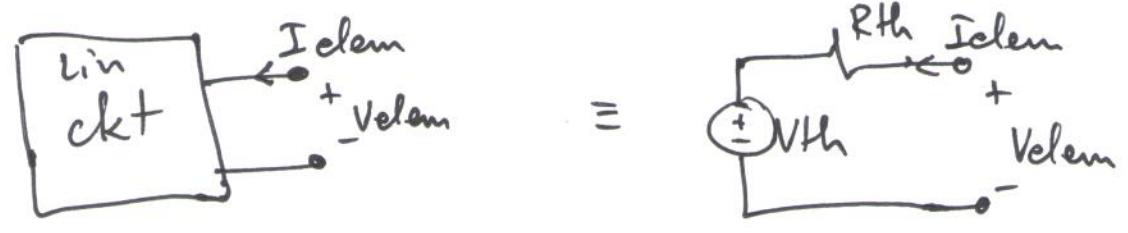
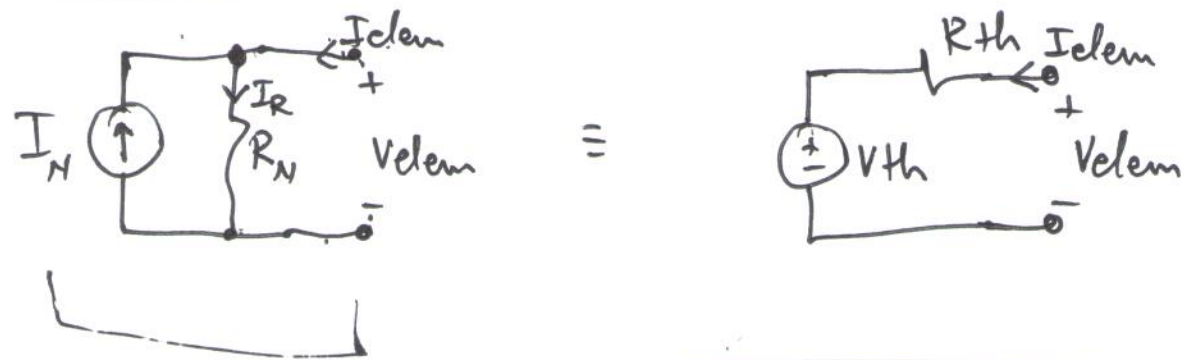


EE16A Touchscreen Module - Lecture 5

- * Norton equivalent & examples
- * Capacitive Touchscreen



Norton:



step 1 (V_{Th}): \Rightarrow $V_{Th} = I_N \cdot R_N$

Measure open-circuit voltage

$$V_{o.c} = I_N \cdot R_N$$

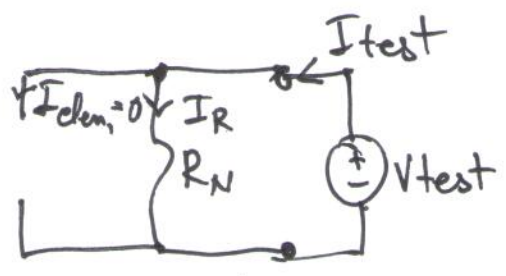
KCL: $I_N + I_{clemat} = I_R$ o b.c open-circuit

$$I_N = I_R$$

$$V_{clemat} = V_R = I_R \cdot R = \boxed{I_N \cdot R_N}$$

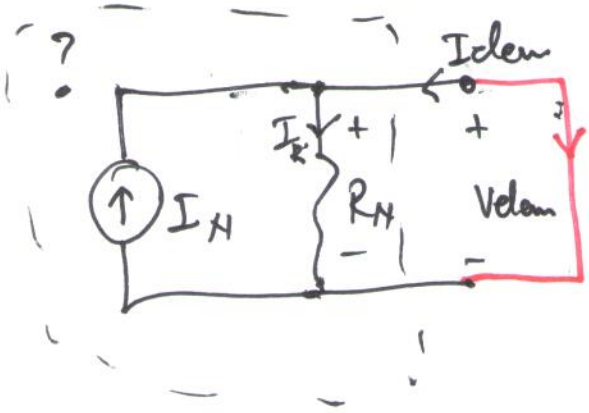
(12)

