

# Lecture 8

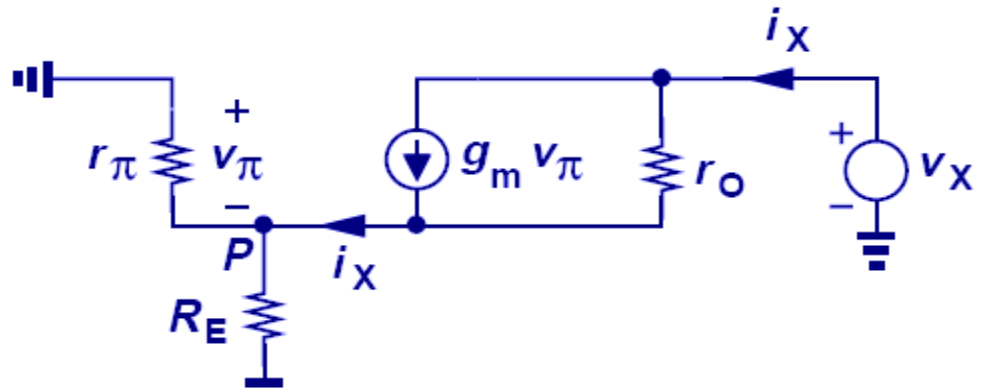
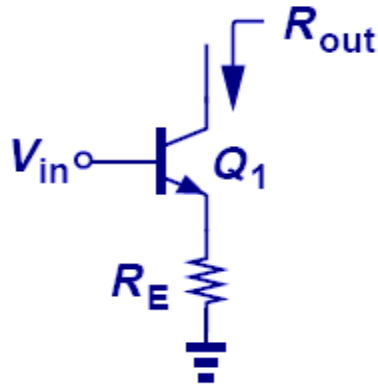
---

## OUTLINE

- Bipolar Amplifier Topologies (Cont'd)
  - Common-Emitter Amplifiers

Reading: Chapter 5.3.1

# Output Impedance of Degenerated Stage with Finite $V_A$



(a)

$$R_{out} = [1 + g_m (R_E \parallel r_\pi)] r_o + R_E \parallel r_\pi$$

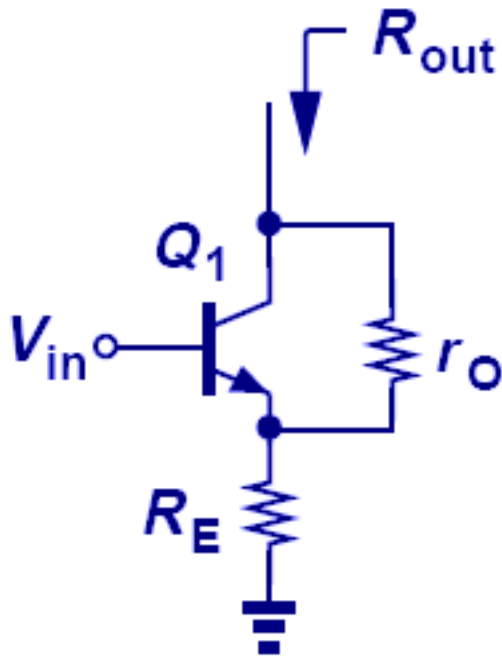
$$R_{out} = r_o + (g_m r_o + 1)(R_E \parallel r_\pi)$$

$$R_{out} \approx r_o [1 + g_m (R_E \parallel r_\pi)]$$

- Emitter degeneration boosts the output impedance by a factor of  $1 + g_m (R_E \parallel r_\pi)$ .
- This improves the gain of the amplifier and makes the circuit a better current source.

