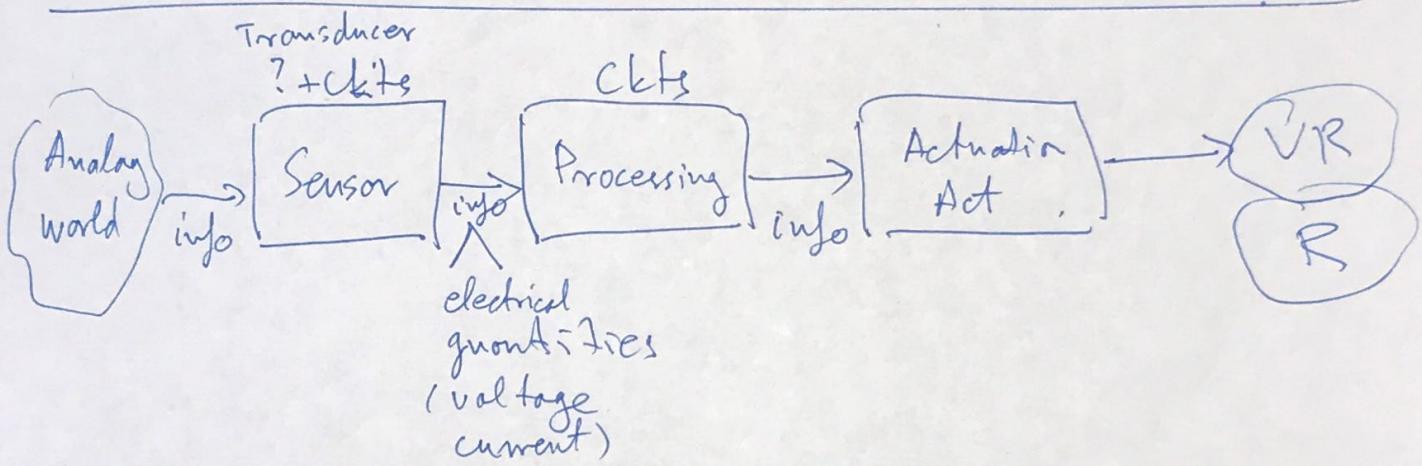


## Lecture 1 - Module 2

Today:

- \* Sensing, Processing & Actuation Systems
- \* Circuit Analysis Algorithm (Note 11)



Electrical Circuit Analysis Algorithm (tool)

SPICE

Nagel, Pederson, Bohm

<u>Quantities:</u>	<u>Analytical Symbol</u>	<u>Units</u>
Voltage	V	Volts [V]
Current	I	Amps [A]
Resistance	R	Ohms [ $\Omega$ ]

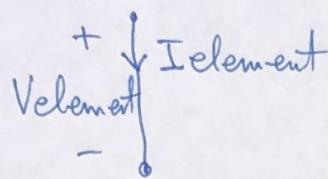
Circuit diagram (collection of elements, where each element has some voltage across it and some current through it)

+ ↓ I<sub>element</sub>  
V<sub>element</sub>      -

l2

## Key circuit elements:

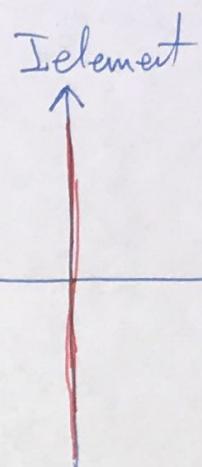
### ① Wire



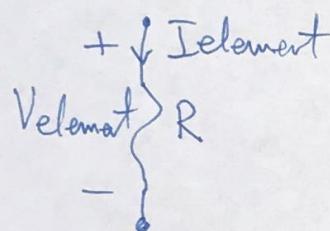
$$V_{\text{element}} = 0$$

$$I_{\text{element}} = ?$$

(set by the  
ext. circuit)

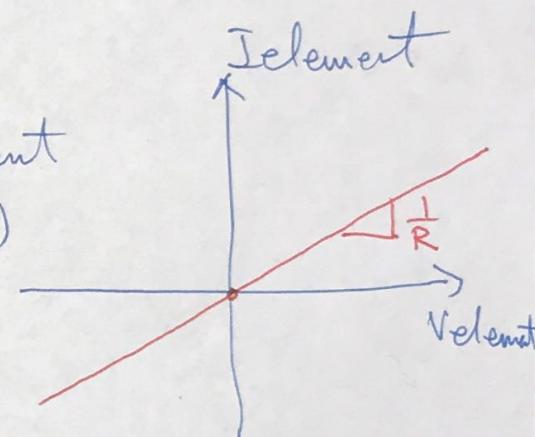


### ② Resistor

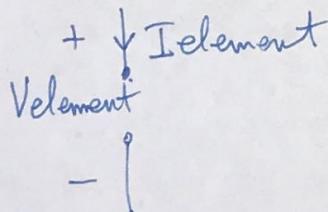


$$V_{\text{element}} = R \cdot I_{\text{element}}$$

(Ohm's law)



