


EECS192 Lecture 10

Power and Control

Mar. 30, 2021

Topics

- 
- Checkpoint 8: Step+ telemetry
 - HW 2 Simulation (due Fri 4/2 6 pm)
 - Progress report (due Fri 4/9 8 pm)
 - ESP32 A/D Issues
 - Quiz3- MOSFET 3/30
 - Motor Drive- details
 - Control Fundamentals

Planned Cory Courtyard Track

Thu and Friday 2-4 pm, supervised by staff member David Au.
All Covid protocols to be followed.
Details on Piazza when set up.



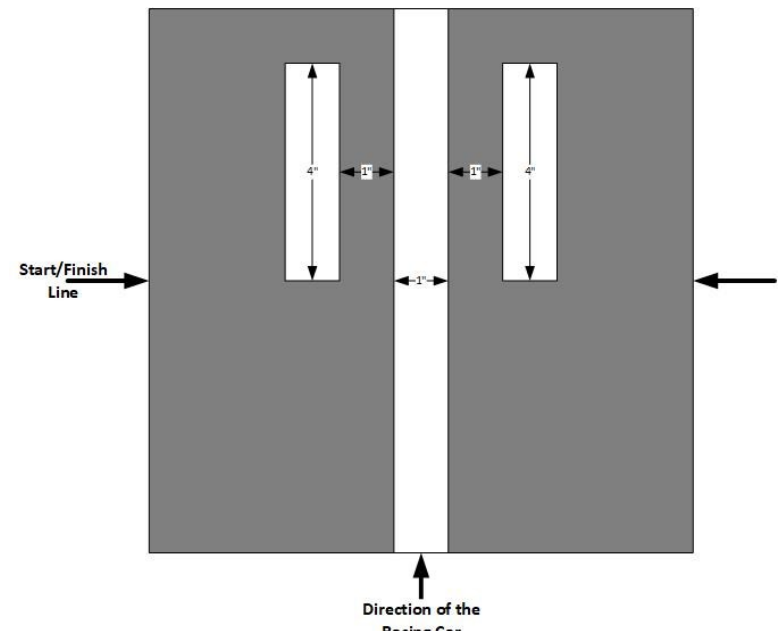
All curves minimum radius 3 feet (bigger radius is fine)
(use 3 foot string and mark circle with chalk)

Checkpoint 8: Stopping (Fri 4/9)

Set up a straight or curved track with length sufficient for car to accelerate to (ideally) 2 m/sec or better and stop when it sees the stop pattern.

Checkoff Procedure

- C8.1 Show car driving on track and then doing emergency stop from remote command.
- C8.2 Show car driving on track and doing emergency stop when it crosses NATCAR stop marking of parallel lines. [Natcar Finish Line](#)
- C8.3 Show telemetry plot of speed and other relevant parameters.
- C8.4 All members must fill out the checkpoint survey before the checkoff close. Completion is individually graded.



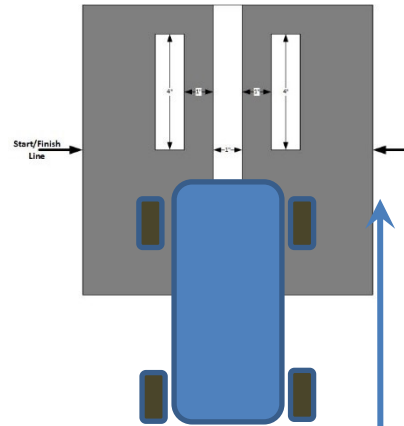
NATCAR Notes

1. Car can start in region shown (running start or avoid seeing stop line...) up to ``several feet'' behind start/stop line

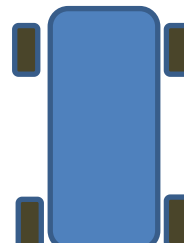
2. A running car can continue running for consecutive laps. If car is doing multiple laps without stopping, 4 second penalty is applied to intermediate laps.

