### UNIVERSITY OF CALIFORNIA, BERKELEY College of Engineering

Department of Electrical Engineering and Computer Sciences

#### EE 105: Microelectronic Devices and Circuits

Fall 2017

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### MIDTERM EXAMINATION #1

Time allotted: 80 minutes

First

Signature

## STUDENT ID#: INSTRUCTIONS:

- 1. SHOW YOUR WORK. (Make your methods clear to the grader!)
- 2. Clearly mark (underline or box) your answers.
- 3. Specify the units of your answer to receive full credit.
- 4. Unless stated in the problem, use the values of physical constants provided below.
- 5. You can use approximations within 20% accuracy any time.
- 6. Calculator is allowed. (Cell phone is not allowed).

\*\*\*\* If you need more space for your answer, use the blank pages in the back. Clearly label which problem is your answer for \*\*\*\*

Commonly used constants and physical parameters:			
Electronic charge	q	$1.6 \times 10^{-19} \text{ C}$	
Boltzmann's constant	k	$8.62 \times 10^{-5} \text{ eV/K}$	
Thermal voltage at 300K	$V_{\rm T} = kT/q$	0.025 V	
Relative permittivity of Si	$\epsilon_{r,Si}$	12	
Relative permittivity of SiO <sub>2</sub>	$\epsilon_{r,ox}$	4	
Vacuum permittivity	$\epsilon_0$	8.854x10 <sup>-14</sup> F/cm	

	Problem 1	20	
	Problem 2	30	
Points	Problem 3	20	
	Problem 4	30	
	Total	100	

1) A simple filter is shown below: (OpAmp is ideal)



- a) What is the transfer function  $H(j\omega) = V_o/V_s$ ?
- b) What is the expression of low frequency gain in dB?
- c) What is the 3-dB frequency (in Hz) of the filter?
- d) Assume  $C_1 = 100 \, pF$ ,  $C_2 = 10 \, pF$ ,  $R_1 = 10 \, k\Omega$ ,  $R_2 = 1 \, k\Omega$ , draw the magnitude Bode plot. Clearly label the graph, including all the breakpoints (in magnitude and frequency).
- e) Draw the phase Bode plot using the same numerical values. Clearly label the graph.

2) Consider the *stable* amplifier circuit below:



- a) Label the plus and minus terminals in the schematic above.
- b) Calculate the transfer function, assuming the op-amp is ideal.

# Now, assume that the op-amp has a finite open-loop gain, $A_0$ , and a pole at frequency $\omega_0$ .

- c) Write out the transfer function representing the op-amp's behavior in open-loop.
- d) Using this non-ideal op-amp, calculate the transfer function  $V_{out}/V_{in}$ .
- e) What are the locations of the poles and zeros?
- f) Assume the op-amp has the following metrics:  $A_0 = 100$  dB,  $f_0 = 50$  kHz. Can you make closed loop amplifiers with the following metrics?
  - i) Closed-loop Gain of 50, bandwidth of 100GHz.
  - ii) Closed-loop Gain of 1, bandwidth of 5GHz
  - iii) Closed-loop Gain of 0.1, bandwidth of 40GHz.

- 3) A non-inverting amplifier with variable gain is shown on the right. Here,  $R_1 = 1 \text{ k}\Omega$  and  $R_2$  is variable from  $1 \text{ k}\Omega$  to  $1 \text{ M}\Omega$ . This input signal is a sinusoidal signal with an amplitude of 100 mV and a frequency of  $\omega = 10^6 \text{ rad/s}$ . The Op Amp has a slew rate (SR) of  $1 \text{ V/}\mu\text{s}$ .
  - a) First, assume the Op Amp has infinite bandwidth. If we gradually increase the gain of the amplifier by increasing  $R_2$ , at what value of  $R_2$  does the output become slew rate limited?



b) Now consider the Op Amp with a finite gain-bandwidth product of 100 MHz and  $R_2 = 49$  k $\Omega$ . The input signal amplitude is fixed at 1 mV, but the frequency is gradually increasing from 100 Hz to higher frequency. Do we encounter bandwidth limit or slew rate limit first? What is that frequency?

- 4) Consider a p-n junction with N-type doping of  $N_D = 10^{18}$  cm<sup>-3</sup> and P-type doping of  $N_A = 10^{16}$  cm<sup>-3</sup>. The length of the N- and P-doped regions are  $L_N = L_P = 10 \ \mu m$ . The cross-sectional area is  $A = 10 \ \mu m^2$ . Assume the intrinsic carrier concentration is  $n_i = 10^{10}$  cm<sup>-3</sup>.
  - a) What is the built-in voltage of the p-n junction?
  - b) Is the depletion region mostly in the P-side or the N-side?
  - c) What is the depletion capacitance at zero bias?
  - d) This capacitance is bias dependent. At what voltage will the capacitance reduce to ½ of the zero-bias value? Specify the polarity of the bias (i.e., forward or reverse).
  - e) The small-signal equivalent circuit of a p-n junction is shown below. The P and N doped region forms a series resistance. Using the mobility chart below, find the series resistance at P and N region.



f) The small signal equivalent circuit of the p-n junction diode at reverse bias is shown below. What is the bandwidth of this device at zero bias? (*Hint: Bandwidth is defined as* the 3-dB cut-off frequency of  $G(j\omega) = i_S/v_S$ .)

