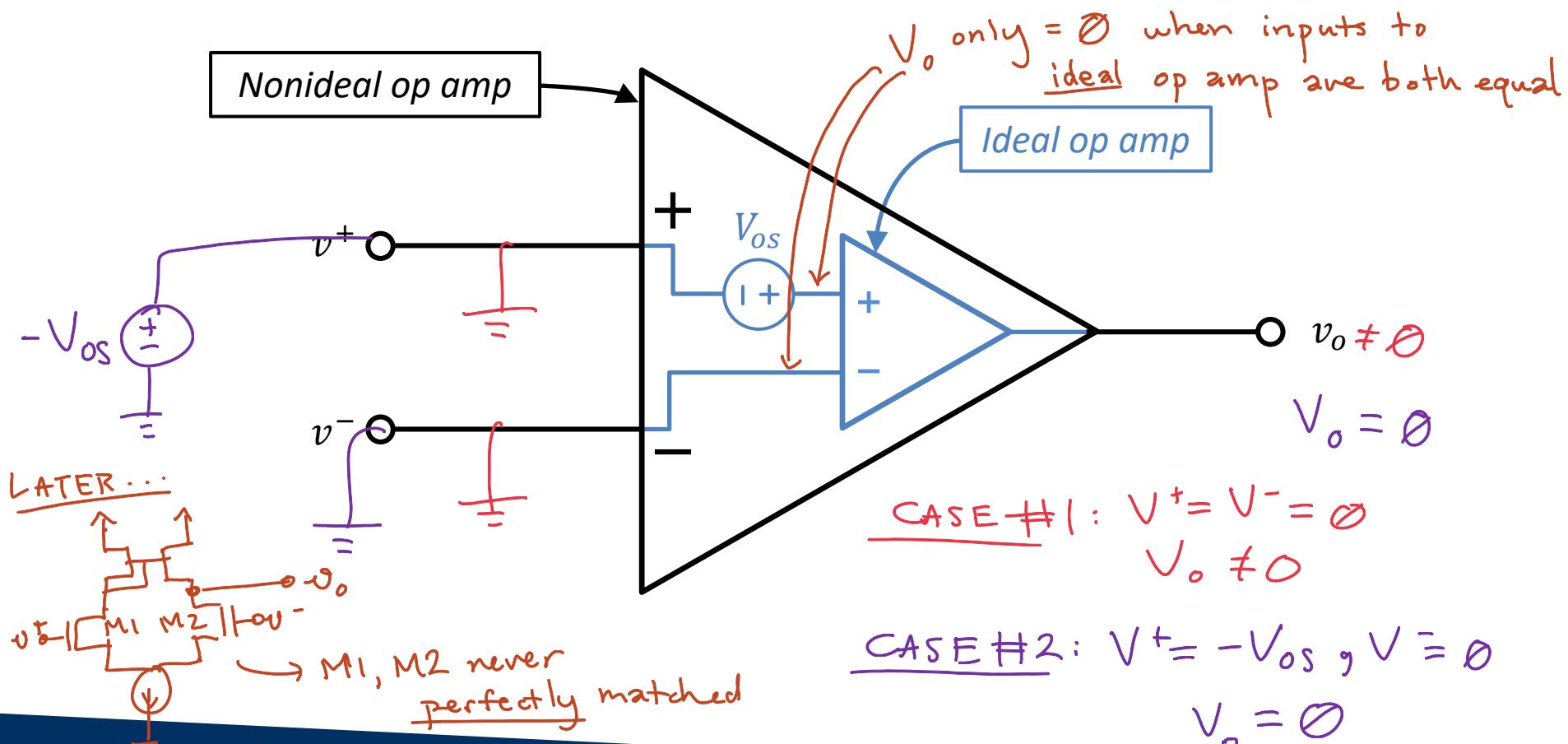
# Nonideal Op Amps | Offset Voltage

$$V_o = A_o (v^+ - v^-)$$

(finite) (infinite) (zero)

