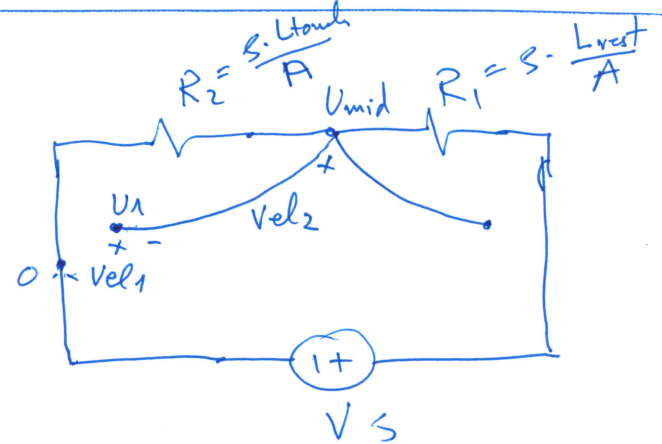
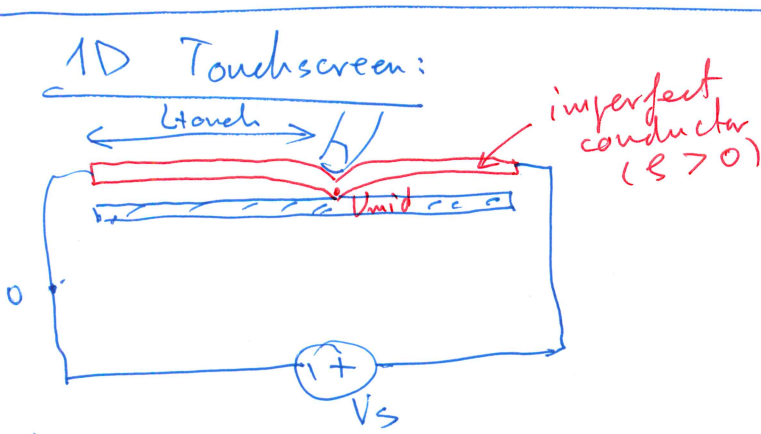


# Lecture 3 - Module 2

- Today:
- \* 1D Touchscreen wrap-up
  - \* Measuring voltage & current
  - \* Power
  - \* An interesting det (start)
- Note 13 & part of Note 14



Model 0:  $V_{mid} - 0 = V_{mid} = \frac{R_2}{R_1 + R_2} \cdot V_s = \frac{L_{touch}}{L} \cdot V_s$

Model 1: = ideal wire  
 el 1: open-circuit  
 el 2: wire

el 1:  $V_{el1} = U_1 - 0$  (def. of elem. voltage) (1)

el 2:  $V_{el2} = V_{mid} - U_1$  (def. of elem. voltage) (2)

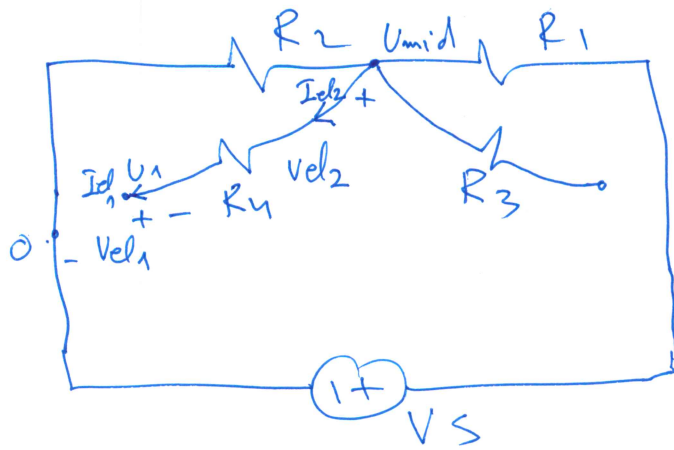
(1)  $U_1 = V_{el1}$

(3)  $V_{el2} = \underline{0}$  (elem. definition)

$V_{mid} - U_1 = 0 \Rightarrow V_{mid} - V_{el1} = 0 \Rightarrow \boxed{V_{el1} = V_{mid}}$

Measure  $V_{mid}$  at  $V_{el1}$  regardless of the background conductor material & value of  $L_{touch}$ .

(2) Model 2 :  imperfect conductor (resistor)



el1: open-circuit  
el2: resistor

KCL :

