

**Problem1.** A random variable  $X$  has pdf  $f_X(x) = cx(1 - x)$ ,  $0 \leq x \leq 1$ .

- Find  $c$ .
- Find the pdf of the area covered by a disc with radius  $X$ .
- Find the pdf of  $Y = X^n$ .

**Problem2.** Generation of random variables.

- Generate random variable  $Y$ , pdf  $f_Y(y) = \frac{a}{\pi(a^2+y^2)}$ ,  $\infty \leq x \leq \infty$ ,  $a > 0$ , given random variable  $X, X \sim U[0, 1]$  uniformly distributed in  $[0, 1]$ .
- Generate random variable  $Y$ , pdf  $f_Y(y) = \frac{a}{2}e^{-a|y|}$ ,  $\infty \leq x \leq \infty$ ,  $a > 0$ , given random variable generator which generates iid random variables  $X$ , pdf  $f_X(x) = be^{-bx}$ ,  $x \geq 0$ ,  $b > 0$ .

**Problem3.** pdf of the sum of the square of Gaussian random variables.  $X, Y$  are independent Gaussian random variables,  $X \sim N(0, 1), Y \sim N(0, 1)$ . Let  $Z = X^2 + Y^2$ .

- Find the pdf of  $Z$ .
- Find the mean and variance of  $Z$ .
- Find the pdf of  $W = \sqrt{Z}$ .