Recall our qualitative understanding for why  $v^+ = v^-$  when  $A_o = \infty$

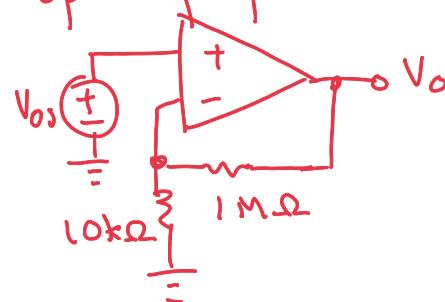
- In actuality, setting both  $v^+$  &  $v^- = 0$  will result in a nonzero  $V_o$
- This is due to mismatches in the op amp *differential pair* (we'll see this later)



# Nonideal Op Amps | Offset Voltage

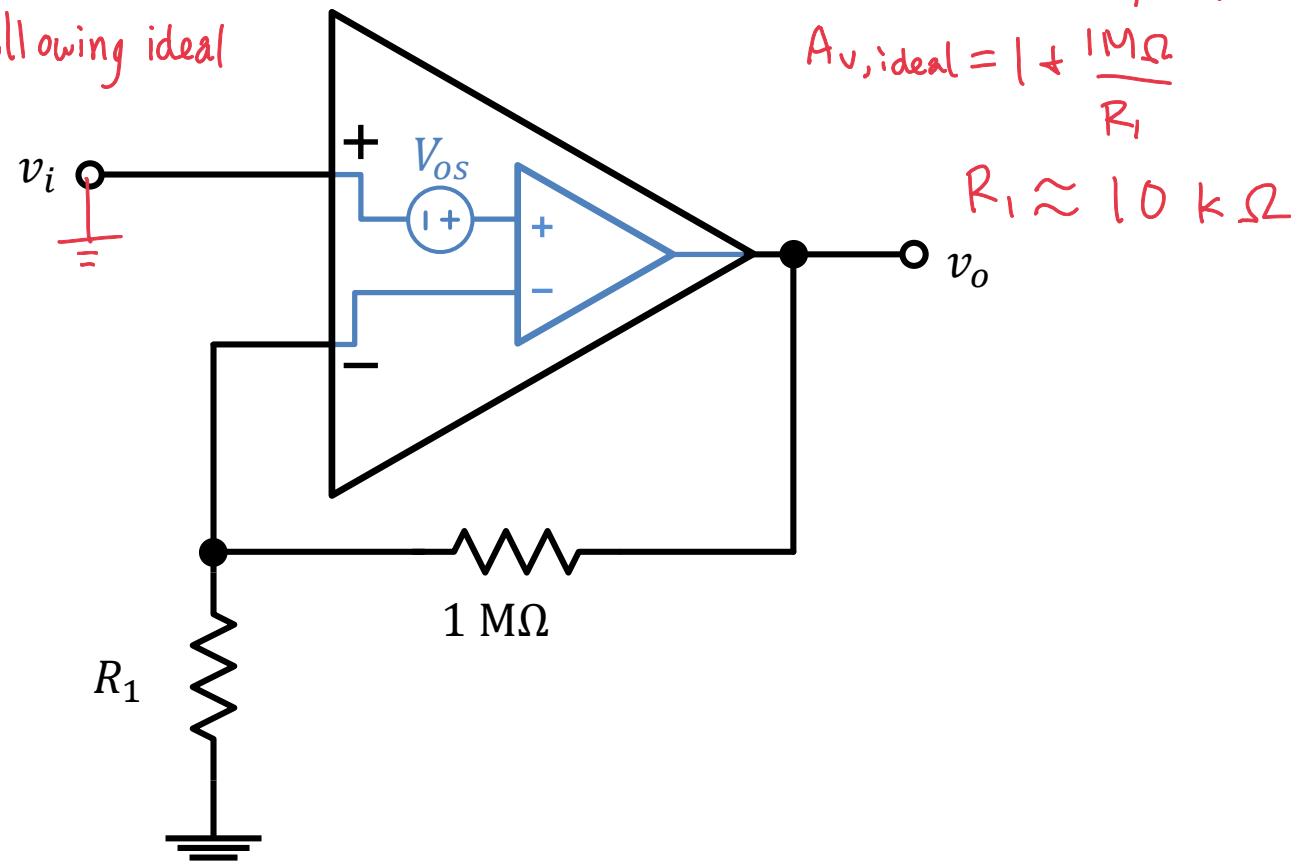
- Now consider an input offset voltage,  $V_{OS} = \pm 2 \text{ mV}$
- What's the largest possible  $v_o$  when  $v_i$  is 0 V? Given  $A_{V,ideal} = 100 \frac{V}{V}$