$$I_{el1} = I_{el2}$$

el1 def:  $I_{el1} = 0$

$$\Downarrow$$

$$I_{el2} = 0$$

el2 def:  $V_{el2} = I_{el2} \cdot R_4$

$$V_{el2} = 0$$

( $V_{el2}$  def):  $V_{el2} = V_{mid} - V_1$

$$V_{mid} - V_1 = 0$$

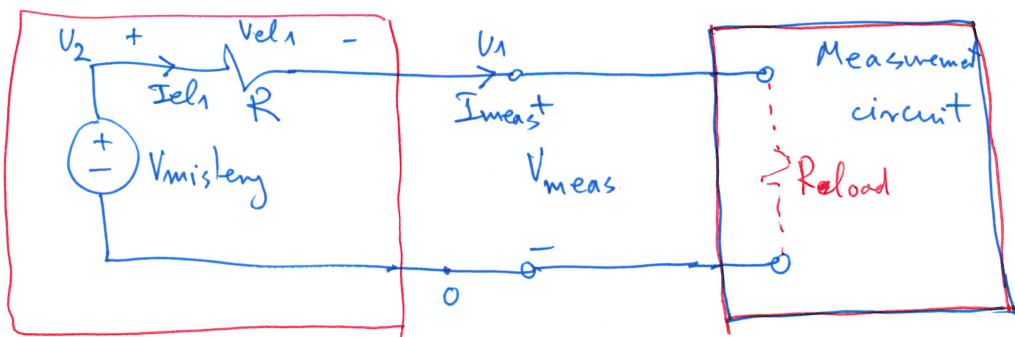
$$V_{mid} = V_1$$

$$V_{el1} = V_{mid}$$

( $V_{el1}$  def):  $V_{el1} = V_1 - 0 = V_1$

Measure  $V_{mid}$  at  $V_{el1}$  regardless of bodybone conductor material.

23



Want:

$$V_{meas} = V_{mistery}$$

$$V_{el1} = I_{el1} \cdot R \quad (\text{elem-def})$$

(KCL)

$$I_{el1} = I_{meas}$$

$$V_{mistery} = U_2 - 0 \quad (\text{voltage def})$$

$$V_{meas} = U_1 - 0 \quad (\text{voltage def})$$

$$\rightarrow V_{el1} = U_2 - U_1 \quad (\text{voltage def})$$

$$\rightarrow I_{el1} \cdot R = V_{mistery} - V_{meas}$$

$$I_{meas} \cdot R = V_{mistery} - V_{meas}$$

$$V_{meas} = V_{mistery} - I_{meas} \cdot R$$

when  $I_{meas} = 0 \Rightarrow V_{meas} = V_{mistery}$ .

$$I_{meas} = \frac{V_{meas}}{R_{load}}$$

Measurement should not change the energy of the circuit (cause energy dissipation)

Define a voltage between points A & B as:

$$V_{AB} = \frac{dE_{AB}}{dq}$$

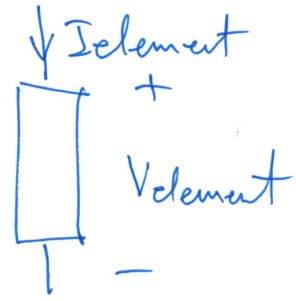
$dE_{AB}$  - energy needed to move a particle  $dq$  from B to A

$$\text{Power: (rate of energy change): } P = \frac{dE}{dt} = \left( \frac{dE}{dq} \right) \cdot \left( \frac{dq}{dt} \right) = V \cdot I$$

Q4

passive - sign convention:

$$P_{element} = \underbrace{V_{element}} \cdot I_{element} \quad (def)$$

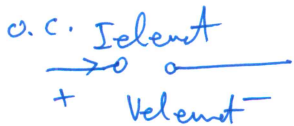


$$\Rightarrow \left| I_{element} - R \cdot I_{element} = R \cdot I_{element}^2 \geq 0 \right.$$

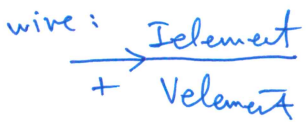
if element  
is a resistor

$$V_{element} = I_{element} \cdot R$$

$$= V_{element} \cdot \frac{V_{element}}{R} = \frac{V_{element}^2}{R} \geq 0$$



$$P_{element} = V_{element} \cdot \cancel{I_{element}} = 0 \quad (def \text{ a.c.})$$

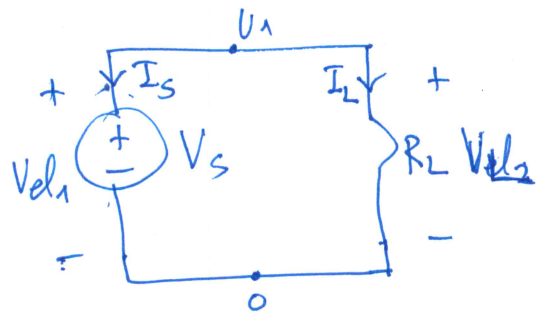


$$P_{element} = \cancel{V_{element}} \cdot I_{element} = 0 \quad (def \text{ wire})$$

$$\text{Units : Power [W] = [V] \cdot [A]}$$

25

Example:



