

Problem Set 4

Fall 2018

Issued: Wednesday, September 12, 2018

Due: For your own practice

Problem 1. Poisson Bounds

Let X be the sum of 20 i.i.d. Poisson random variables X_1, \dots, X_{20} with $\mathbb{E}[X_1] = 1$. Use Markov's Inequality and Chebyshev's Inequality to find an upper bound of $\Pr(X \geq 26)$.

Problem 2. Convergence of Exponentials

Let X_1, X_2, \dots be i.i.d. $\text{Exp}(\lambda)$ random variables. Show that

$$\frac{X_n}{\ln n} \rightarrow 0 \quad \text{in probability as } n \rightarrow \infty.$$

Problem 3. Transform Practice

Consider a random variable Z with transform

$$M_Z(s) = \frac{a - 3s}{s^2 - 6s + 8}, \quad \text{for } |s| < 2.$$

Calculate the following quantities:

1. The numerical value of the parameter a .
2. $\mathbb{E}[Z]$.
3. $\text{Var}(Z)$.