This looks just like the following ideal op amp problem:



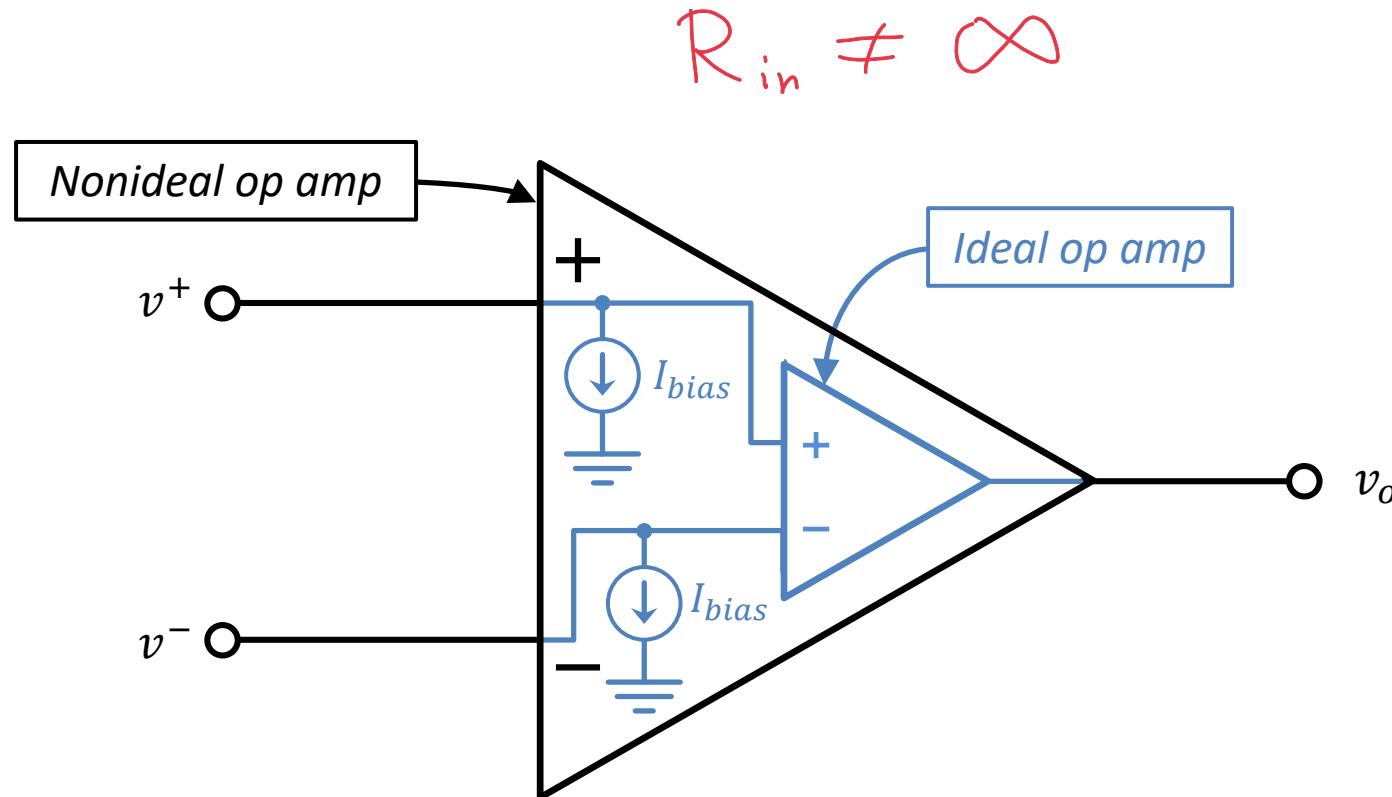
$$|V_o| = (100 \frac{V}{V}) |V_{OS}|$$
$$= (10^2) (2 \times 10^{-3})$$

$$V_o = \pm 200 \text{ mV}$$



# Nonideal Op Amps | Input Bias Current

If  $i^+, i^- \neq 0$ , what's another way to describe this nonideality?



