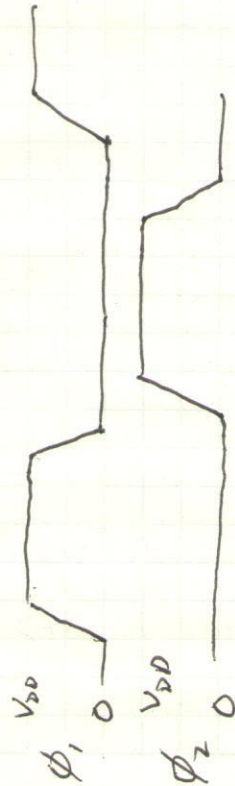


## switched capacitors

SC circuits have 1 or more clock signals, often

w/ non-overlapping phases



clock phases open and close switches (FETs)

which rewire the circuit.

"During  $\phi_1$ " "During  $\phi_2$ "

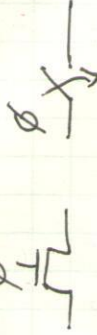
## Switched Capacitors

Bipolar amps tend to use resistive feedback

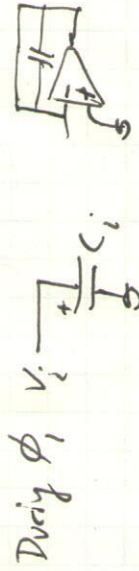
MOS amps ~~in~~ in the early days couldn't drive as much current

Berkeley led the charge on capacitors in FB

MOS make great switches



simplest model: short or open  
next: resistor or open



$$Q_{Ci} = V_i C_i \quad Q_{Cf} = 0$$

~~During~~  $\phi_2$



$$Q_{Ci} = V_i C_i \quad Q_{Cf} = 0$$

During  $\phi_2$ :



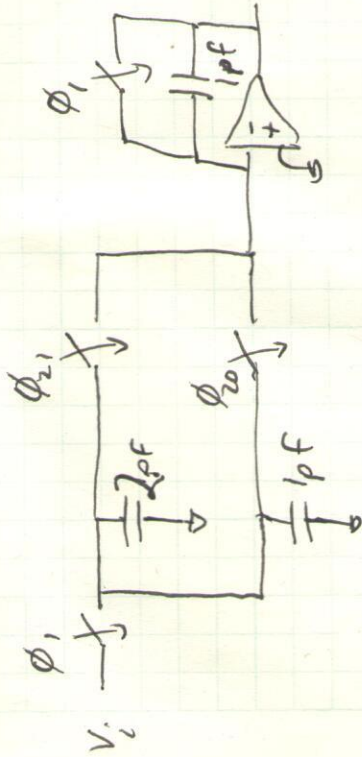
op-amp drives  $V_- = 0$  so  $Q_{C_i} = 0$

where does it go? To  $C_f$

$$Q_{C_f} = Q_{C_i} = V_i \cdot C_i$$

$$V_{C_f} = \frac{Q_{C_f}}{C_f} = V_i \cdot \frac{C_i}{C_f}$$

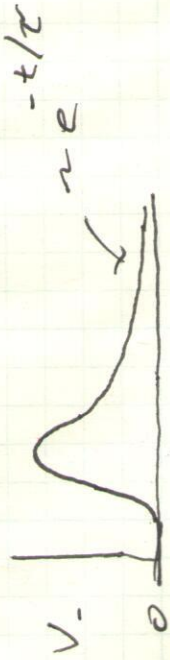
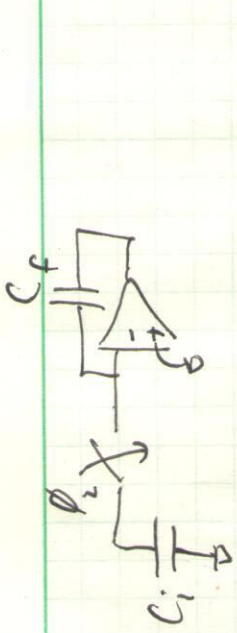
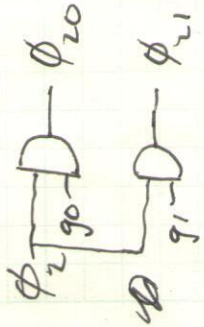
$$V_o = V_- - V_{C_f} = 0 - V_i \cdot \frac{C_i}{C_f}$$



programmable gain

digital input  $[g_{1,2,3}]$

determines gain  $g_{1,2,3}$



What's  $\tau$ ?  $\frac{1}{\omega_{pCL}}$

$$\omega_{pCL} = f_{Wu}$$

$$f = \frac{C_f}{C_i + C_f}$$

A note on caps  $Q = C \cdot V$

label the "+" side!

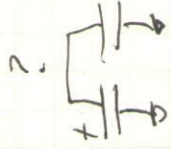
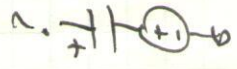
$$Q_- = Q_+$$

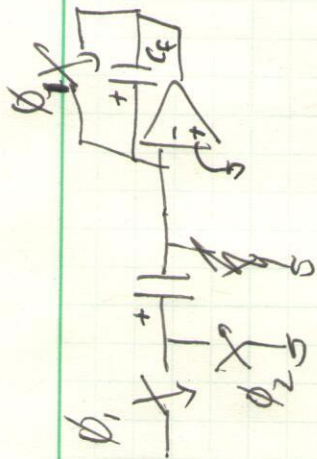
Real caps have parasitics - we will mostly ignore (24073)

Charge a cap to 1V



disconnect





same

same? no!

$$A_v = + \frac{C_i}{C_f}$$

optimistic pessimistic  $R_{on} = \frac{I_{DSAT}}{V_{DSAT}} = \frac{\mu_n C_{ox} \frac{W}{L} V_{OV}^2}{V_{OV}}$

$$R_{on} = \frac{2}{\mu_n C_{ox} \frac{W}{L} V_{OV}}$$

optimistic pessimistic

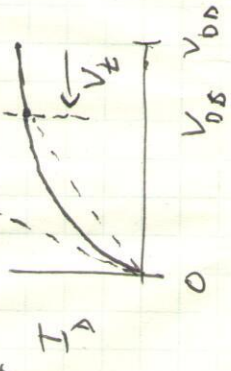
$$\frac{1}{R_{on}} = \frac{\partial I_D}{\partial V_{DS}} \Big|_{V_{GS}=0}$$

$$I_D = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T - \frac{1}{2} V_{DS}) V_{DS}$$

$$\frac{\partial I_D}{\partial V_{DS}} \Big|_{V_{GS}=0} = \mu_n C_{ox} \frac{W}{L} V_{OV} \quad R_{on} = \frac{1}{\mu_n C_{ox} \frac{W}{L} V_{OV}}$$

2x diff

Switches  $\phi$   $\phi$ ?  $R_{on}$   
 Charge injection (later)  
 Non-linear resistor

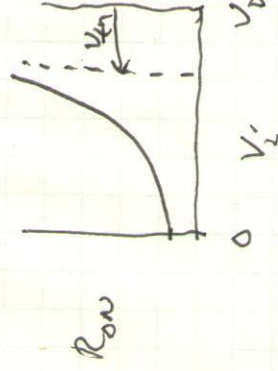


What value to use for  $R_{on}$ ?



$$I_D = \mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{in} - V_{Tn}) V_{DS}$$

$$R_{on} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{in} - V_{Tn})}$$



Nmos can pull high (above  $V_{DD} - V_{Tn}$ )

Pmos can pull low (below  $V_{Tp}$ )

body effect makes this worse  $|V_{Tn}|$  bigger