

**PROBLEM SET #6**

Issued: Tuesday, Oct. 8<sup>th</sup>, 2013

Due: Wednesday, Oct. 16<sup>th</sup>, 2013, 8:00 a.m. in the EE 140/240A homework box

1. For the high-swing cascode mirror shown in Fig. PS6.1 answer the following questions:
  - a) Calculate  $W$  such that the minimum output voltage for which both  $M_1$  and  $M_2$  are in saturation is  $0.5V$ . Assume that  $M_3$ - $M_5$  can provide appropriate gate biases for  $M_1$  and  $M_2$ .
  - b) Calculate  $W_5$  in order to achieve the minimum output voltage calculated in (a).
  - c) Briefly explain the function of  $M_4$ .
  - d) What is the output resistance of this current source?
  - e) What is the change in  $I_{OUT}$  for  $\Delta V_{OUT}=1V$ ?
  - f) What is the resistance seen by the  $I_{IN}$  that biases  $M_3$  and  $M_4$ ?
  - g) Calculate input voltages  $V_{IN1}$  and  $V_{IN2}$ .
  - h) Replace transistors  $M_5$  and  $M_6$  with one diode connected device. What is the  $W$  of the new device?

$$I_{IN} = 100\mu A, \quad L = 1\mu m, \quad C_{ox} = 5 \frac{fF}{\mu m^2}, \quad \mu_n = 450 \frac{cm^2}{Vs}, \quad V_{th0} = 0.6V, \quad \lambda = 0.02V^{-1}, \quad \gamma = 0$$

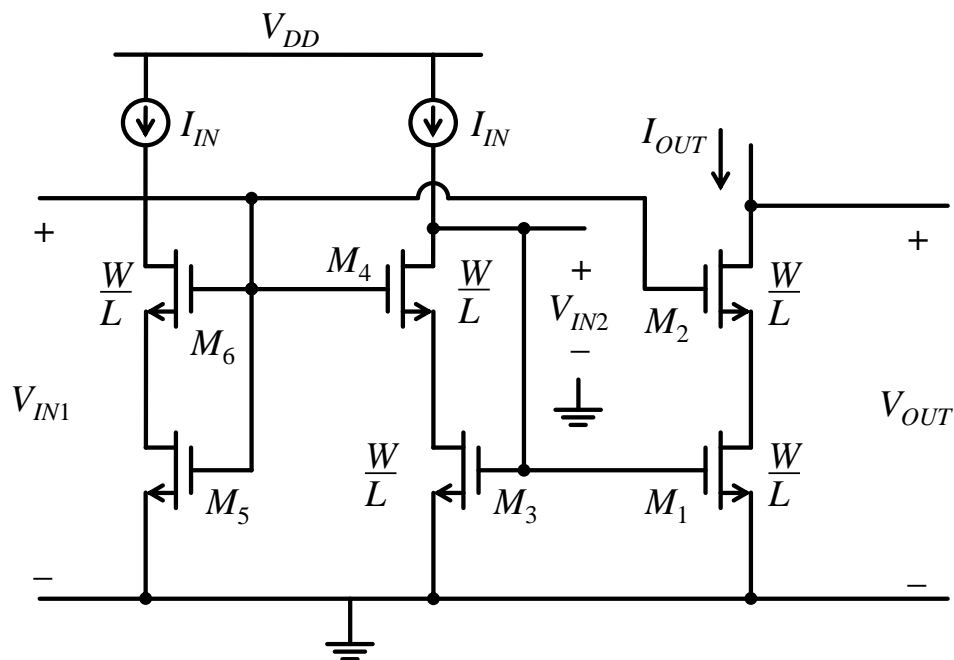


Fig. PS6.1

2. Consider the low voltage cascode current mirror shown in Fig. PS6.2, for which  $10\mu\text{A}$  reference ideal current sources  $I_1$  and  $I_2$  are available, and the desired output current is  $I_{out} = 100\mu\text{A}$ . Assuming the size of  $M_3$  is  $(W/L)$ , determine the  $(W/L)$ 's of  $M_1$ ,  $M_2$ ,  $M_4$ , and  $M_5$  relative to that of  $M_3$  to provide the maximum headroom at the  $I_{out}$  node. In your design,  $M_1$ ,  $M_2$ ,  $M_3$ , and  $M_4$  should all have the same  $V_{ov}$  and be operating in saturation. Assume  $\lambda = 0$  and ignore the body effect.