# Nonideal Op Amps | Input Bias Current

- The circuit below has a closed-loop gain of 100 V/V

- Input bias current,  $I_{bias} = 200 \text{ nA}$

- What's  $v_o$  when  $v_i$  is 0 V?

$$v^+ = v_i \quad (\text{ignoring } V_{os})$$

$R_1$  grounded on both sides,  $I_i = 0$

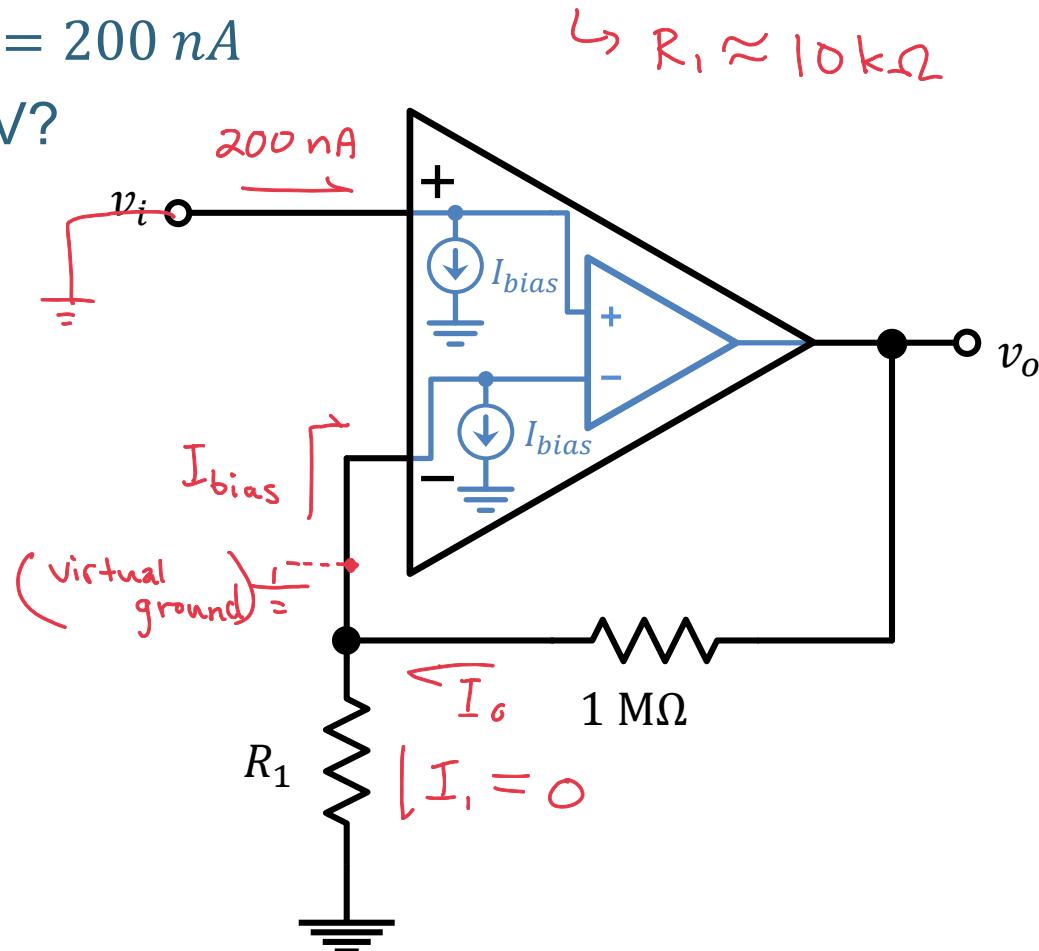
$$\hookrightarrow I_o = I_{bias}$$

$$\therefore v_o = I_{bias} (1\text{M}\Omega)$$

$$= (2 \times 10^{-7} \text{ A})(10^6 \Omega)$$

$$v_o = 200 \text{ mV}$$

$\overbrace{\hspace{10em}}$



# Nonideal Op Amps | Bias Current Compensation

- Find the value of  $R_b$  required to null the effects of  $I_{bias}$  on  $v_o$