# Two Special Cases

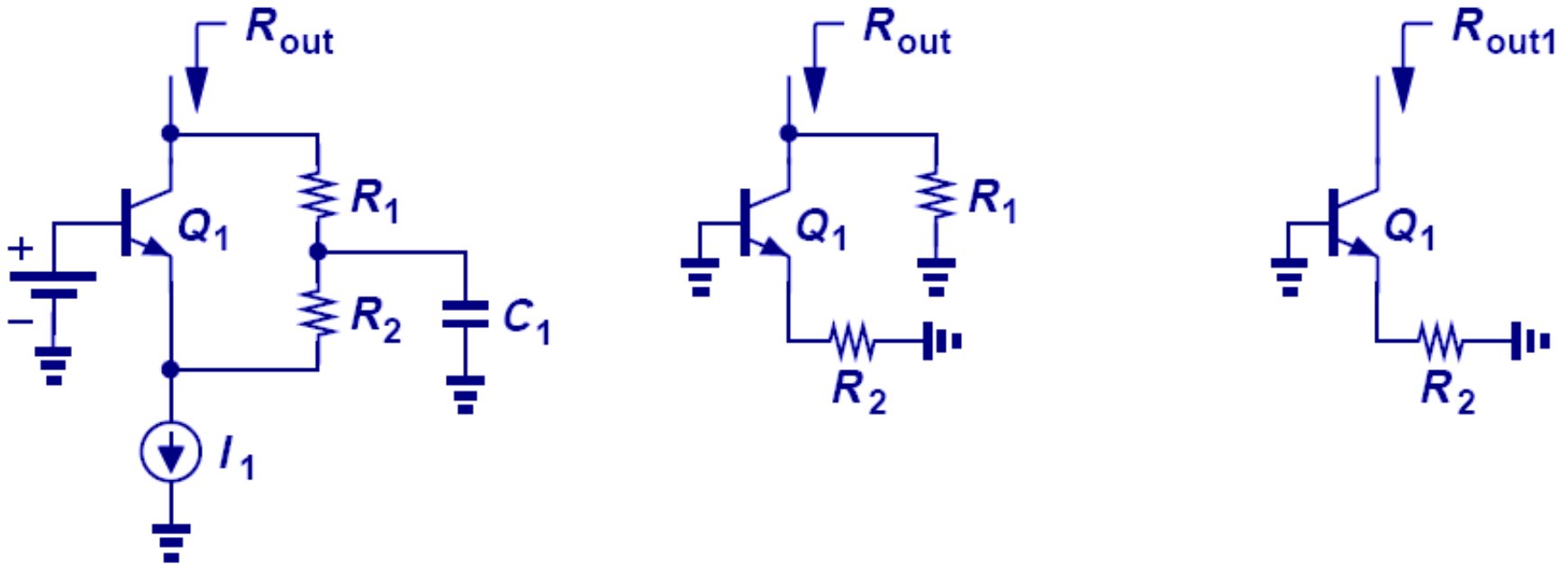
---



$$(1) \quad R_E \gg r_\pi$$
$$R_{out} \approx r_o (1 + g_m r_\pi) \approx \beta r_o$$

$$(2) \quad R_E \ll r_\pi$$
$$R_{out} \approx (1 + g_m R_E) r_o$$

# Analysis by Inspection

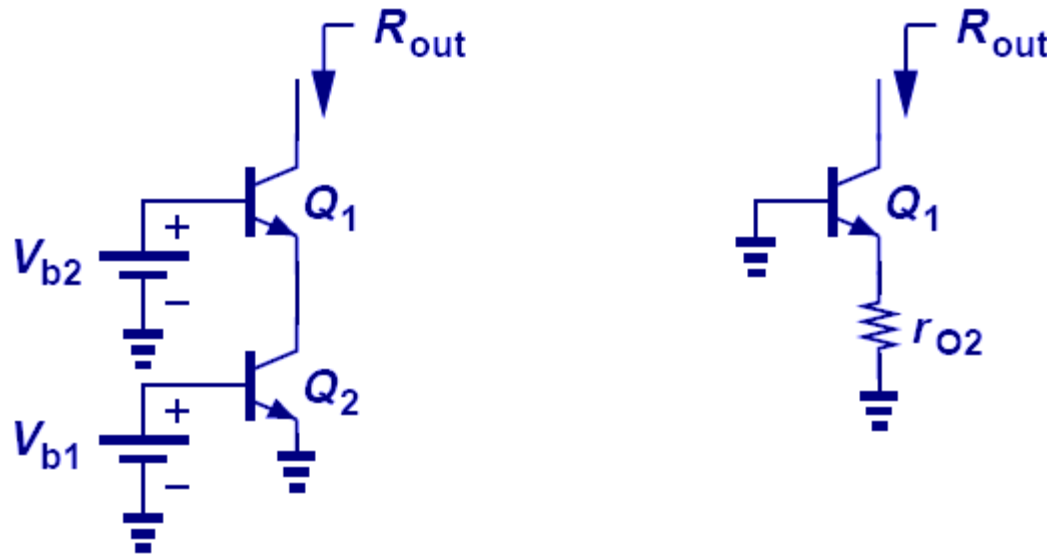


$$R_{out} = R_1 \parallel R_{out1} \xrightarrow{\text{red arrow}} R_{out1} = [1 + g_m (R_2 \parallel r_\pi)] r_o \xrightarrow{\text{red arrow}} R_{out} = [1 + g_m (R_2 \parallel r_\pi)] r_o \parallel R_1$$