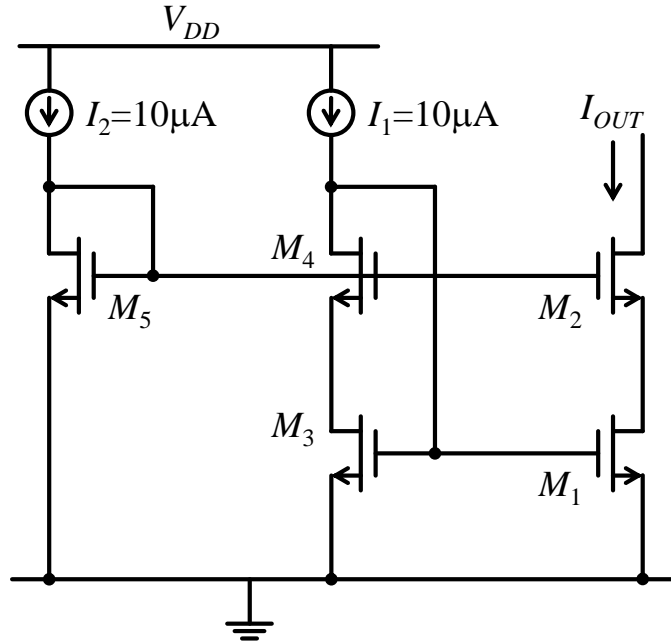


Fig. PS6.2

3. In the circuit shown in Fig. PS6.3, a source follower using a wide transistor  $M_4$  and a small bias current is inserted in series with the gate of  $M_3$  so as to bias  $M_2$  at the edge of saturation. Assuming  $M_0 - M_3$  are identical and  $\lambda \neq 0$ , estimate the mismatch between  $I_{out}$  and  $I_{REF}$  if:

- (a)  $\gamma = 0$
- (b)  $\gamma \neq 0$

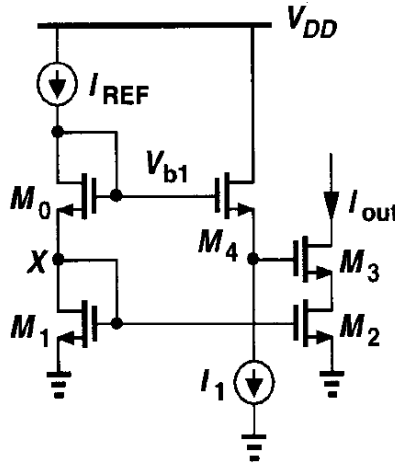


Fig. PS6.3

4. Provide an expression and calculate a numerical value for the output current mismatch between  $I_{C2}$  and  $I_{C3}$  shown in Fig. PS6.4 caused by finite fabrication tolerances.

Nominal parameter values:

$$\beta = 100, I_s = 37.751 \times 10^{-15} \text{ A}, V_T = 25 \text{ mV}, R_0 = 3.4 \text{ k}\Omega, R_1 = R_2 = R_3 = 1 \text{ k}\Omega.$$

Fabrication tolerances:

$$\Delta\beta/\beta = 10\%, \Delta I_s/I_s = 5\%, \Delta R/R = 20\%.$$

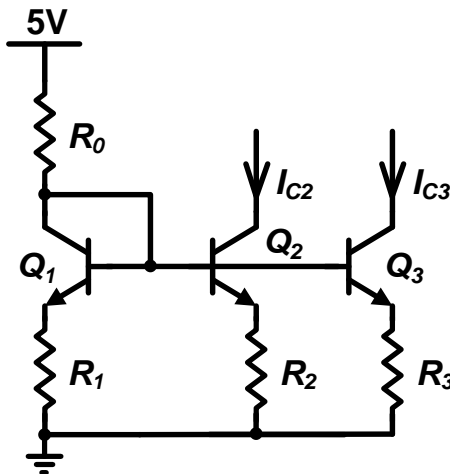


Fig. PS6.4