## EE119 Homework 9: LCDs and Lasers

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1. The electro-optic characteristics for a TN-LCD and STN-LCD are given in the figure 1. Two vertical lines in each graph indicate the OFF- ON rms-operating voltages for 240:1 multiplexing. (This is a dual scan VGA display, so M = 240 instead of 480.)



Figure 1: electro-optic characteristics for TN-LCD and STN-LCD

- (a) Which graph corresponds to the characteristics of a TN-LCD? Why?
- (b) The Pixel Contrast Ratio is defined to be

$$PCR = \frac{L_{\rm high} + (M-1)L_{\rm low}}{ML_{\rm low}}$$

Where M is the number of display rows,  $L_{\text{low}}$  is the lowest value of transmitted luminance, and  $L_{\text{high}}$  is the highest value of transmitted luminance. Calculate the PCR for the TN-LCD and STN-LCD displays, using the values shown on the graph in the figure. Explain any difference between the two values.

- 2. A nematic liquid crystal has  $n_0=1.52$  and  $n_e=1.75$  at  $\lambda=577$  nm. Find the half-waveplate thickness at this wavelength.
- 3. Spontaneous and Stimulated Emission

(a) [Hecht 13.16] Show that for a system of atoms and photons in equilibrium at a temperature T the ratio of the transition rates of stimulated to spontaneous emission is given by

$$\frac{1}{e^{h\nu/k_BT}-1}$$

- (b) [Hecht 13.17] A system of atoms in thermal equilibrium is emitting and absorbing photons with energy of 2 eV. Determine the ratio of the transition rates of stimulated emission to spontaneous emission at a temperature of 300 K. Discuss the implications of your answer. [Hint: See the previous problem.]
- 4. Resonator cavities

A cavity, such as the space between two end mirrors on a laser, will allow light to resonate in it if an integer number of half-wavelengths of light fit into the cavity. The end mirrors of a laser are separated by 25 cm, and the cavity is filled with air (n=1).

- (a) What is the spacing between longitudinal modes in the laser cavity?
- (b) The bandwidth of the gain curve is approximately 1500 Mhz. What is the maximum number of possible frequencies that can lase?
- (c) If the length of the cavity were to decrease, how would your answers to (a) and (b) change?
- 5. To make short pulses of laser light, the different modes in a cavity are fixed relative to one another so that the electric fields add constructively in one place and destructively everywhere else, giving a pulse of light that is as close to a delta function (in time) as possible. The lower limit on the duration of the pulse is the energy-time uncertainty principle, which states that  $\Delta E \Delta t \geq \hbar$  or, equivalently  $\Delta \nu \Delta t \geq 1/2\pi$ . If you want to make a pulse centered at 600 nm that is 10 femtoseconds long, what is the range of wavelengths at which your lasing medium must have gain?
- 6. [Hecht 13.22] Make a rough estimate of the amount of energy that can be delivered by a ruby laser whose crystal is 5.0mm in diameter and 0.050 m long. Assume the pulse of light lasts  $5.0 \times 10^{-6}$ s. The density of aluminum oxide (Al<sub>2</sub>O<sub>3</sub>) is  $3.7 \times 10^3$  kg/m<sup>3</sup>. Use the data in the discussion of Fig. 13.6 and the fact that the chromium ions make a 1.79eV lasing transition. How much power is available per pulse?

You can assume that the concentration of Chromium in Aluminum Oxide is 0.05 % for ruby.