

Lecture 16: Bipolar Junction Transistors (BJTs) I

- **Announcements:**
- HW#6 online soon and due Friday two weeks from now via Gradescope
- Lab#3 continues next week
 - ↳ Prelab due before lab next week
- Midterm 1 on Friday, Oct. 11
 - ↳ We have 7-9 p.m., 160 Kroeber Hall
 - ↳ For the review session, please post on Piazza specific problems you would like covered
- My Monday Office Hours will move to 5-6 p.m. on Oct. 14 and thereafter
- I am traveling today and will still be gone Monday, Oct. 7
 - ↳ This lecture is pre-recorded as will be the Monday lecture
 - ↳ I will be back on Wednesday, Oct. 9

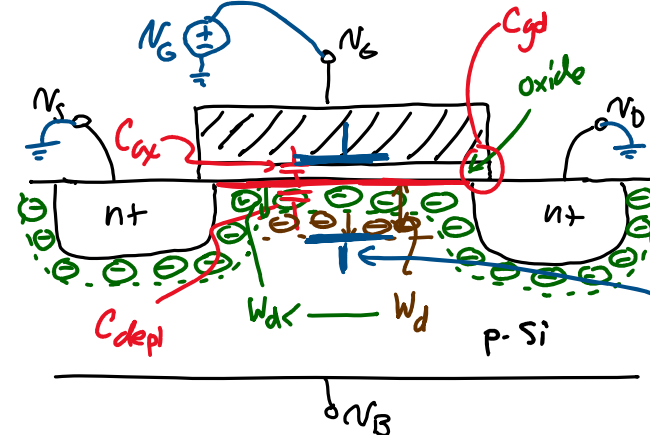
Lecture Topics:

- ↳ MOS CV Curve
- ↳ Bipolar Junction Transistor (BJT)
 - Regions of Operation
 - Cutoff
 - Forward-Active

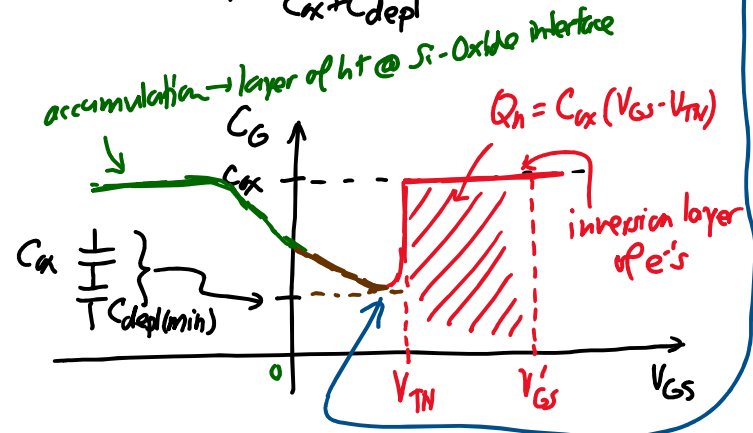
Last Time:

- Almost finished with MOS physics (for now)
- Now, finish it, then proceed with BJTs