Step 2: Find R_{th} :



$$V_{test} = I_{test} \cdot R_N$$

$$R_{th} = \frac{V_{test}}{I_{test}} = R_N$$



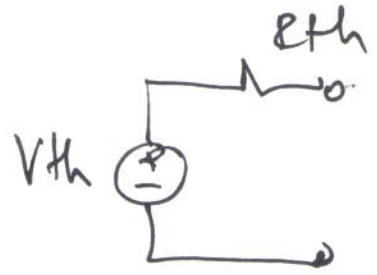
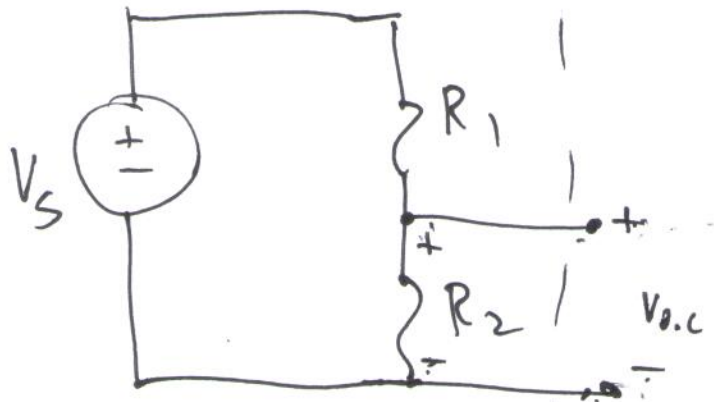
$$I_{s.c} = I_N$$

$$V_R = I_R \cdot R_N$$

$$V_R = V_{wire} = 0 \Rightarrow I_R = 0$$

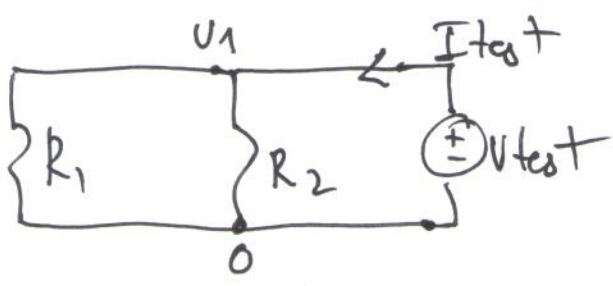
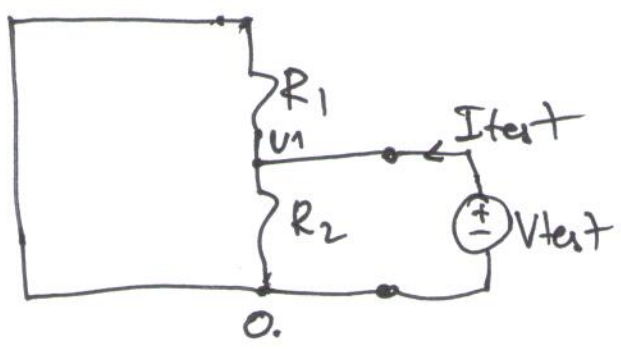
$$KCL: \underline{I_N} = \cancel{I_R} + \underline{I_{s.c}}$$