The car must automatically stop within 6 feet of the finish line after finishing the race.

A penalty of 4 seconds will be added to the lap time for any car that does not automatically stop within the required region.



Permitted
Start region

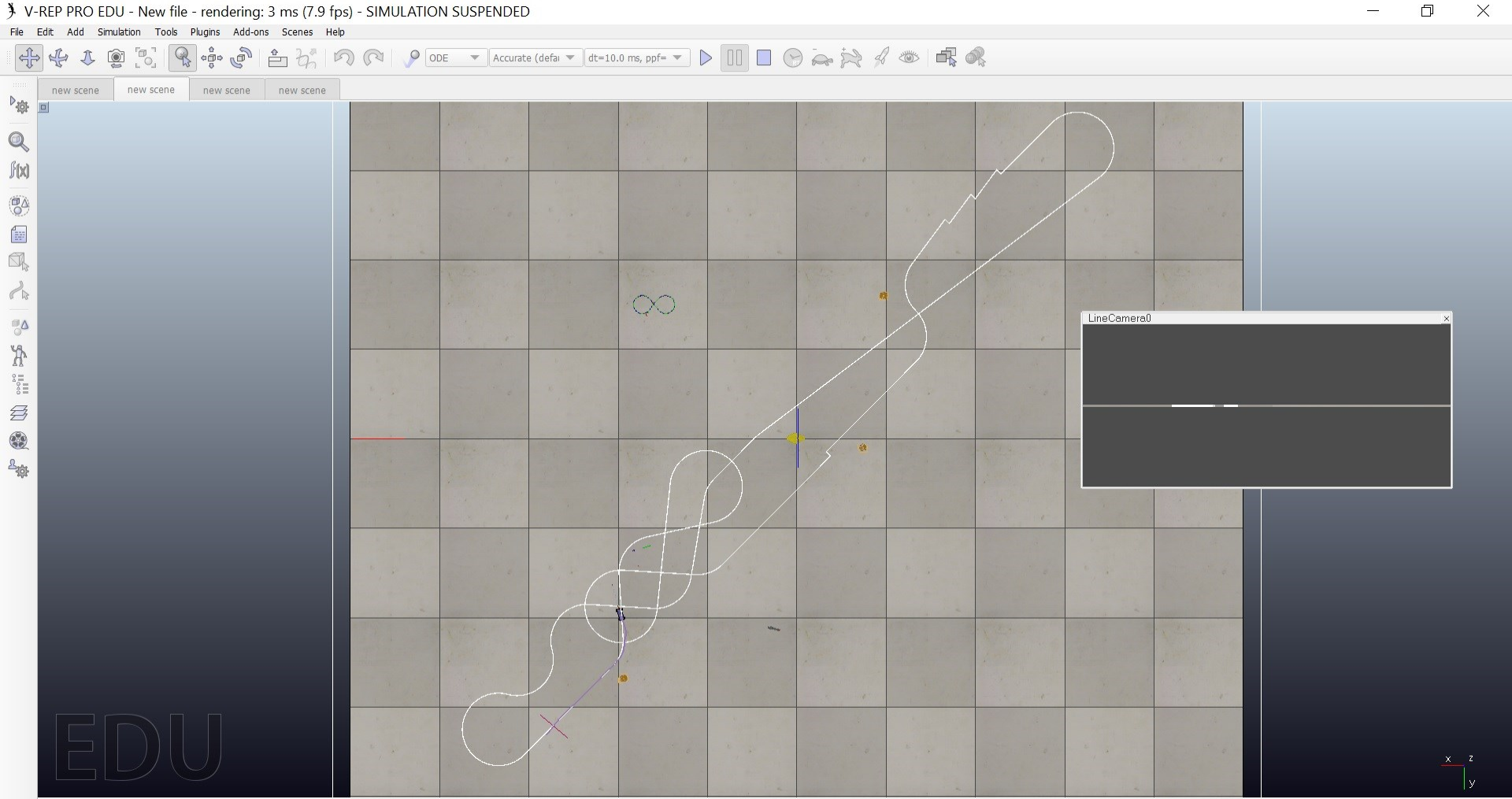


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V-rep simulation- HW2 (due 6 pm Fri 4/2)



demo

Progress Report Due Fri 4/9 (8 pm)