To get  $v_o = 0V$ ,

$$v^- = -I_o R_2$$

(b/c  $v_o = v^- + I_o R_2$ )

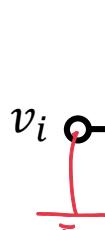
Assuming  $v^- = v^+$ , we need  $v^+ = -I_o R_2$

$$v^+ = v_i - I_b R_b = -I_b R_b = -I_o R_2 \quad (\text{!})$$

(ii) into (i)

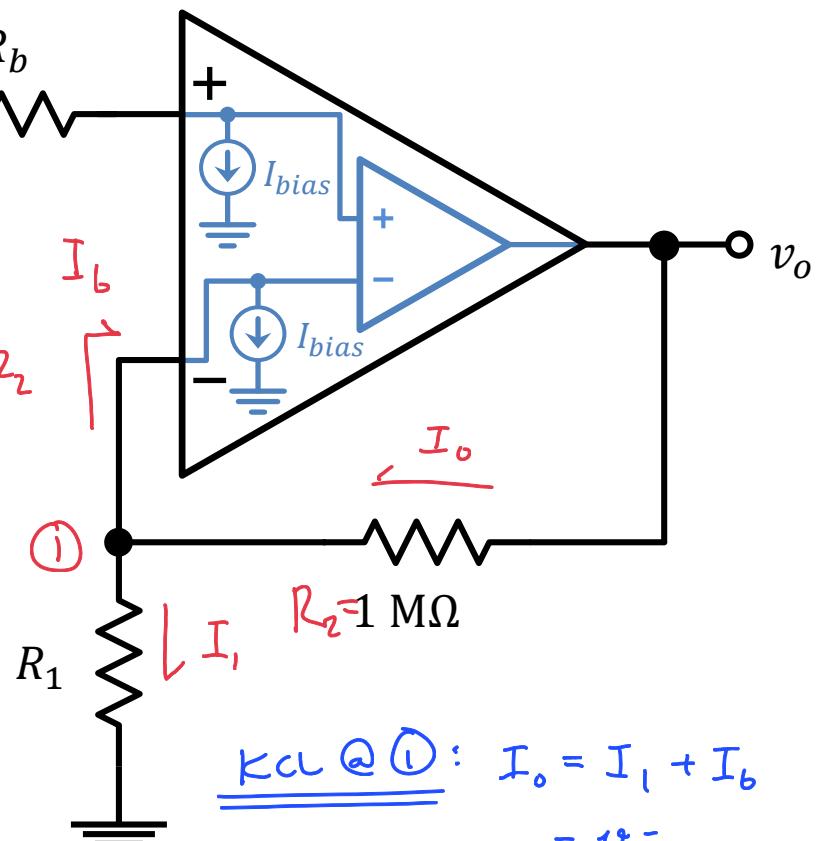
$$-I_b R_b = -I_b \left( \frac{R_1}{R_1 + R_2} \right) R_2$$

$$R_b = \frac{R_1 R_2}{R_1 + R_2} = R_1 \parallel R_2$$



$I_b$

$R_b$



(i)

$R_1$

$I_1$

$R_2 = 1 \text{ M}\Omega$

KCL @ (i):  $I_o = I_1 + I_b$

$$= \frac{v^-}{R_1} + I_b$$

$$= -I_o \frac{R_2}{R_1} + I_b$$

$$(ii) I_o = I_b \left( \frac{R_1}{R_1 + R_2} \right)$$

$$\Leftrightarrow I_o = -I_o \frac{R_2}{R_1} + I_b$$