MOSFET CV Curves

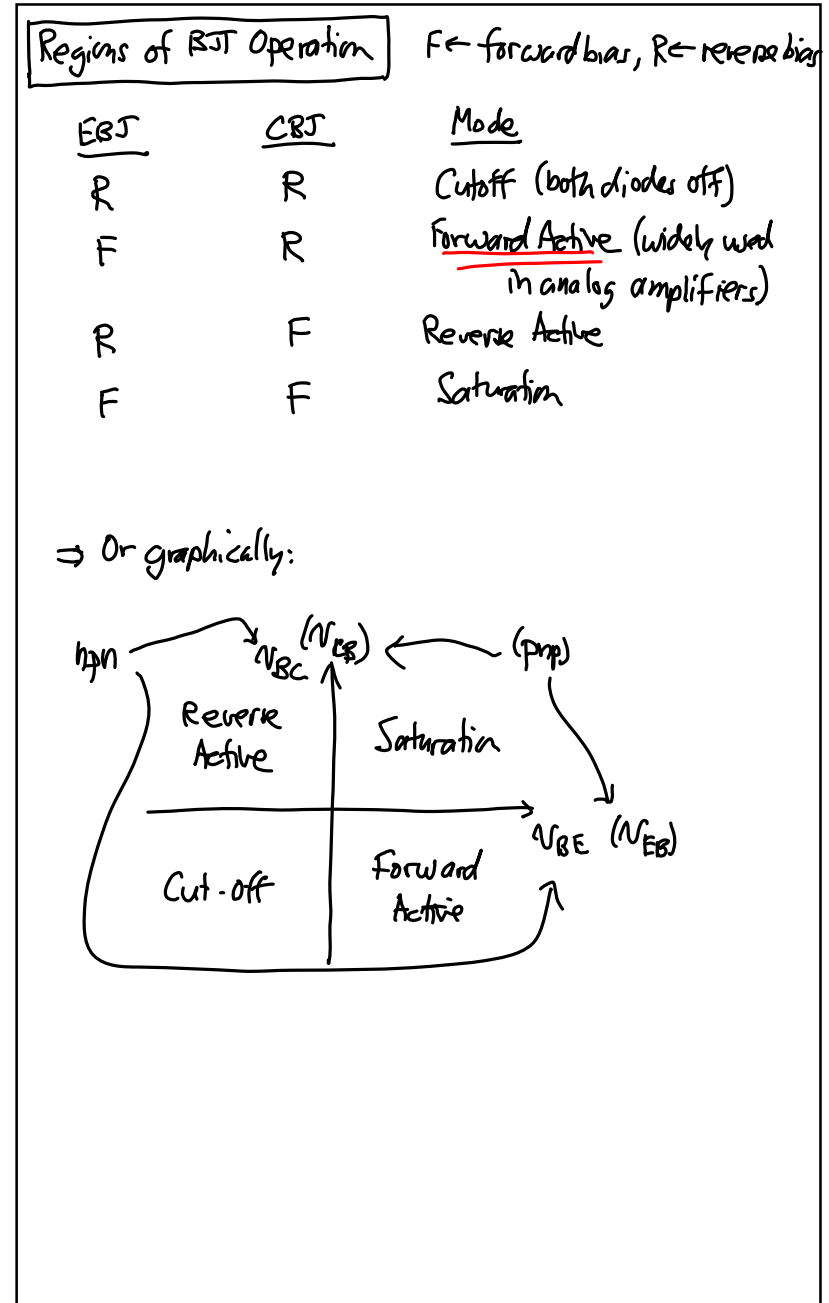
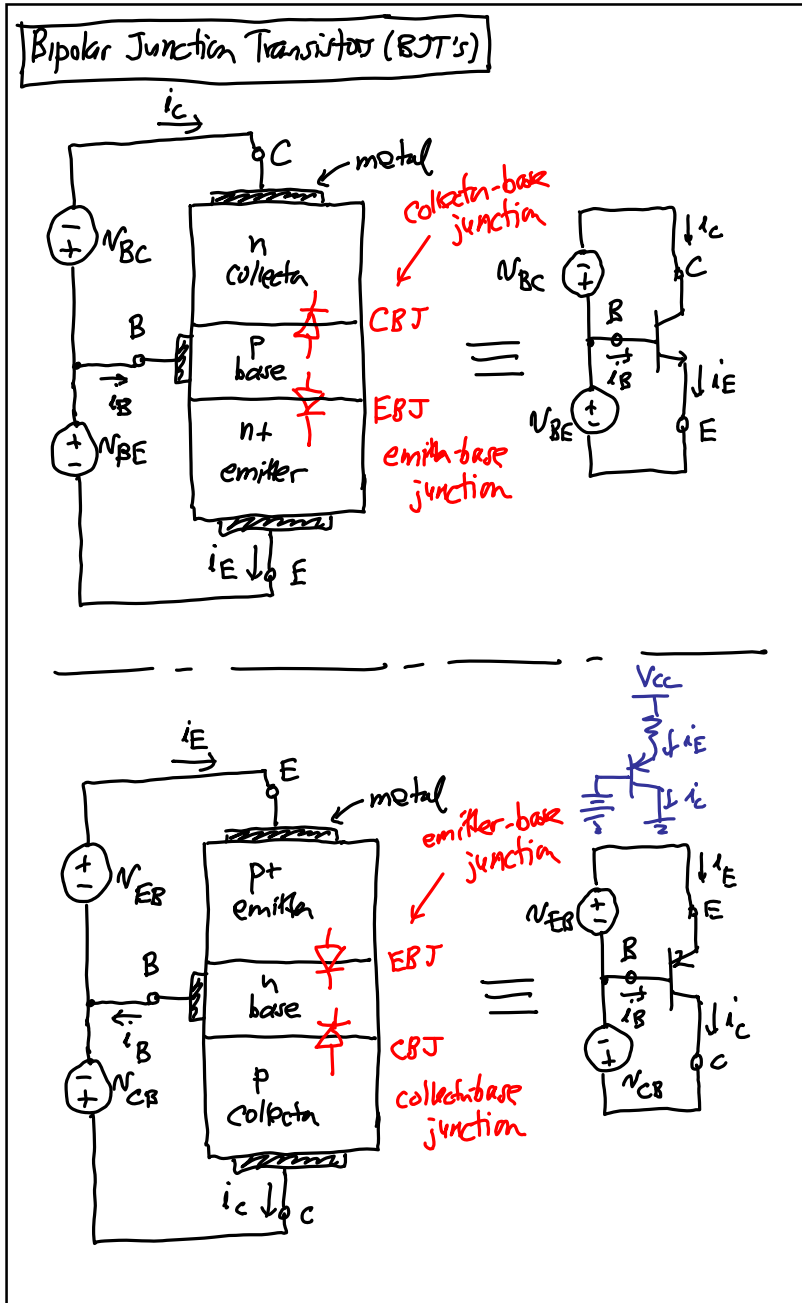