Q3



step 1:
$$V_{o.c.} = \frac{R_2}{R_1 + R_2} V_s = V_{th}$$

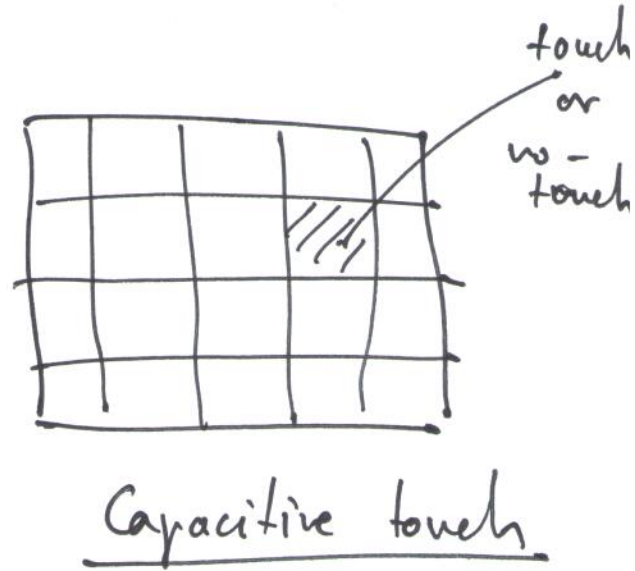
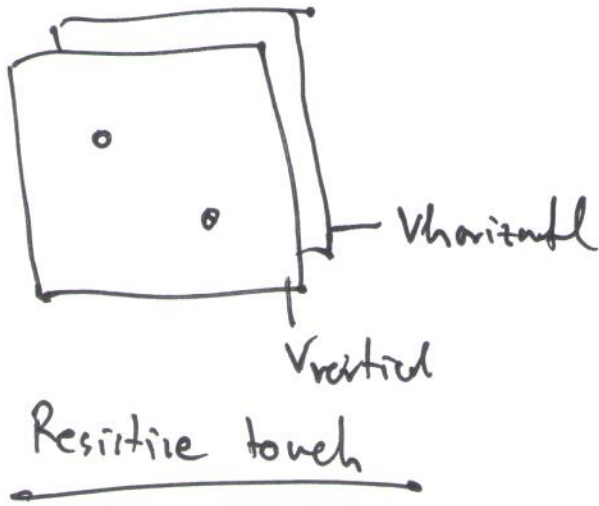
step 2: R_{th} (zero-out V_s)



$$R_{th} = R_1 \parallel R_2 = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

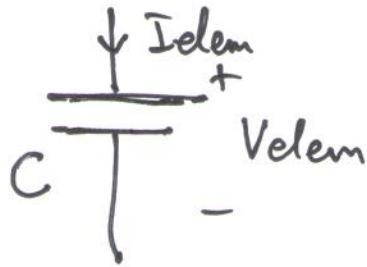
(14)

An improved touchscreen



Circuit model:

Capacitor
Symbol



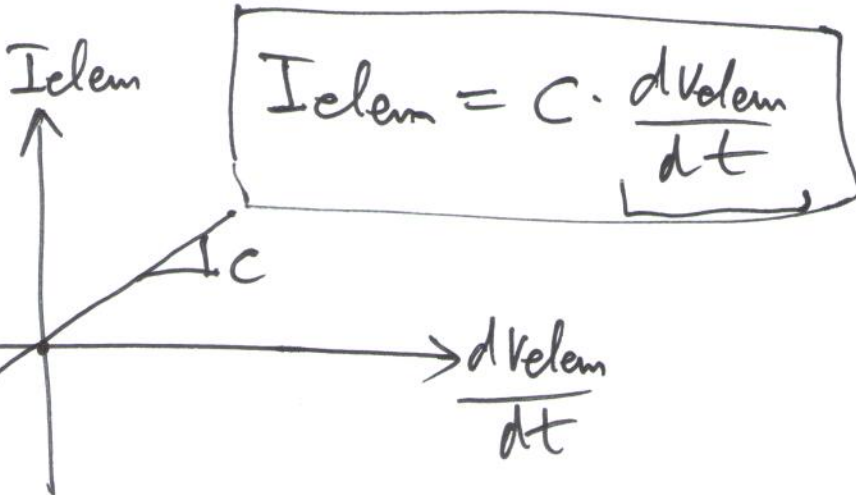
"I-V"

