EECS140
Spring 2015
Midterm 1

Name $\qquad$

| Prob. | Score |
| :--- | ---: |
| 1 | $/ 18$ |
| 2 | $/ 8$ |
| 3 | $/ 10$ |
| 4 | $/ 16$ |
| 5 | $/ 18$ |
| Total | $/ 70$ |

1) Fill in the following table where each row is a different single-pole amplifier

| $\mathbf{G}_{\mathrm{m}}[\mathbf{S}]$ | $\mathbf{R}_{0}[\Omega]$ | $\mathbf{C}_{\mathbf{L}}[\mathbf{F}]$ | $\mathbf{A v}$ | $\omega_{\mathrm{p}}[\mathrm{rad} / \mathrm{s}]$ | $\omega_{\mathrm{u}}[\mathrm{rad} / \mathrm{s}]$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 10 m |  |  | 10 |  | 100 G |
| 1 u | 1 M | 10 f |  |  |  |
|  |  | 1 p | 100 | 10 M |  |

2) You have a single-pole amplifier with a gain of 100 at 100 MHz , and a low frequency gain of 500. What is the unity gain frequency? What is the pole frequency? What is the gain at 100 Hz , and 1 GHz ?

| Frequency | Gain |
| :--- | :--- |
| $\omega_{\mathrm{u}}$ |  |
| $\omega_{\mathrm{p}}$ |  |
| 100 Hz |  |
| 1 GHz |  |

3a) You apply a 1 V sine wave at $1 \mathrm{Mrad} / \mathrm{s}$ to a capacitor, and measure $1 \mu \mathrm{~A}$ of current.
What is the capacitance?
What current will flow if you raise the frequency to $1 \mathrm{Grad} / \mathrm{s}$ ?

| C |  |
| :--- | :--- |
| I |  |

3b) You invent a new transistor, and find that the output current is given by $I_{x y}=K V_{z y}^{3} V_{x y}{ }^{1 / 2} ; \quad I_{z}=\mathbf{0}$
What are the formulas for the transconductance and the output resistance?
What is the intrinsic gain when the device is biased at $\mathrm{V}_{\mathrm{zy}}=\mathrm{V}_{\mathrm{xy}}=1 \mathrm{~V}$ ? (give a numerical answer)


| $\mathrm{g}_{\mathrm{m}}$ |  |
| :--- | :--- |
| $\mathrm{r}_{\mathrm{o}}$ |  |
| Av |  |

4) You have biased the amplifier below with a particular input overdrive voltage $V_{o v}$. Both devices are in saturation, and the quadratic model is appropriate. The low frequency gain is $-1000 . \mathrm{C}_{\mathrm{gs} 1}=1 \mathrm{pF}, \mathrm{C}_{\mathrm{gd} 1}=0.1 \mathrm{pF}$.


What is the input capacitance? (give an exact numerical answer)

| $\mathrm{C}_{\text {in }}$ |  |
| :--- | :--- |

You adjust the bias voltages so that $\mathbf{V}_{\text {ov }}$ increases by a factor of two. What happens to the current, small signal parameters, low frequency gain, output pole frequency, output unity gain frequency, and input capacitance? Answers should be of the form "increase 5x" "decrease 10x" "stay the same", etc.

| $\mathrm{I}_{\mathrm{D}}$ |  |
| :--- | :--- |
| $\mathrm{g}_{\mathrm{m}}$ |  |
| $\mathrm{r}_{\mathrm{o}}$ |  |
| $\mathrm{A}_{\mathrm{v} 0}$ |  |
| $\omega_{\mathrm{p}}$ |  |
| $\omega_{\mathrm{u}}$ |  |
| $\mathrm{C}_{\mathrm{in}}$ |  |

Find the total low frequency impedance seen "looking up" and "looking down" at each output node indicated in each circuit. Write your answer in terms of $g_{m}, g_{m}, r_{o}$, and $r_{o}$. Assume that all devices have transconductance $g_{m}$ and output resistance $r_{0}$. Write the full expression for up and down, and then the simplified total impedance assuming that $g_{m} * r_{o}$ >> 1 .

|  | Full expression | Simplified expression <br> for Ro, assuming gm ro >>1 |
| :--- | :--- | :--- |
| $\mathrm{R}_{\text {out, up }}$ |  | $\mathrm{R}_{\text {out }}$ |
| $\mathrm{R}_{\text {out, dn }}$ |  |  |
| $\mathrm{R}_{\mathrm{D} 1, \text { up }}$ |  | $\mathrm{R}_{\mathrm{D} 1}$ |
| $\mathrm{R}_{\mathrm{D} 1, \mathrm{dn}}$ |  |  |



Given the bias voltages above, what are the bias voltages at the sources of the cascode transistors, and what is the output swing? Assume that $\left|\mathbf{V}_{\mathbf{t p}}\right|=\mathbf{V}_{\mathbf{t n}}=\mathbf{0 . 5 V}$, and that M1 and M1C have the same W/L, and that M2 and M2C have the same W/L.

| $\mathrm{V}_{\mathrm{S} 1 \mathrm{C}}$ |  |
| :--- | :--- |
| $\mathrm{V}_{\mathrm{S} 2 \mathrm{C}}$ |  |
| swing |  |