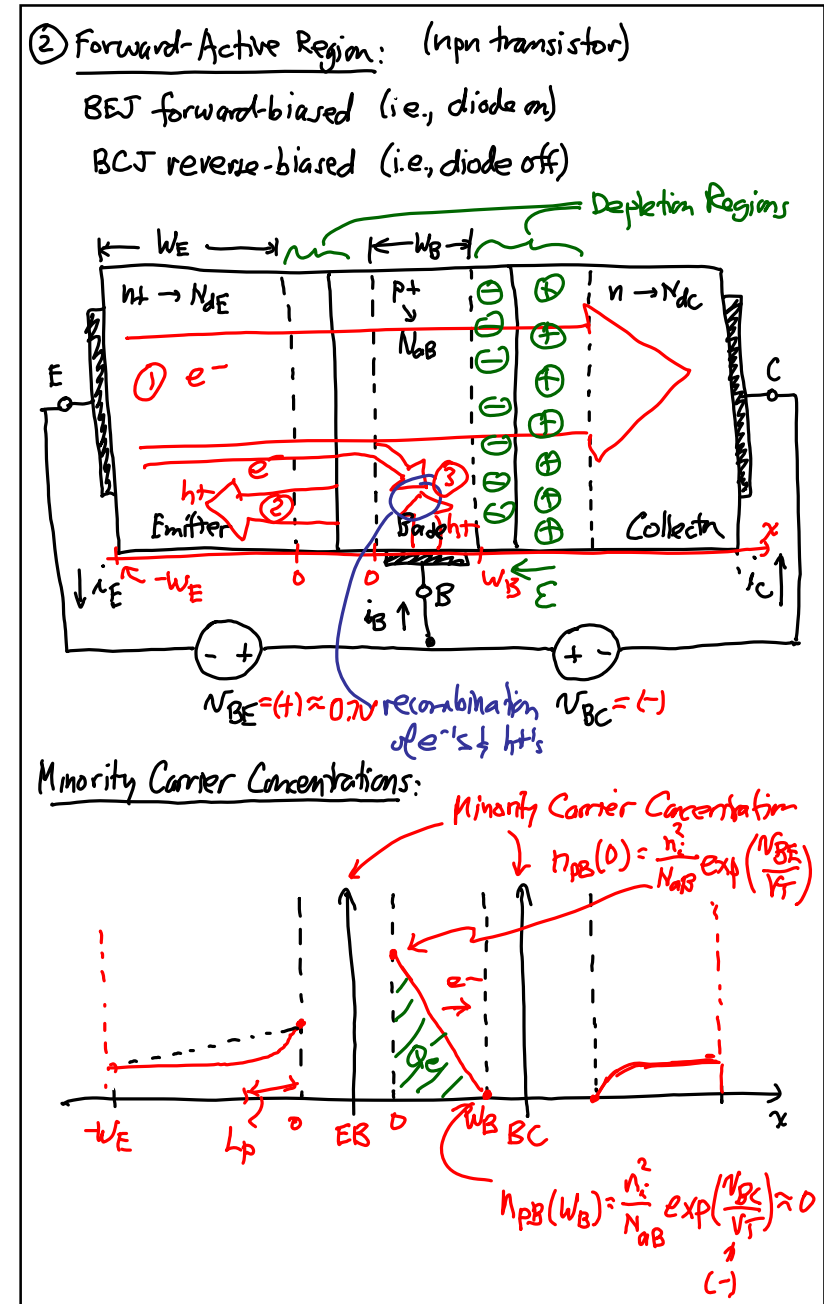
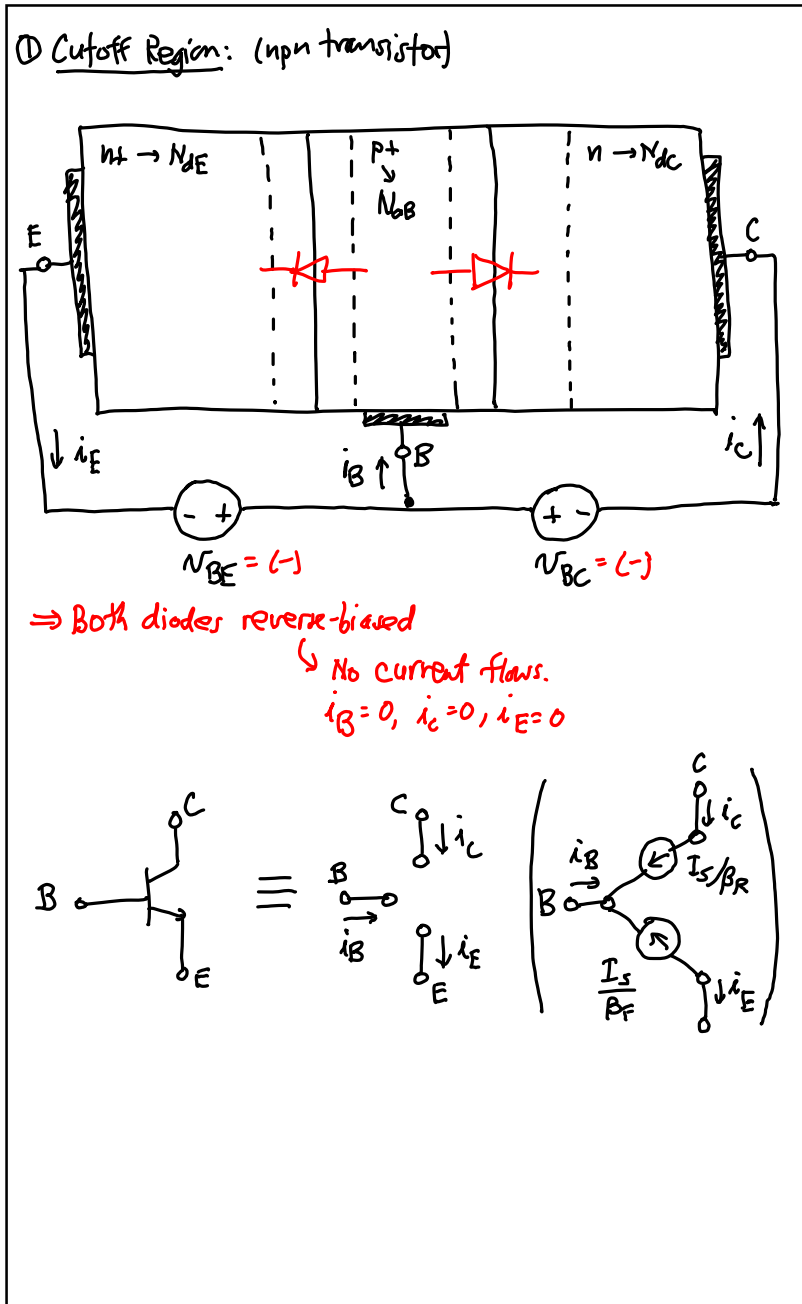
$$C_{ox} \text{ series w/ } C_{depl} = \frac{C_{ox} C_{depl}}{C_{ox} + C_{depl}}$$