$$Q_{elem} = C \cdot V_{elem}$$

\uparrow \uparrow \uparrow
 [C] [F] [V]
 Farad

$$I_{elem} = \frac{dQ_{elem}}{dt} = C \cdot \frac{dV_{elem}}{dt}$$

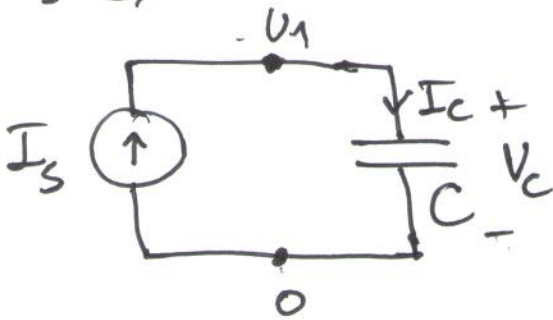
(assume C does not change in time)



$$I_{elem} = C \cdot \frac{dV_{elem}}{dt}$$

(25)

simple ckt #1:



KCL: $I_s = I_c$ ✓

elem. def for: $I_c = C \cdot \frac{dV_c}{dt}$

KVL: $V_c = U_1$

$$\int_0^t I_s \cdot dt = \int_{U_1(0)}^{U_1(t)} C dU_1$$

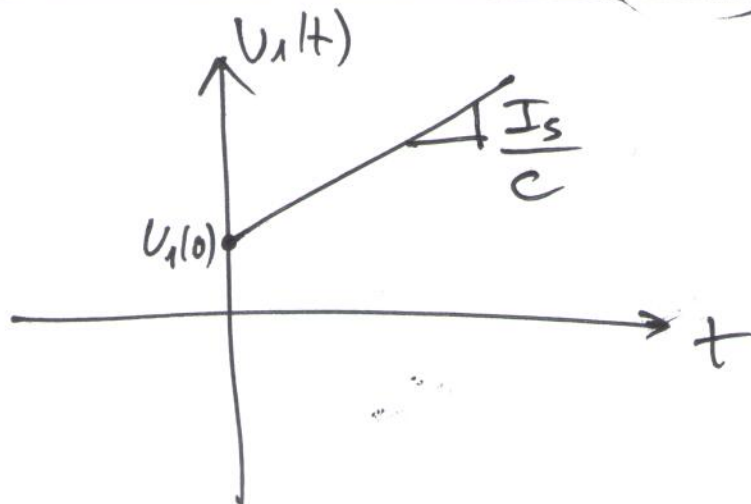
$I_s = C \frac{dU_1}{dt} \Rightarrow U_1$

$\frac{I_s}{C} = \frac{dU_1}{dt}$
rate

$$I_s \cdot (t-0) = C \cdot [U_1(t) - U_1(0)]$$

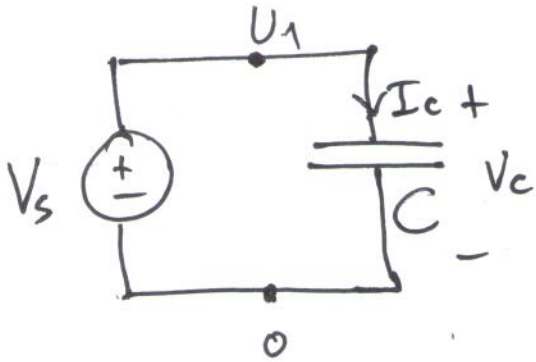
$$I_s \cdot t = C \cdot [U_1(t) - U_1(0)]$$

$$U_1(t) = \frac{I_s}{C} \cdot t + U_1(0)$$



16

Simple ckt #2:

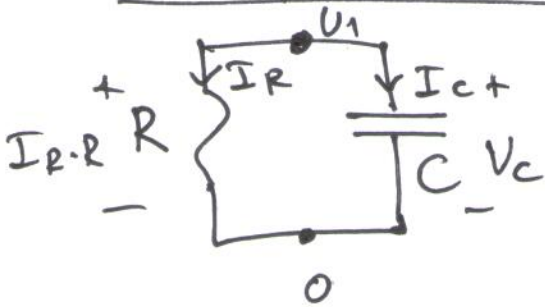


$$U_1 = V_s$$

$$V_c = U_1 \Rightarrow V_c = V_s$$

$$I_c = C \cdot \frac{dV_c}{dt} = C \cdot \frac{dV_s}{dt} = 0$$

Simple ckt #3:



