## **PROBLEM SET #6**

Issued: Tuesday, Feb.28, 2012

Due: Tuesday, March.6, 2012, 6:00 p.m. in the EE 140 homework box in 240 Cory

1. (a) For the two current mirror circuits shown in Fig. PS6.1-1, determine the size of  $M_4$  to achieve the minimum output voltage  $2V_{ov, MI}$ . Then determine the  $I_{out}$  percent difference from  $I_{REF}$  for the two circuits when the output voltage is  $2V_{ov, MI}$ . Assume  $\lambda \neq 0, \gamma=0$ .



Fig. PS6.1-1

(b) A resistively-biased high-swing cascode current source with only one  $I_{REF}$  is shown in Fig. PS6.1-2(a). Determine all transistor sizes and the value of  $R_b$  in this circuit that yield  $I_{out}=I_{REF}=250\mu\text{A}$  with a minimum output voltage  $V_{OMIN}=0.5\text{V}$ .Assume  $V_{t0}=0.7\text{V}$ ,  $k'=110\mu\text{A/V}^2$ ,  $\gamma=0.4$ ,  $\lambda=0$ ,  $2/\varphi_f$ =0.7.



Fig PS6.1-2

(c) Fig. PS6.1-2(b) now presents a self-biased  $V_{bias}$  generator that generates its own  $I_{REF}$ . Determine the sizes of all transistors and the value of  $R_{ref}$  that yield  $I_{out}=I_{REF}=250\mu$ A and a minimum output voltage  $V_{OMIN}=0.5V$  for  $V_{DD}=3V$ . Assume  $V_{t0,n}=0.7V$ ,  $V_{t0,p}=-0.7V$ ,  $k_n'=110\mu$ A/V<sup>2</sup>,  $k_p'=50\mu$ A/V<sup>2</sup>,  $\gamma=0.4$ ,  $\lambda=0$ ,  $2/\varphi_f$ =0.7 and  $M_9=M_7=M_2=M_1$ . 2. Consider the simple current mirror illustrated in Fig. PS6.2. Over the process, the absolute variations of physical parameters are as follows:

Width variation:	<u>+</u> 5%
Length variation:	<u>+</u> 5%
k' variation:	<u>+</u> 5%
$V_T$ variation:	$\pm 5 mV$

Assume that the drain voltages are identical, what is the minimum and maximum output current measured over the process variations given above? Assume  $k = 110 \mu A/V^2$ .



Fig. PS6.2

3. Draw the differential-mode and common-mode half-circuits for the differential amplifier in Fig. PS6.3. Use half-circuits to find the DC operating point, differential-mode gain, common-mode gain, and differential-mode input resistance for the amplifier if  $\beta_o = 100$ ,  $V_{CC} = 20$  V,  $V_{EE} = 20$  V,  $I_{EE} = 100 \mu$ A, and  $R_{EE} = 600 \text{ k}\Omega$ ?



Fig. PS6.3

4. (a) For the single-ended output differential pair with active current mirror load in Fig. PS6.4(a), derive the differential gain:  $A_d = g_{m1,2}(r_{o1,2} || r_{o3,4})$ , assuming  $g_m r_o >> 1$ .

(b) Due to a manufacturing defect, a large parasitic resistance,  $R_1$ , has appeared in the circuit of Fig. 6.4(b). Determine an expression for the differential gain of this circuit.



Fig. PS6.4