<https://inst.eecs.berkeley.edu/~ee192/sp21/docs/progrpt.pdf>

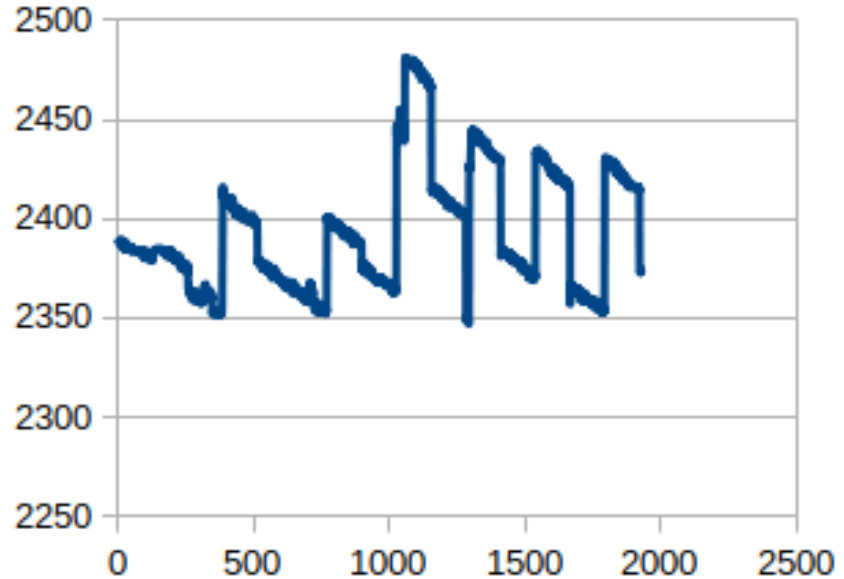
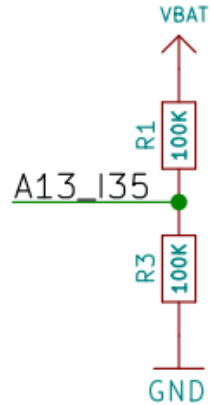
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ESP32 A/D Issues



— Column

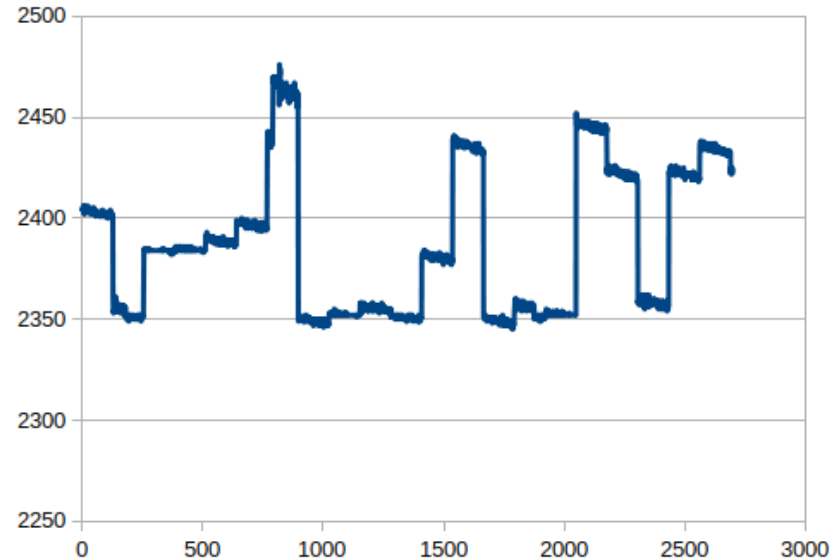
```
static const adc_channel_t channel =  
ADC_CHANNEL_7;
```

```
128 reads are done at 51 us for  
adc1_get_raw()
```

and

```
128 reads are done at 12.2 us for  
local_adc1_read()
```

Then there is a 5 second delay before reading the A/D again. A lot of drift is noticeable.