steady-state means when voltages settle

I am looking for U_1 value when $U_1 = \text{const}$ (i.e. in steady-state)

$$U_1 = 0$$

$$I_c = 0$$

KCL: $I_R + I_c = 0$

Ohm's law: $I_R \cdot R = 0$

$$U_1 = I_R \cdot R = 0$$

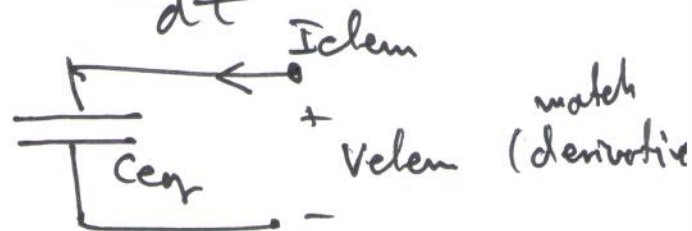
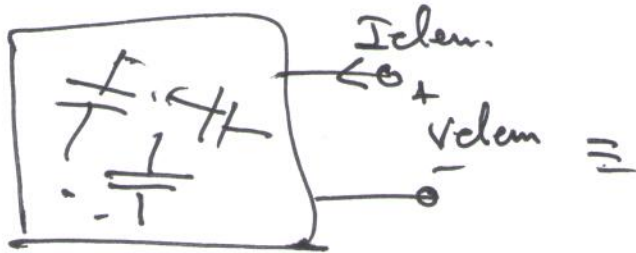
(17)

Equivalent ckt with capacitors:

* Capacitor-only ckt

~~step 1: find V_{th} or I_N No source~~

step 2: $C_{eq} = \frac{I_{elem}}{\frac{dV_{elem}}{dt}}$

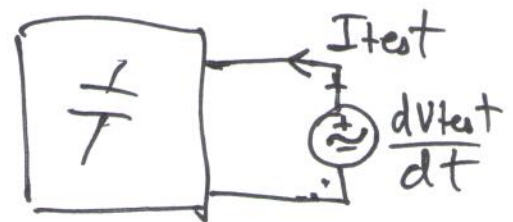
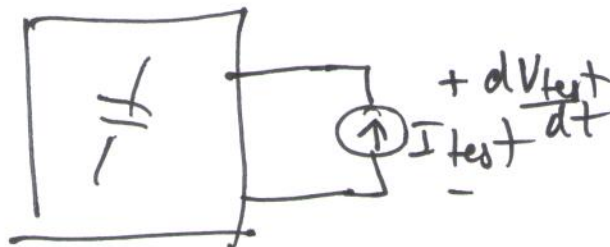


a) Apply I_{test} and measure $\frac{dV_{test}}{dt}$

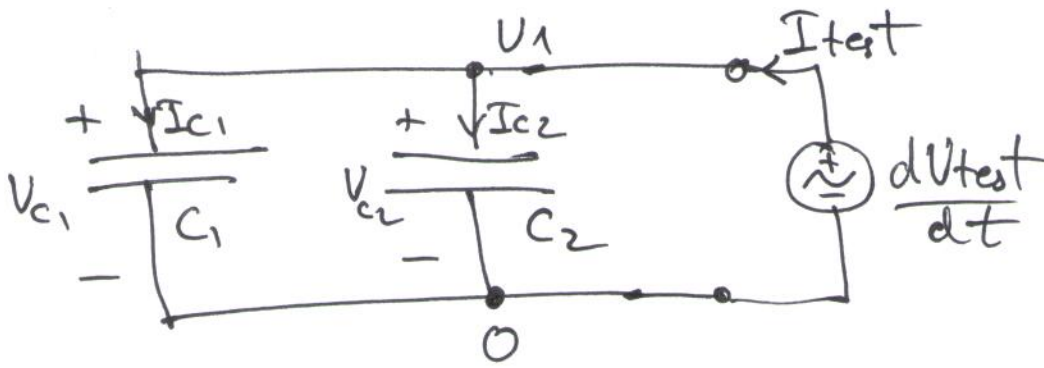
or

b) Apply $\frac{dV_{test}}{dt}$ and measure I_{test}

$\Rightarrow C_{eq} = \frac{I_{test}}{\frac{dV_{test}}{dt}}$



(8)



$$V_{c1} = U_1, \quad V_{c2} = U_1 \quad \text{and} \quad U_1 = \frac{dV_{test}}{dt}$$

