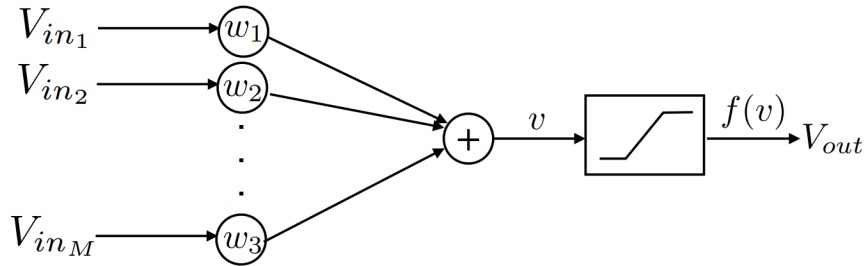


- iv. Update the error vector: $\vec{e} = \vec{y} - \mathbf{A}\vec{x}$
- v. Update the counter: $j = j + 1$

2. Brain-on-a-Chip with 16A Neurons (Spring 2017 Final)

Neurelic Inc, is a hot new startup building chips that emulate some of the brain functions (for example associative memory). As an intern, fresh out of 16A you get to implement the neural network circuits on this chip. The neural network consists of neurons that consist of the following blocks shown on the figure below.

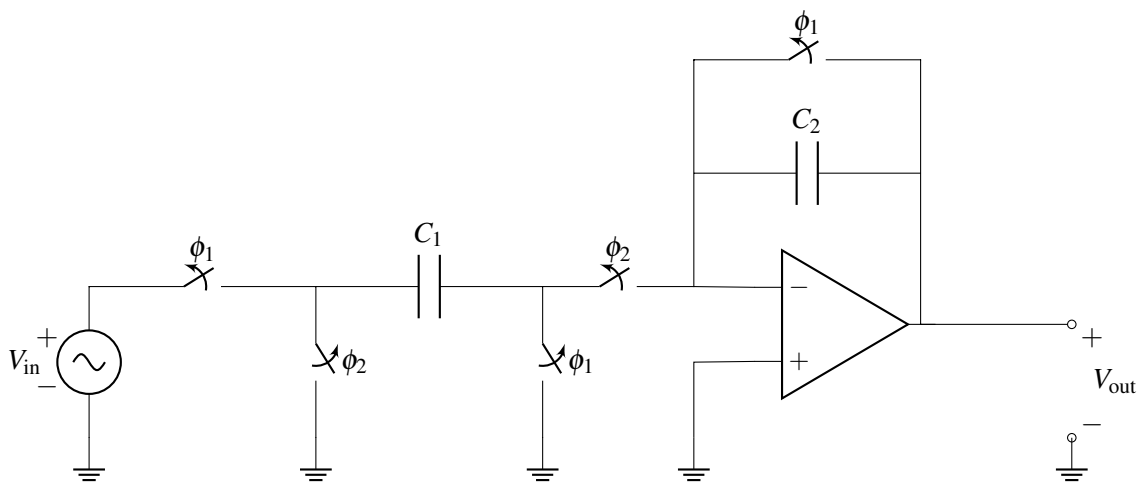


Input signals V_{in_i} are voltages from other neurons, which are multiplied by a constant weight w_i in each synapse and summed in the neuron. Each neuron also contains a nonlinear function (called a sigmoid) which is defined as

$$f(v) = \begin{cases} -1, & v \leq -1 \\ v, & -1 < v < 1 \\ +1, & v \geq +1 \end{cases}$$

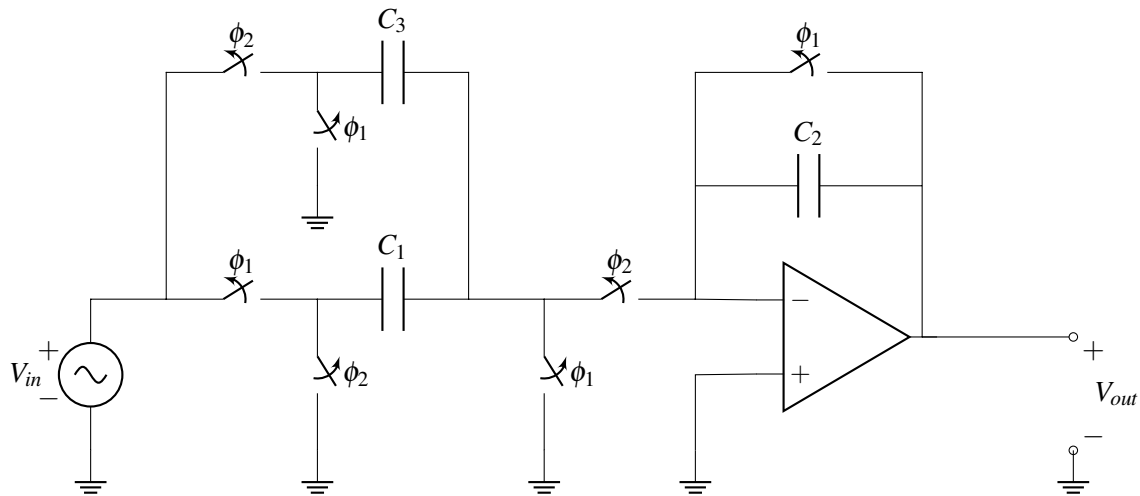
where v is the internal neuron voltage after the synapse summer and $f(v)$ is the neuron voltage output.

- (a) Your mentor suggests that you warm-up first by analyzing the circuit below to use as neuron with a single synapse. ϕ_1 and ϕ_2 are non-overlapping clock phases that control the circuit switches.



- i. Draw an equivalent circuit during ϕ_1 and write an expression for V_{out} as a function of V_{in} , C_1 and C_2 .

- ii. Draw an equivalent circuit during ϕ_2 and write an expression for V_{out} as a function of V_{in} , C_1 and C_2 .
- (b) **(Out of scope for this semester. Questions involving op amp supply voltages will not be in the final.)** Write an equation for V_{out} during ϕ_2 as a function of V_{in} for $C_1 = C_2$ and op-amp supply voltages of $\pm 1\text{ V}$. Briefly explain how this circuit implements the sigmoid function.
- (c) Then, your mentor shows you the following neuron circuit, which can realize both positive and negative synapse weight and create $V_{out} = w_1 V_{in}$ in ϕ_2 .



- i. Draw an equivalent circuit during ϕ_1 and write an expression for V_{out} as a function of V_{in} , C_1 , C_2 , and C_3 .
- ii. Draw an equivalent circuit during ϕ_2 and write an expression for V_{out} as a function of V_{in} , C_1 , C_2 , and C_3 .
- (d) Now it is your turn to implement a neuron that realizes the following function $V_{out} = w_1 V_{in_1} + w_2 V_{in_2}$. Draw the circuit, such that $w_1 = 1/2$ and $w_2 = -1/4$. Label all circuit elements appropriately. You should use a single op-amp and as many capacitors and switches as you need. All capacitors must be of size C_{unit} . Assume that the op-amp power supplies are $\pm 1\text{ V}$ (no need to draw them in the circuit). The circuit should operate in 2 phases, with $V_{out} = w_1 V_{in_1} + w_2 V_{in_2}$ in the second phase (ϕ_2), and reset in ϕ_1 .