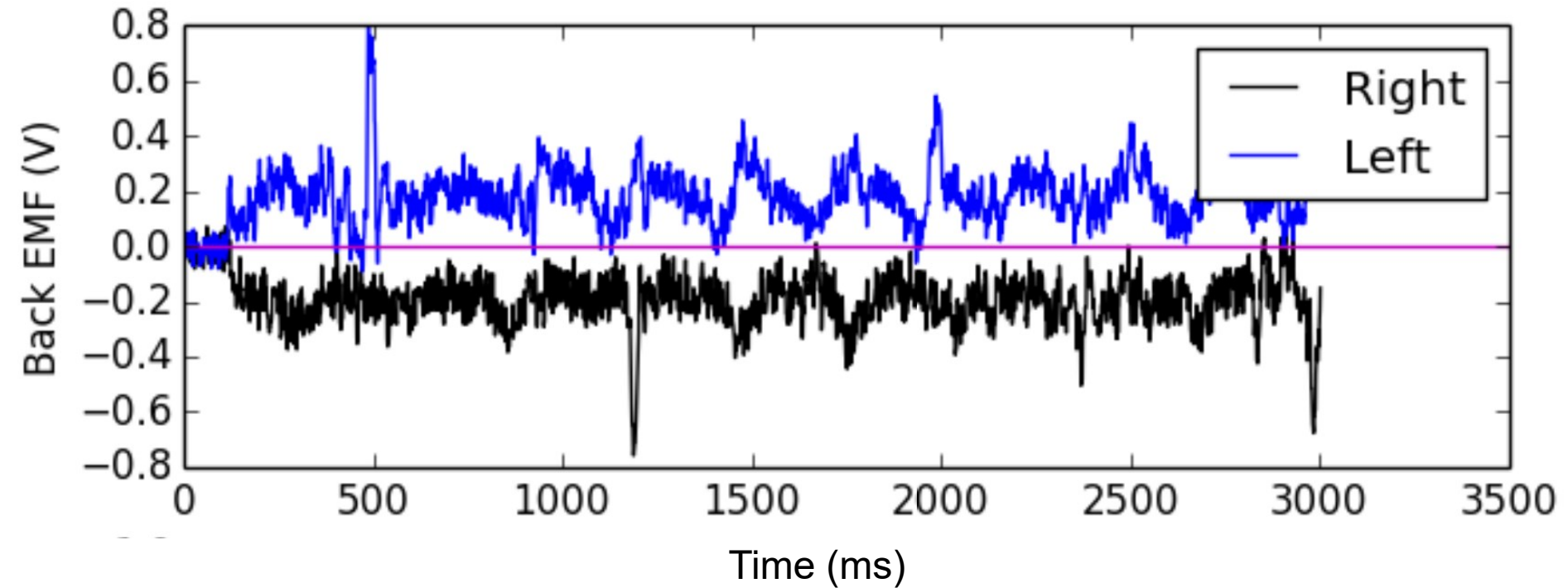
— Column

Digital Filtering

- Moving average
 - $y_1[n] = (y[n-2] + y[n-1] + y[n]) / 3$
- Median filter (outlier rejection)
 - $\text{median}(7, 10, 11, 12, 16, 200, 205) = ?$
- Notch filter (mechanical vibration)
 - $y[n] = (x[n-2] + 2x[n-1] + x[n]) / 4$
- Model based filtering (or Kalman filter)

