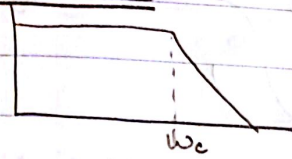


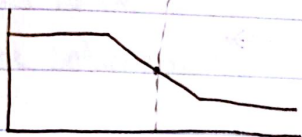
Discussion 9

- Bode plots & review of phase
- Importance of phase
 - w/ multiple signals
- Stacking filters

Bode Plots



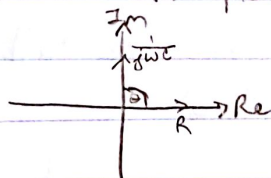
for each corner freq



90° phase shift

Where does 90° come from?

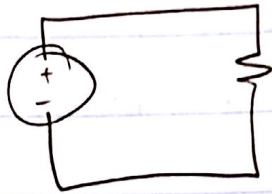
Recall the $Re-Im$ plot



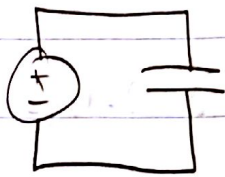
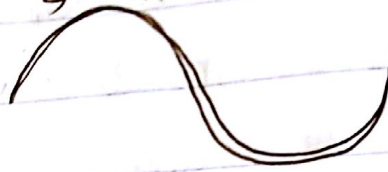
Some impedance R & $\frac{1}{j\omega C}$

Phase is θ from the origin. We can immediately see that R has $\theta = 0$ & $\frac{1}{j\omega C}$ has $\theta = 90^\circ$.

Because capacitors don't like voltage changing & pull a lot of current to stop voltage changing, they cause I & V to get out of alignment \leftarrow phase

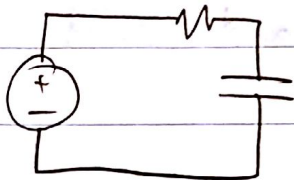
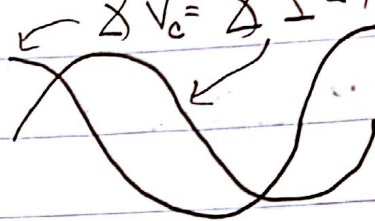


$$\phi V_R = \phi I$$

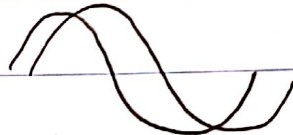


$$\phi V_C = \phi I - 90^\circ$$

V_C lags I

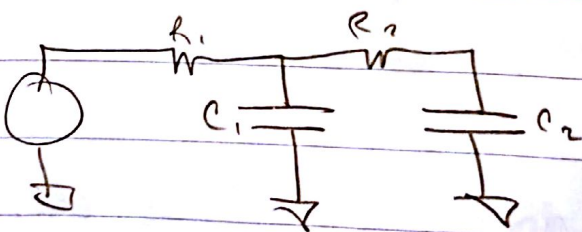
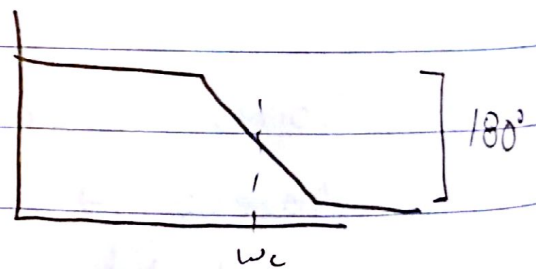
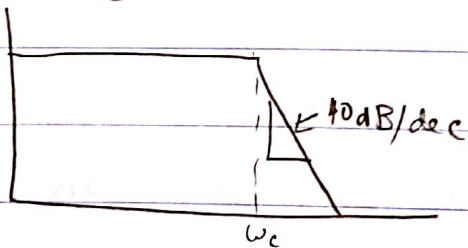


$$\phi V_C = \phi I + \theta$$



phase calculated as $\tan^{-1}\left(\frac{Z_C}{R}\right)$

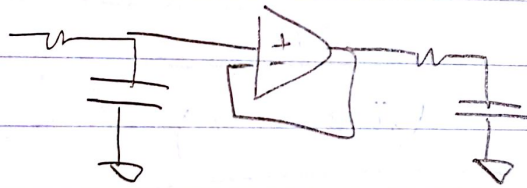
Recall last week when we talked about making sharper filters



Turns out choosing an R_1 , R_2 , C_1 , C_2 to get that ω_c in the same place is very tricky

$$H(s) = \frac{1}{s^2 R_1 R_2 C_1 C_2 + s [R_1 (C_1 + C_2) + R_2 C_2] + 1}$$

This is because the two capacitors are interacting. How to make that stop?



Now, $A(s) = (\text{Normal RC})^2 = \frac{1}{(sRC + 1)^2}$