### ③ "Open" circuit



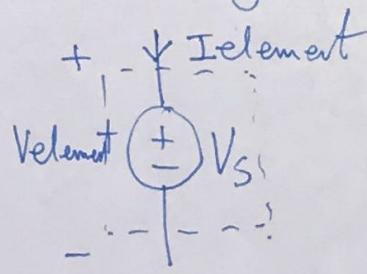
$$I_{\text{element}} = 0$$

$$V_{\text{element}} = ?$$

(set by ext. ckt)



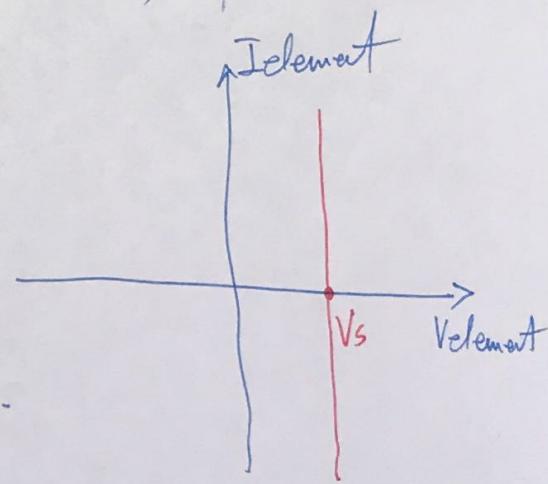
### ④ Voltage source



$$V_{\text{element}} = V_s$$

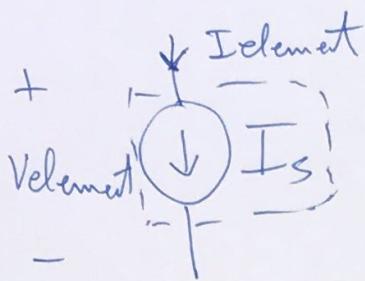
$$I_{\text{element}} = ?$$

(set by ext.  
ckt)



(l3)

## ⑤ Current source



$$I_{\text{element}} = I_s$$

$$V_{\text{element}} = ?$$

(set by ext. cir.)

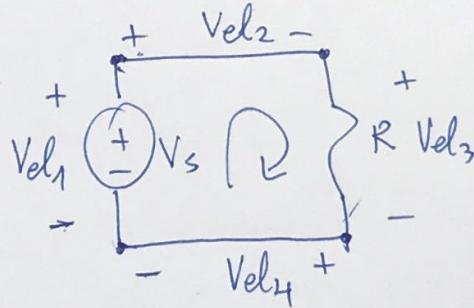


$V_{\text{element}}$  and  $I_{\text{element}}$  can be positive or negative or zero.  $\in \mathbb{R}$

### Rules of circuit analysis:

① KVL: sum of voltages across the elements in a loop = 0

example :



$$Vel_1 + Vel_2 + Vel_3 + Vel_4 = 0$$

$$Vel_1 - Vel_2 - Vel_3 - Vel_4 = 0$$

$$-Vel_1 + Vel_2 + Vel_3 + Vel_4 = 0$$

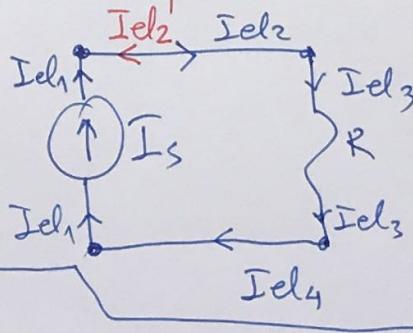
$\begin{matrix} Vel_1 \\ \hline + \\ Vel_2 \\ \hline - \\ Vel_3 \\ \hline + \\ Vel_4 \end{matrix}$

② KCL: The current flowing must equal the current flowing into any junction

$$I_{el1} = -I_{el2}'$$

$$I_{el1} + I_{el2}' = 0$$

example 2:

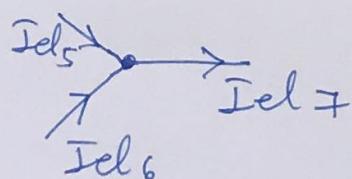


$$I_{el1} = I_{el2} \quad I_{el1} - I_{el2} = 0$$

$$I_{el2} = I_{el3}$$

$$I_{el3} = I_{el4}$$

~~$$I_{el4} = I_{el1}$$~~

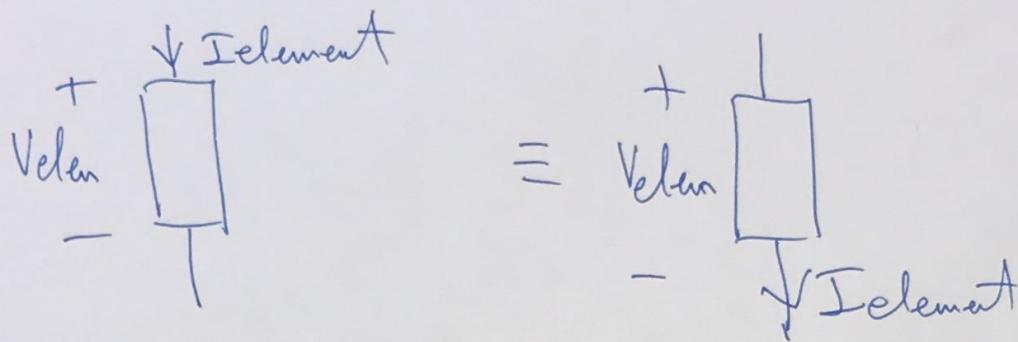


$$I_{el5} + I_{el6} - I_{el7} = 0$$

$$I_{el5} + I_{el6} = I_{el7}$$

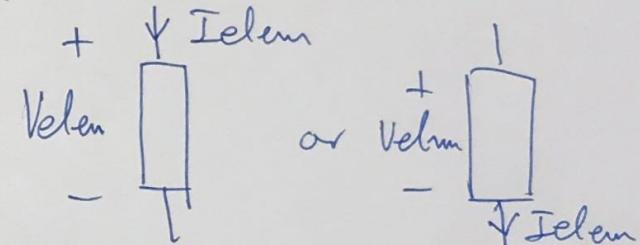
l4

KCL within the element :



Passive - sign convention:

Ielement goes into a + or out of  
a - terminal label of Ielem.      + ↓ Ielem      |

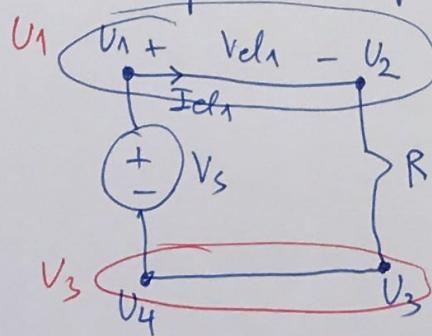


Circuit analysis algorithm:

$(V_{jk})$  voltage = difference of two potentials  $(V_j, V_k)$

$$V_{jk} = V_j - V_k$$

Find: currents through elements and potentials  
of inputs/outputs of each element (junctions)



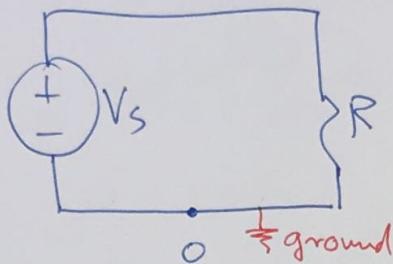
$U_1, \dots, U_4$  potentials

$$V_{el1} = U_1 - U_2$$

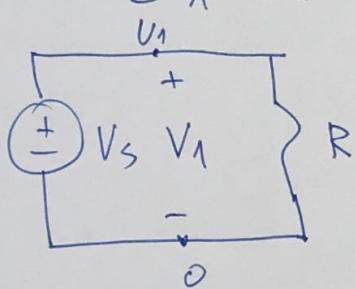
$$\underline{\text{def: } V_{el1} = 0} \Rightarrow 0 = U_1 - U_2$$

node is an equi-potential part of the net.  $U_1 = U_2$   
 - collapse junctions into nodes

(l5) step 1: Pick a "reference" node and label as a "0" potential. All voltages relative to this node.

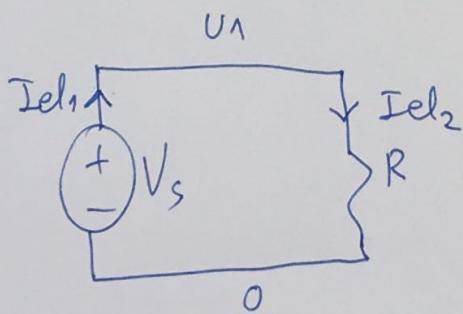


step 2: Label all remaining nodes as potentials  $U_1 \dots U_{N-1}$



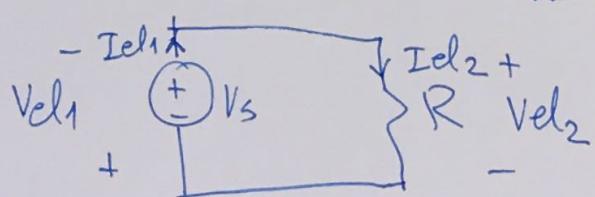
$$U_1 - 0 = V_1 \text{ (voltage between node 1 and node "0")}$$

step 3: Label all branch currents with  $I_{el_m}$ . Arbitrarily pick directions of  $I_{el_m}$



$$[I_{el_1} \dots I_{el_k}]$$

step 4: Add  $\pm V_{el}$  (element voltages) to each element following the Passive-sign convention



(indep. of what is in the element)