Moving Average vs. Median Filter

Example: motor brush noise, back EMF measurement




$\{0, 2, -1, 4, 0, 2, 1, 1, 20, 1, 0, 2\} \rightarrow$

$\{0, 2, -1, 2, 0, 1, 1, 1, 1, 1\}$ 3 element median filter

$\{0, 2, 0.3, 1.7, 2, 1, 1.3, 7.3, 7.3, 7, 1, \dots\}$ 3 elem MA

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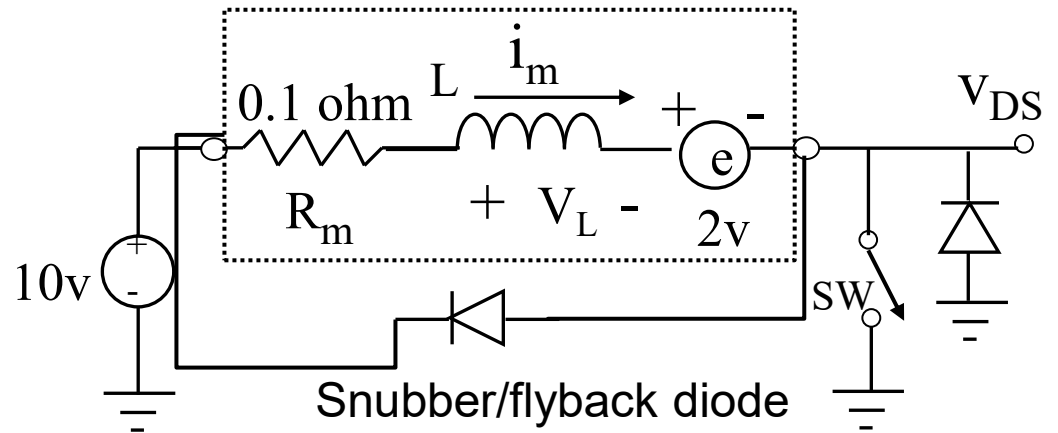