(KCL):  $I_s = -I_L$

$$V_{ch1} = U_1 - 0$$

$$V_L = U_1 - 0 \Rightarrow V_{ch1} = V_L$$

$$P_s = V_{ch1} \cdot I_s$$

$$= V_s \cdot I_s \quad (\text{el. df source})$$

$$P_L = V_L \cdot I_L \quad (\text{def})$$

$$= V_L \cdot (-I_s)$$

$$= V_{ch1} \cdot (-I_s)$$

$$= V_s \cdot (-I_s) \quad (\text{def source})$$

$$P_s = V_s \cdot I_s$$

$$P_L = -V_s \cdot I_s$$

$$P_s = -P_L$$

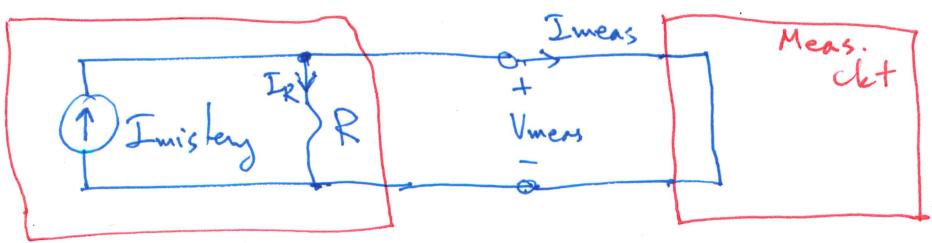
$$P_L \geq 0$$

b/c of  $R_L$

$$P_s \leq 0$$

$$P_L + P_s = 0$$

Conservation of energy (power)



Task:  
Measure  $\underline{I_{mistry}}$   
 $I_{meas} = I_{mistry}$

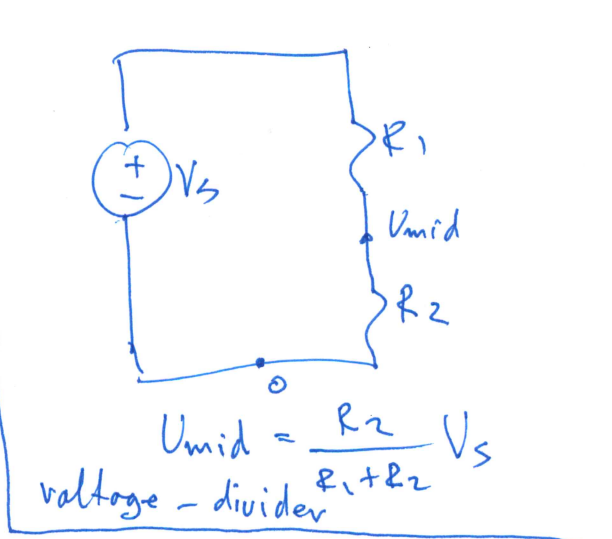
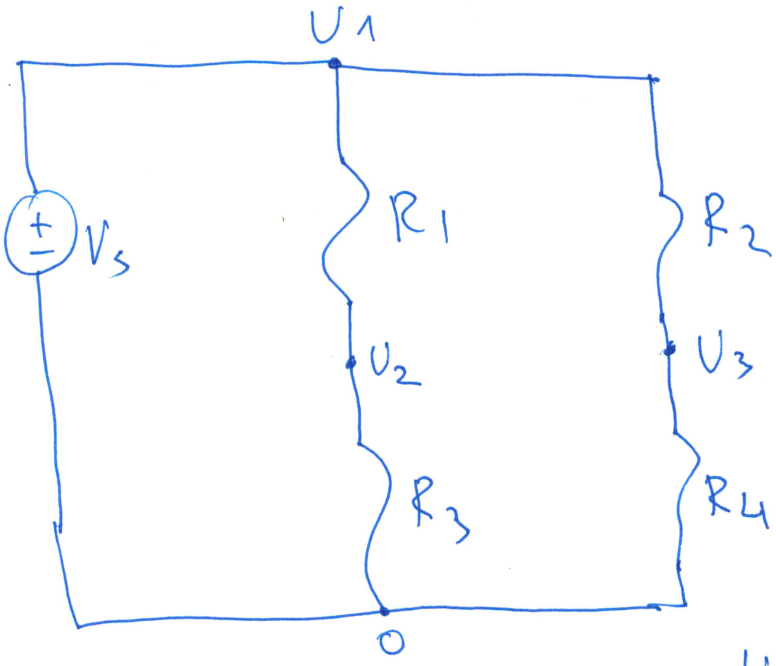
(KCL)  $I_{mistry} = I_R + I_{meas}$        $V_{meas} = I_R \cdot R$

$$P_{meas} = \overset{0}{V_{meas}} \cdot I_{meas} = \frac{V_{meas}}{R} + I_{meas}$$

wire  $\Rightarrow V_{meas} = 0$  (def)  $\Rightarrow \underline{I_{mistry} = I_{meas}}$

Q6

An interesting circuit :



What are  $U_2$  &  $U_3$ ?

$$V_s = U_1 - 0 \text{ (def)}$$

$$U_2 = \frac{R_3}{R_1 + R_3} V_s \quad U_3 = \frac{R_4}{R_2 + R_4} \cdot V_s$$

$$U_2 = \frac{R_3}{R_1 + R_3} \cdot (U_1 - 0) \quad (v. \text{ div})$$

$$U_3 = \frac{R_4}{R_2 + R_4} \cdot (U_1 - 0) \quad (v. \text{ div})$$