- This seemingly complicated circuit can be greatly simplified by first recognizing that the capacitor creates an AC short to ground, and gradually transforming the circuit to a known topology.

# Example: Degeneration by Another Transistor

---

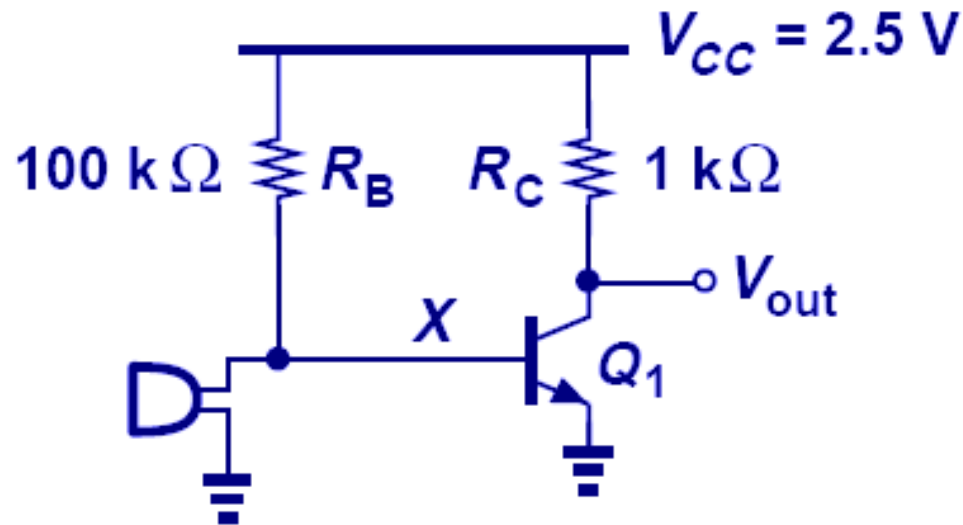


$$R_{out} = \left[ 1 + g_{m1} (r_{O2} \parallel r_{\pi1}) \right] r_{O1}$$

- Called a “cascode”, the circuit offers many advantages that are described later in the book.

# Bad Input Connection

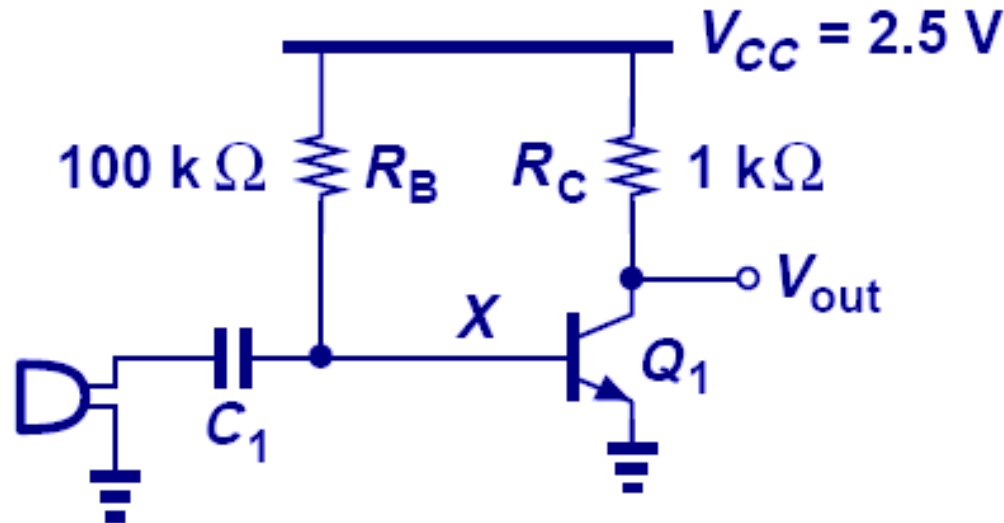
---



- Since the microphone has a very low resistance that connects from the base of  $Q_1$  to ground, it attenuates the base voltage and renders  $Q_1$  without a bias current.