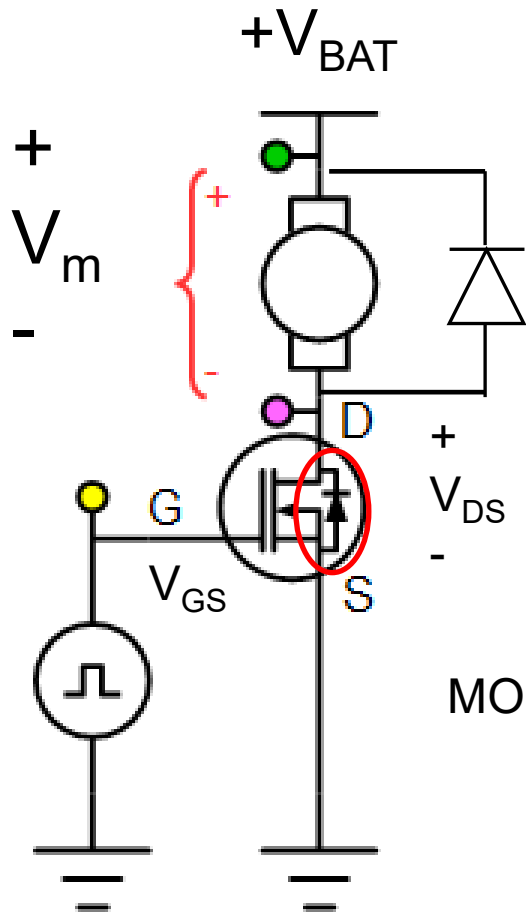
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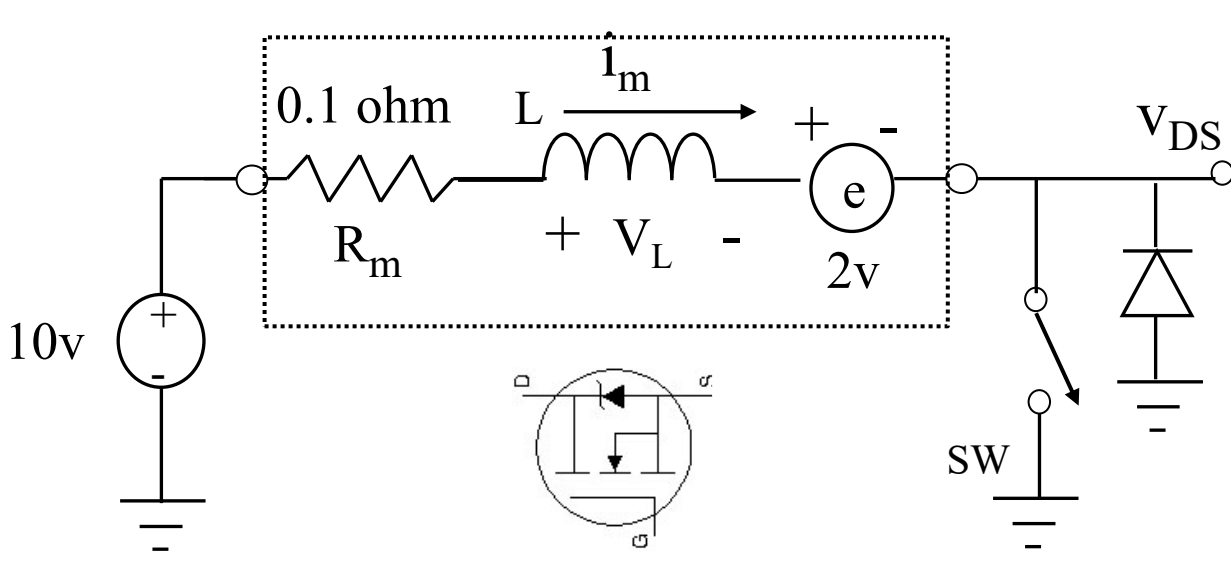
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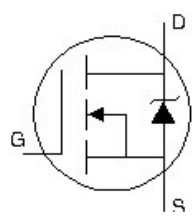
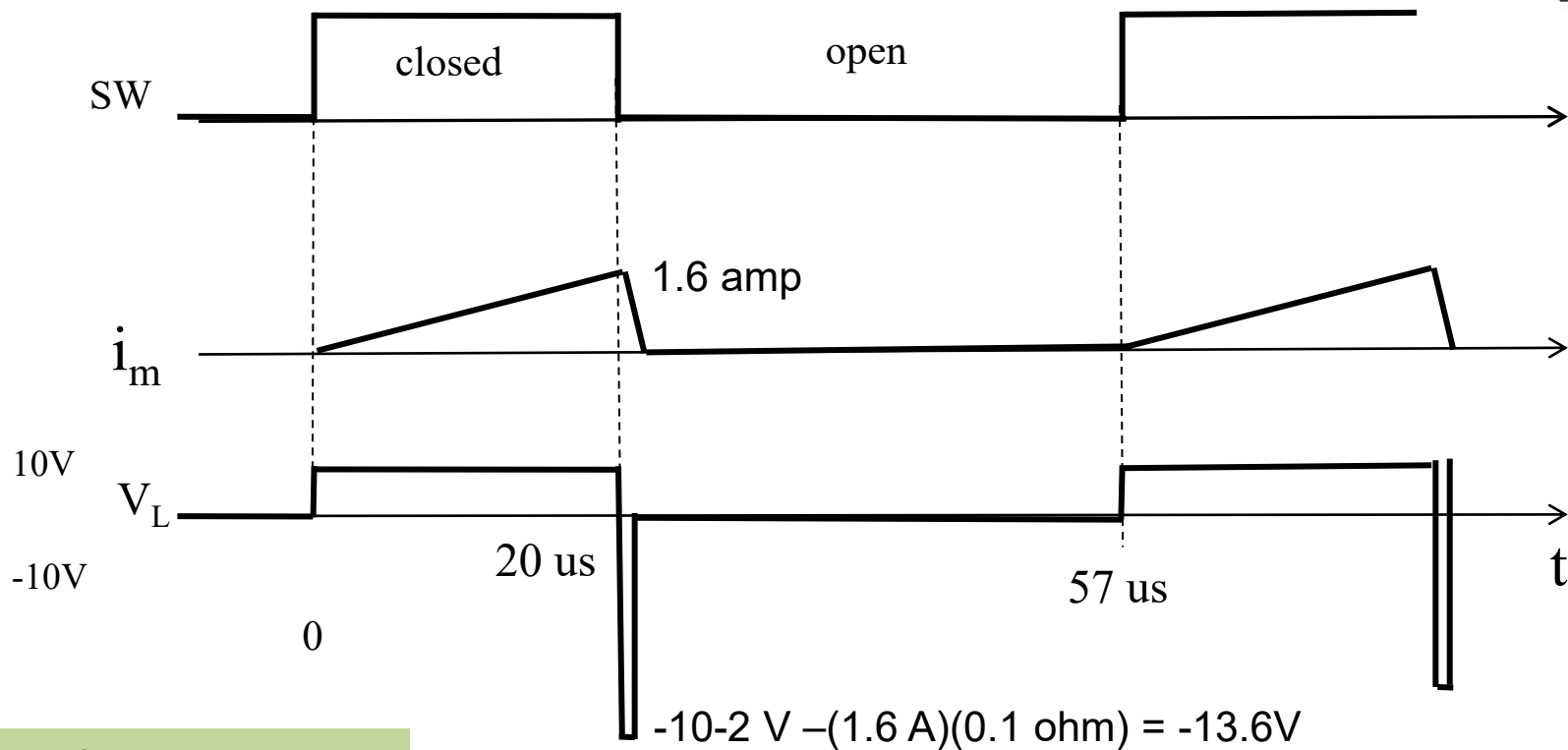
Low side motor drive

