

**Due at 1700, Fri. Sep. 6 on BCourses.**

Note: up to 2 students may turn in a single writeup. Reading Nise 1,2.

1. (20 pts) Case study (Nise 1.4)

In an aircraft, the roll rate can be controlled by ailerons as shown in Fig. 1. A gyroscope is used to measure actual roll angle rate. Assume a reference input  $r$  (from pilot) is used to specify desired roll angle rate.

- a) Draw a functional block diagram for a roll angle rate control system. Show all blocks and signals, identify input and output transducers, controller and plant.
- b) Suppose the gyro fails (e.g. stuck at maximum full range). Draw a block diagram for a controller which could allow pilot to reasonably handle this case.

2. (20 pts) Static Nonlinearity in Feedback

A nonlinear amplifier has voltage response  $g(\varepsilon) = 1000 \log(\varepsilon + 1)$ . Let  $\delta(t) = 0$ . The nonlinear amplifier is used in a negative feedback system as shown in Fig. 2, with  $k = \frac{1}{3}$ .

- a) Assume  $|x(t)| \ll 1$ . Using Taylor series approximation, show that  $y(t) \approx 3x(t)$ .
- b) Consider constant output  $y_1 = 3$ . Without approximations, find the value of input  $x$  corresponding to this output.
- c) Consider constant output  $y_2 = 6$ . Without approximations, find the value of input  $x$  corresponding to this output.
- d) What is the per cent error for b) and c) compared to an ideal gain of 3?

*Aside: For stable systems with slow dynamics, with sufficient gain, a learned control law can have wide variation with little effect on reward.*

3. (20 pts) Laplace transform review (Nise 2.2)

For each transfer function below determine  $h_i(t)$ .

- i)  $H_1(s) = \frac{1}{s^2+14s+48}$
- ii)  $H_2(s) = \frac{s}{s^2+14s+48}$
- iii)  $H_3(s) = \frac{s+10}{s^2+14s+48}$
- iv)  $H_4(s) = \frac{1}{s^2+6s+18}$
- v)  $H_5(s) = \frac{1}{s^3+14s^2+48s}$

4. (20 pts) Initial value, final value (Nise 2.2)

For each of the following Laplace transforms  $Y_i(s)$  determine  $y_i(t = 0^+)$  and if the limit exists,  $\lim_{t \rightarrow \infty} y_i(t)$ :

- i)  $Y_1(s) = \frac{s}{s+5}$
- ii)  $Y_2(s) = \frac{s-3}{s+5}$
- iii)  $Y_3(s) = \frac{(s+3)}{s(s+5)}$
- iv)  $Y_4(s) = \frac{1}{s(s+5)}$
- v)  $Y_5(s) = \frac{(s+3)^2}{(s+5)^2}$

5. (20 pts) Electrical circuit example (Nise 2.4)

For the circuit in Fig. 3. below, using ideal op-amp assumptions (p. 58 in 6th edition), determine  $H(s) = \frac{v_{out}(s)}{v_{in}(s)}$ .



Fig.1.

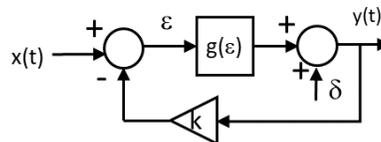


Fig. 2.

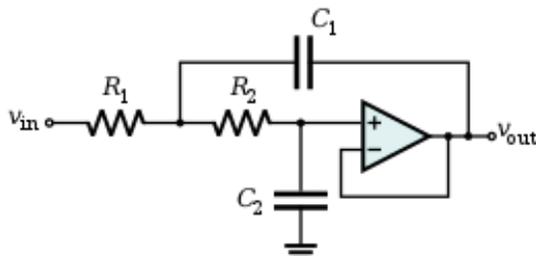


Fig. 3