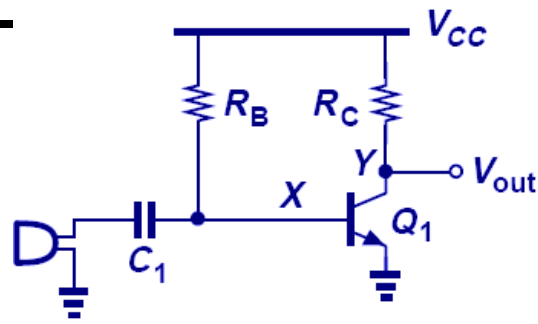
# Use of Coupling Capacitor

---

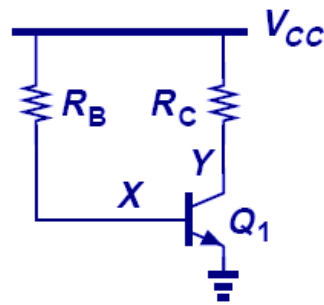


- Capacitor isolates the bias network from the microphone at DC but shorts the microphone to the amplifier at higher frequencies.

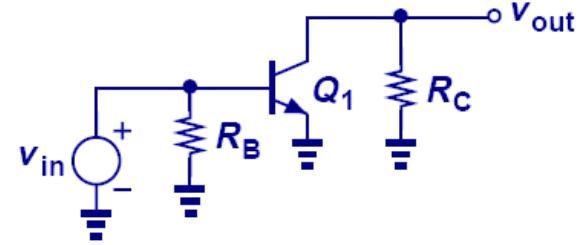
# DC and AC Analysis



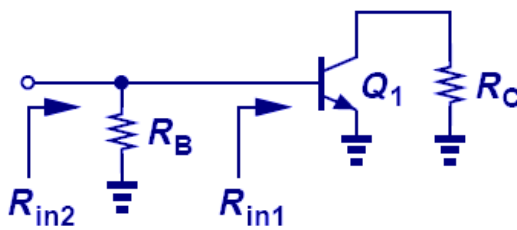
(a)



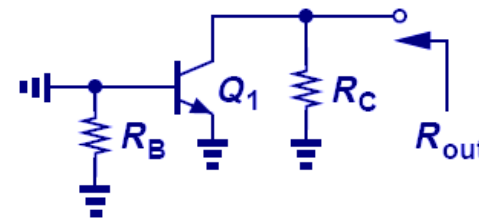
(b)



(c)



(d)



(e)