$$C_G = \frac{dQ}{dV} = \frac{dQ_n}{dV} \rightarrow \text{when inversion charge can keep up w freq.}$$

$$\Rightarrow C_G = f(V_{GS})$$





BEJ Forward-Biased:

- ⇒ get diffusion current as in diode
- ⇒ forward-biasing of a BJT → three current components.

① e⁻s injected from emitter to base:

$$I_{nB} = -A J_{nB}^{diff}$$

② h⁺s injected from base to emitter:

$$I_{pE} = -A J_{pE}^{diff}$$

③ recombination of e⁻s & h⁺s in the base

$$I_{rB} \propto \exp\left(\frac{V_{BE}}{V_T}\right)$$

$$i_c = I_{nB} = \textcircled{1}$$

$$i_E = I_{nB} + I_{pE} + I_{rB} = \textcircled{1} + \textcircled{2} + \textcircled{3}$$

$$i_B = I_{pE} + I_{rB} = \textcircled{2} + \textcircled{3}$$

Diffusion Current:

$$I_{nB} = -A J_{nB}^{diff} = -A q D_{nB} \frac{dn_p(x)}{dx}$$

cross-sectional area diffusion constant for e⁻s in base

$$= -q A D_{nB} \frac{[n_{pB}(W_B) - n_{pB}(0)]}{W_B}$$

e⁻ conc. in p-type region

Current Formulations

$$\textcircled{1}: I_{nB} = -A J_{nB}^{diff} = -A q D_{nB} \frac{dn_p(x)}{dx}$$

cross-sectional area

diffusion constant for e⁻s in base slope of minority carrier concentration

$$= -q A D_{nB} \frac{[n_{pB}(W_B) - n_{pB}(0)]}{W_B}$$

$$\left[\begin{aligned} n_{pB}(W_B) &= \frac{n_i^2}{N_{aB}} \exp\left(\frac{V_{BC}}{V_T}\right) \approx 0 \\ n_{pB}(0) &= \frac{n_i^2}{N_{aB}} \exp\left(\frac{V_{BE}}{V_T}\right) \end{aligned} \right]$$

$$I_{nB} = q A D_{nB} \frac{n_i^2}{N_{aB} W_B} \exp\left(\frac{V_{BE}}{V_T}\right) = \textcircled{1}$$

$$i_c = \textcircled{1} = I_S \exp\left(\frac{V_{BE}}{V_T}\right)$$

$$\textcircled{2}: I_{pE} = A J_{pE}^{diff} = q A D_{pE} \frac{dp_n(x)}{dx}$$

diffusion constant for h⁺s in emitter slope

$$= q A D_{pE} \frac{[p_{nE}(0) - p_{nE}(-W_E)]}{W_E}$$

W_E ← (or L_p)
↑ for long emitter
↓ for a short emitter
*

$$p_{nE}(0) = \frac{n_i^2}{N_{dE}} \exp\left(\frac{V_{BE}}{V_T}\right)$$

$$p_{nE}(-W_E) \approx 0$$

$$I_{pE} = qA D_{pE} \frac{n_i^2}{N_{dE} W_E} \exp\left(\frac{V_{BE}}{V_T}\right) = \textcircled{2}$$

← minority carrier charge in the base

$$\textcircled{3}: I_{rB} = \frac{Q_e}{\tau_b}$$
 ← minority carrier lifetime in base

$$= \frac{1}{\tau_b} \left[\frac{1}{2} n_{pB}(0) W_B qA \right]$$
 area under the minority carrier (e-) charge curve

$$\therefore I_{rB} = \frac{1}{2} \frac{n_i^2 W_B qA}{N_{aB} \tau_b} \exp\left(\frac{V_{BE}}{V_T}\right) = \textcircled{3}$$

Define: Forward Current Gain = β_F

$$\beta_F = \frac{i_c}{i_B} = \frac{\textcircled{1}}{\textcircled{3} + \textcircled{2}} = \frac{qA D_{nB} n_i^2}{N_{aB} W_B} \frac{1}{\frac{1}{2} \frac{n_i^2 W_B qA}{N_{aB} \tau_b} + \frac{qA D_{pE} n_i^2}{N_{dE} W_E}}$$

$$\therefore \beta_F = \left[\frac{W_B^2}{2 \tau_b D_{nB}} + \frac{D_{pE} W_B N_{aB}}{D_{nB} W_E N_{dE}} \right]^{-1}$$

* make emitter doping large to reduce

To maximize β_F , want:

- ① $W_B = \text{small}$
 - ② $N_{dE} \gg N_{aB} \xrightarrow{\text{leads to}} D_{pE} \ll D_{nE}$
 - ③ $\tau_b = \text{large} \rightarrow$ base Si should be free of impurities/defects to prevent recombination of e-'s & h+'s
- This is why emitter is nt.