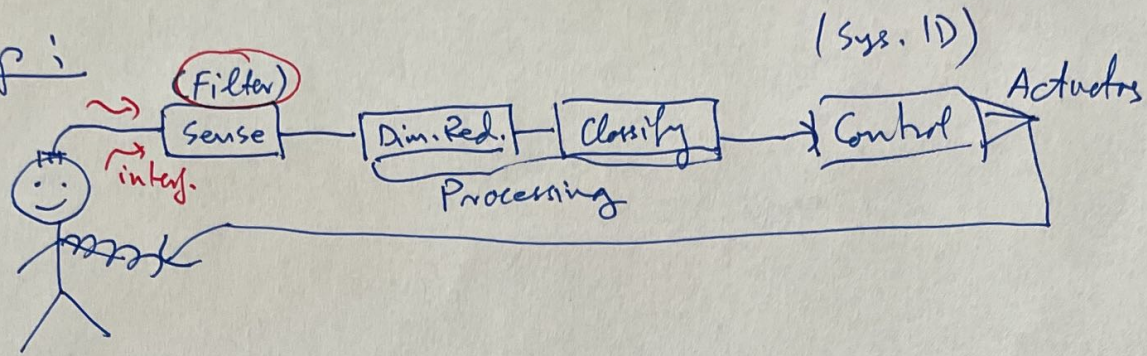


Recaps:



Design perspective:

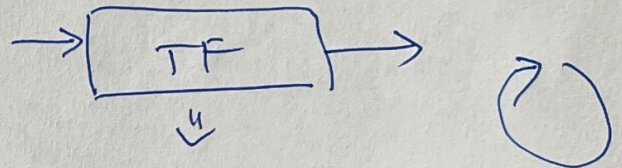
e.g. Filter

Step 1: Specifications

Attenuate intef. 100x while keeping the signal intact.

Step 2: Game-plan (Strategy)
System-level.

- helps derive the sub-block specs.

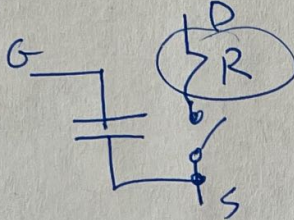


Step 3: Implementation (Circuits)

- may evaluate some candidates RC RL

Step 4: Validation $\nabla(s_i)$ Verification (pre- s_i) :

Does the design meet the specification over all manufacturing variations & operating conditions.

Motivation	Modeling	Math
<p>Why don't computers work ∞ fast?</p> <p>- why are they heating up?</p> <p>- average AI training run $\sim 1-10$ MW & lasts for days</p>	<p><u>Logic</u>: consist of transistors.</p> <p>Transistor: NMOS/PMOS modeled as switches + R & C</p>  <p>RC - time constants & delays</p> <p>Power spent on R</p>	<p>Diff. equations.</p> $\frac{d}{dt}x(t) = \lambda x(t) + u(t)$ <p>* Solve by guess & check</p> <p>* Based on uniqueness proofs</p> <p><u>Transformations</u>:</p> <ol style="list-style-type: none"> 1) Change of variables 2) Discretization & limits

Motivation

How can we filter interference & keep the signal?

Modeling

- * Analog information processing with filters
- * Inductor as a "dual" to capacitor
- * Impedance idea
 - reduces the R, L, C circuit to look like a resistive net
- * Transfer functions: impedances (j ω)
 - * Low-pass
 - * high-pass
 - * Bandpass
 - * Magnitude plots
 - * Phase plots
 - Composition of filters (TFs)
 - * Multiply TFs (series)
 - * Sometimes add (parallel)

Bode-plot approximations

Math

- Systems of diff-eqns.
- Transformations:
- * Vector "change-of-variables"
 - coordinate changes
 - Eigenbasis
 - * complex evectors
 - * complex evalues
- Reduce the sys. \Rightarrow 1. diff-eq. to a sys of lin. eqs.
- \Downarrow
- * Transfer functions

Another perspective: By themes & patterns (14)

(1) Reductions (the most important theme of 16B₀)

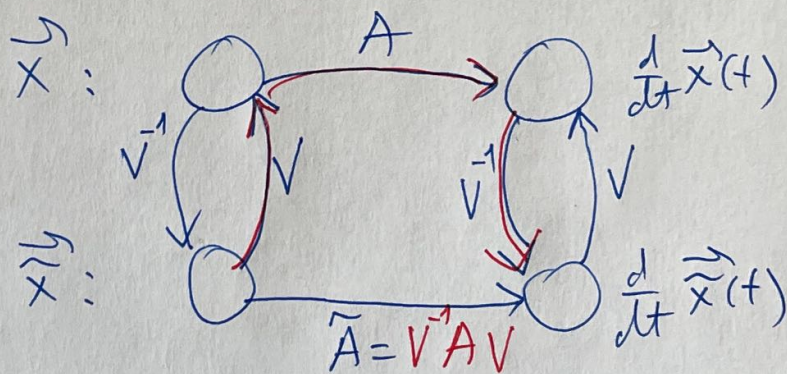
Turn the problem you don't **yet** know how to solve into a problem(s) you know how to solve.

* Derivatives \Rightarrow Solve homog. diff. eqs.
Guess & check

* \Rightarrow non-homog. with const. input
change-of variables

\Rightarrow cont. input
piece-wise & limit

$$\vec{x} = V \tilde{x}$$



Eigenbasis (when it works): reduces to a set of parallel problems (scalars)

Orthonormal basis: Preserve length, angles
easy inverses (conj. transpose)
easy projections.

Phasors are what mix of transformations? (15)

- coordinate change
- linearization (if needed)
- Eigenbasis.
- (out-of-scope) orthonormal basis