$$A_v = -g_m (R_C \parallel r_o)$$

$$R_{in} = r_\pi \parallel R_B$$

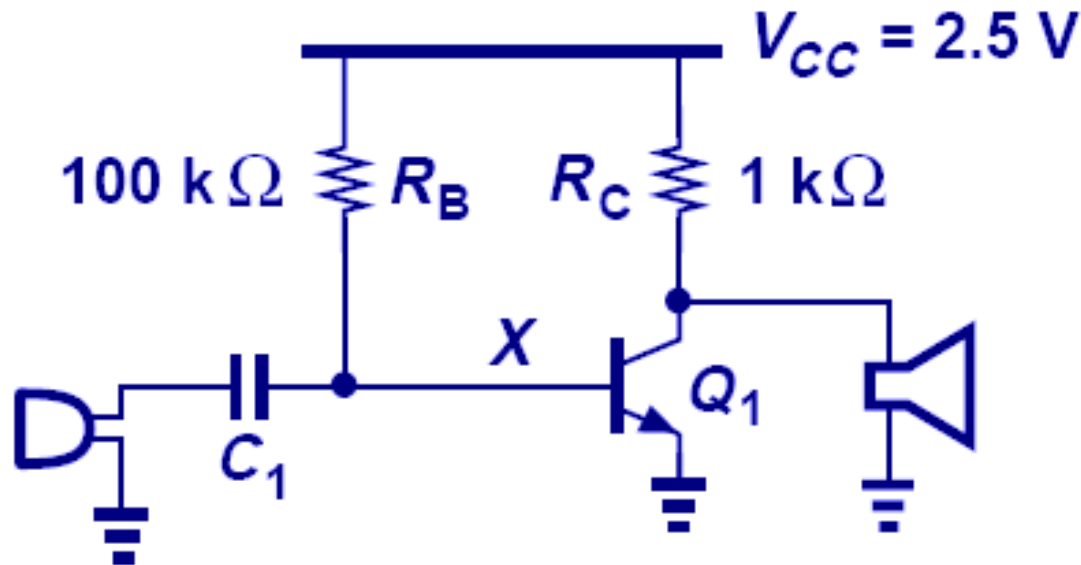
$$R_{out} = R_C \parallel r_o$$

- Coupling capacitor is open for DC calculations and shorted for AC calculations.



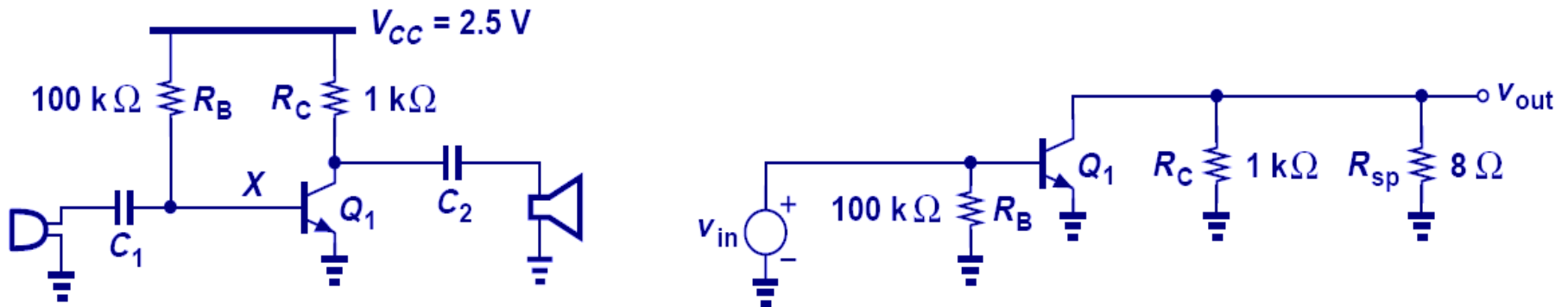
# Bad Output Connection

---



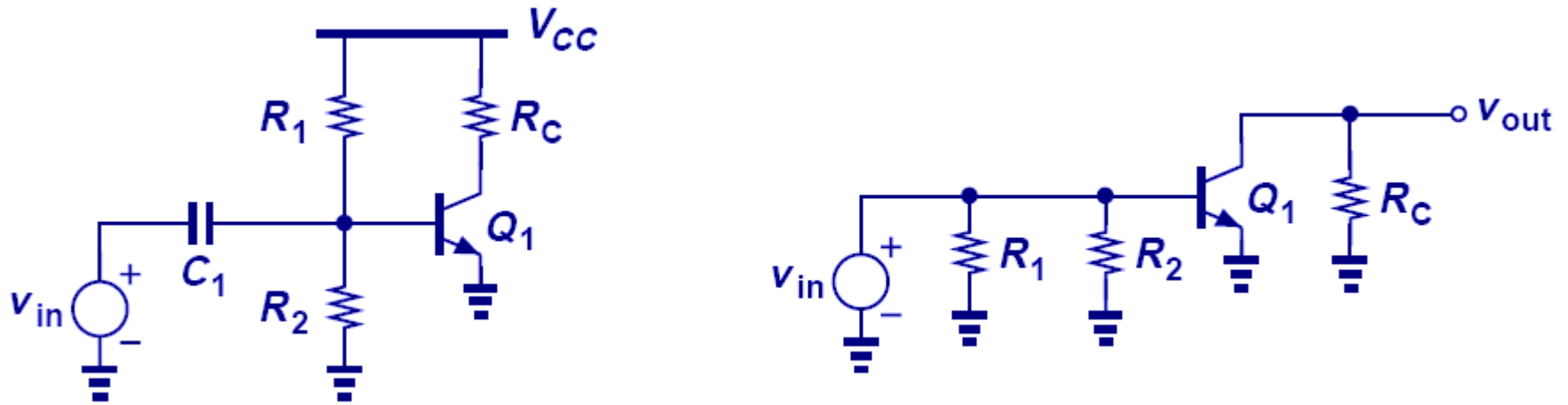
- Since the speaker has an inductor, connecting it directly to the amplifier would short the collector at DC and therefore push the transistor into deep saturation.