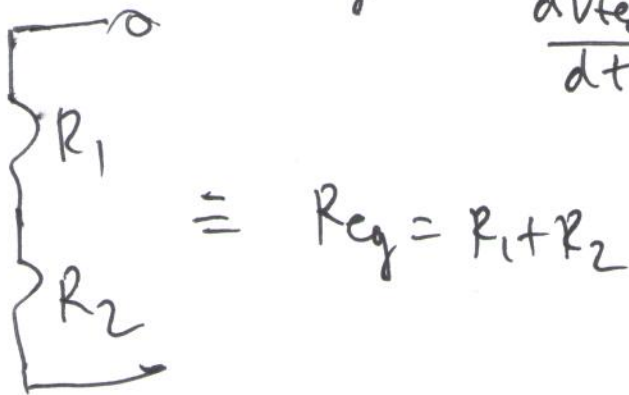
$$I_{c1} = C_1 \frac{dV_{c1}}{dt} = C_1 \frac{dU_1}{dt} \quad \left. \begin{array}{l} \frac{dU_1}{dt} = \frac{dV_{test}}{dt} \end{array} \right\}$$

$$I_{c2} = C_2 \cdot \frac{dV_{c2}}{dt} = C_2 \cdot \frac{dU_1}{dt}$$

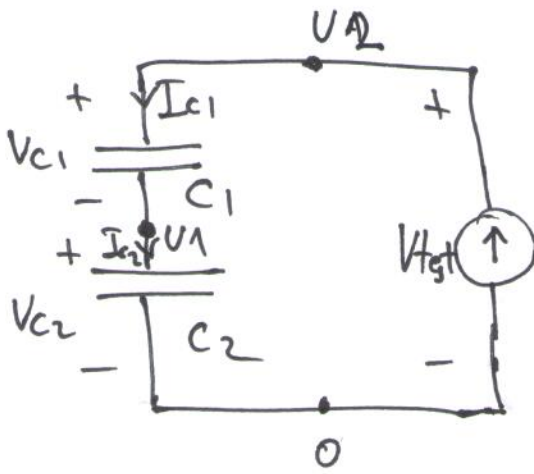
$$\text{KCL: } I_{test} = I_{c1} + I_{c2} = C_1 \frac{dV_{test}}{dt} + C_2 \frac{dV_{test}}{dt}$$

$$I_{test} = (C_1 + C_2) \frac{dV_{test}}{dt}$$

$$C_{eq} = \frac{I_{test}}{\frac{dV_{test}}{dt}} = C_1 + C_2$$



(19)



KCL: $I_{C1} = I_{C2} = \underline{I_{test}}$

elements: $I_{C2} = C_2 \frac{dV_{C2}}{dt}$

$I_{C1} = C_1 \cdot \frac{dV_{C1}}{dt}$

KVL: $V_{C2} = U_1$
 $V_{C1} = U_2 - U_1$

$U_2 = V_{test}$

$\frac{dU_1}{dt} = \frac{I_{test}}{C_2}$

$\frac{dV_{C2}}{dt} - \frac{dV_{C1}}{dt} = \frac{I_{test}}{C_1} \Rightarrow \frac{dU_2}{dt} = \frac{dV_{C1}}{dt} + \frac{I_{test}}{C_1}$

$\frac{dV_{test}}{dt} = I_{test} \cdot \left(\frac{1}{C_1} + \frac{1}{C_2} \right)$

$C_{eq} = \frac{I_{test}}{\frac{dV_{test}}{dt}} = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2}} = \frac{C_1 C_2}{C_1 + C_2} = C_{1||C_2}$

$C_{eq} = C_1 || C_2$ → operator (mathematical)