# Still No Gain!!!



- In this example, the AC coupling indeed allows correct biasing. However, due to the speaker's small input impedance, the overall gain drops considerably.

# CE Stage with Biasing

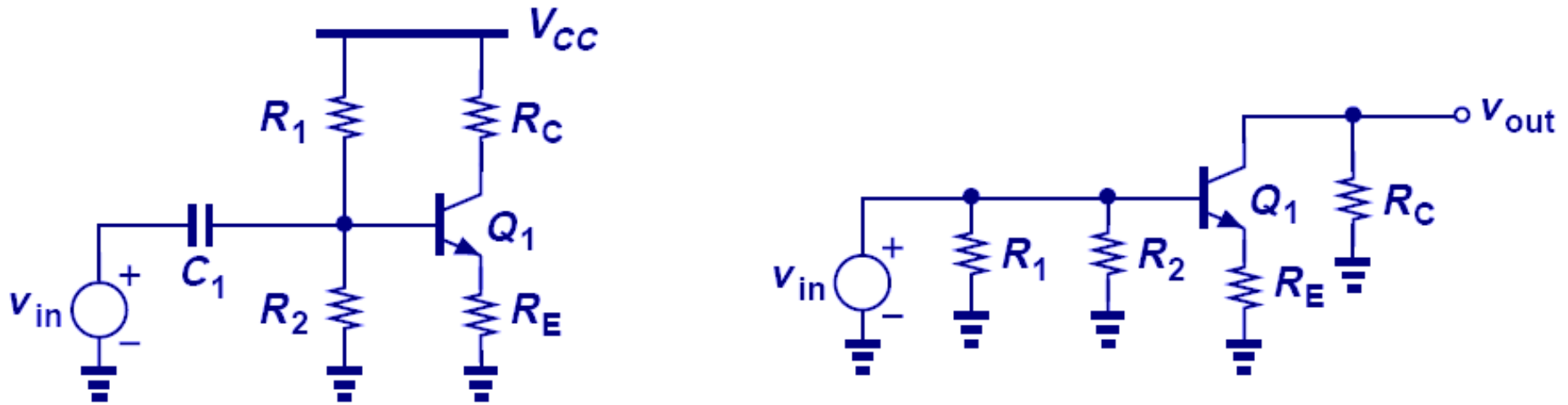


$$A_v = -g_m (R_C \parallel r_o)$$

$$R_{in} = r_\pi \parallel R_1 \parallel R_2$$

$$R_{out} = R_C \parallel r_o$$

# CE Stage with Robust Biasing

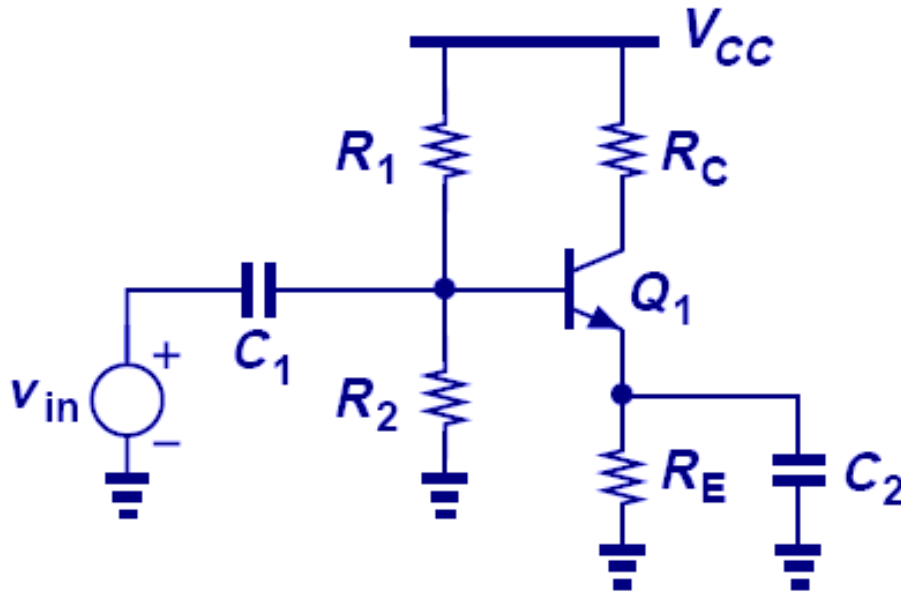


$$A_v = \frac{-R_C}{\frac{1}{g_m} + R_E}$$

$$R_{in} = [r_{\pi} + (\beta + 1)R_E] \parallel R_1 \parallel R_2$$

$$R_{out} = R_C$$

# Removal of Degeneration for Signals at AC



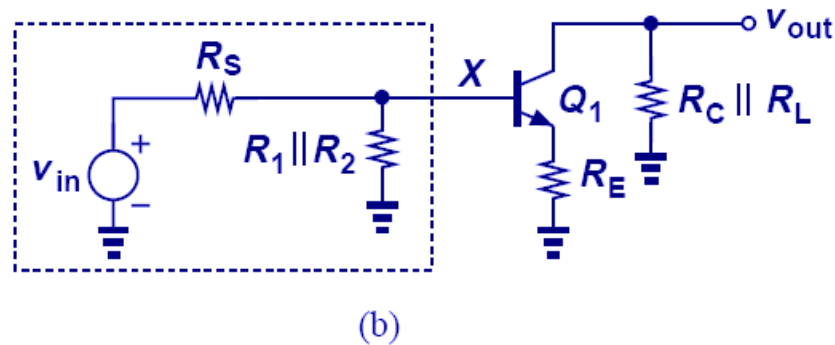
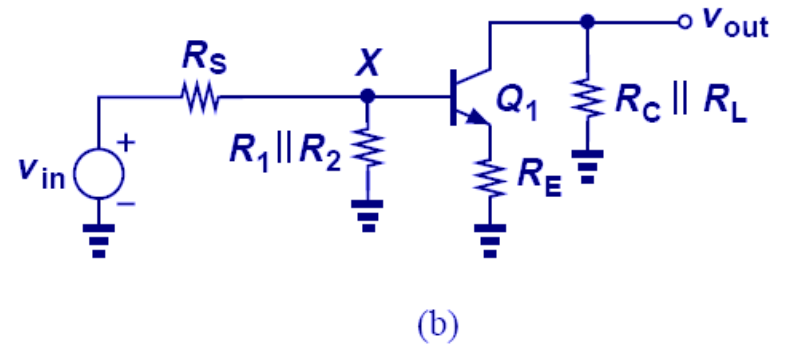
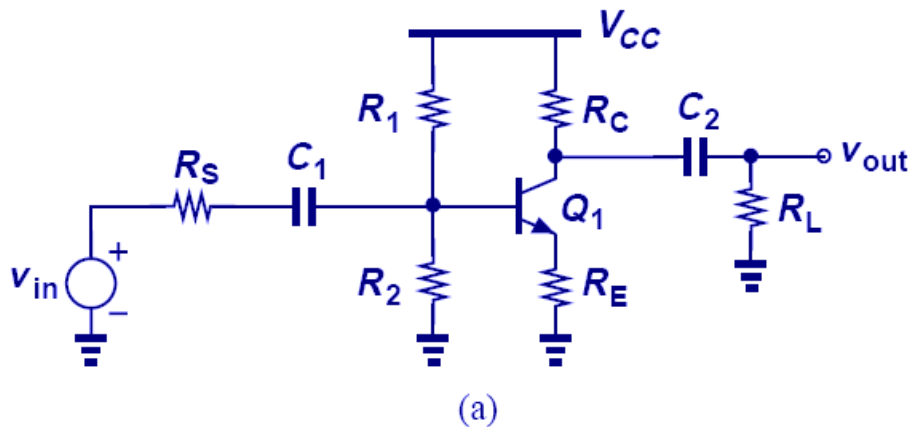
$$A_v = -g_m R_C$$

$$R_{in} = r_{\pi} \parallel R_1 \parallel R_2$$

$$R_{out} = R_C$$

- Capacitor shorts out  $R_E$  at higher frequencies and removes degeneration.

# Complete CE Stage



$$A_v = \frac{-R_C \parallel R_L}{\frac{1}{g_m} + R_E + \frac{R_s \parallel R_1 \parallel R_2}{\beta + 1}}$$

# Summary of CE Concepts