What about motor inductance?

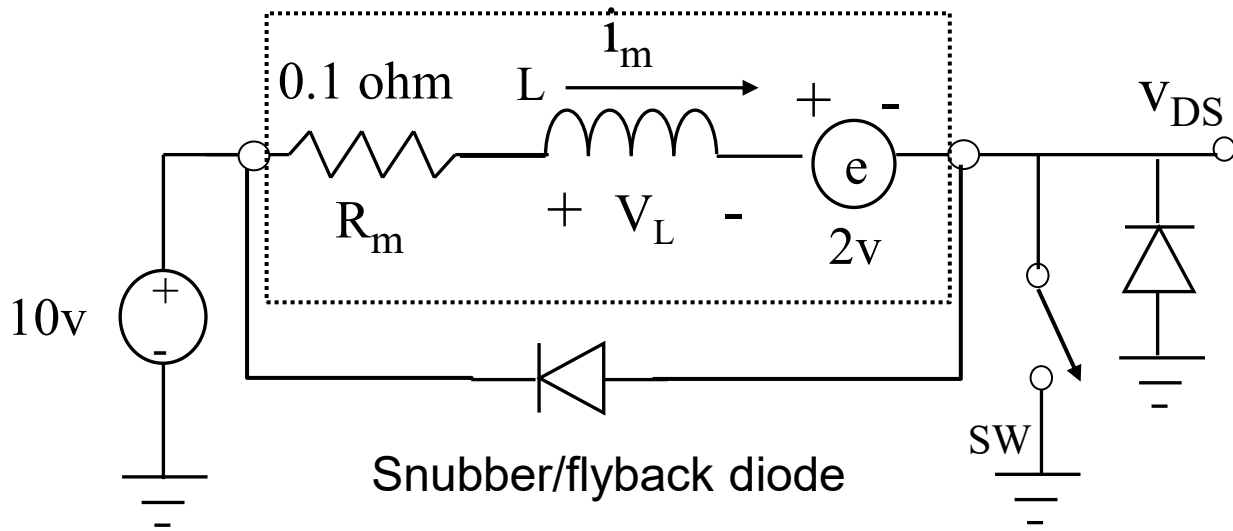




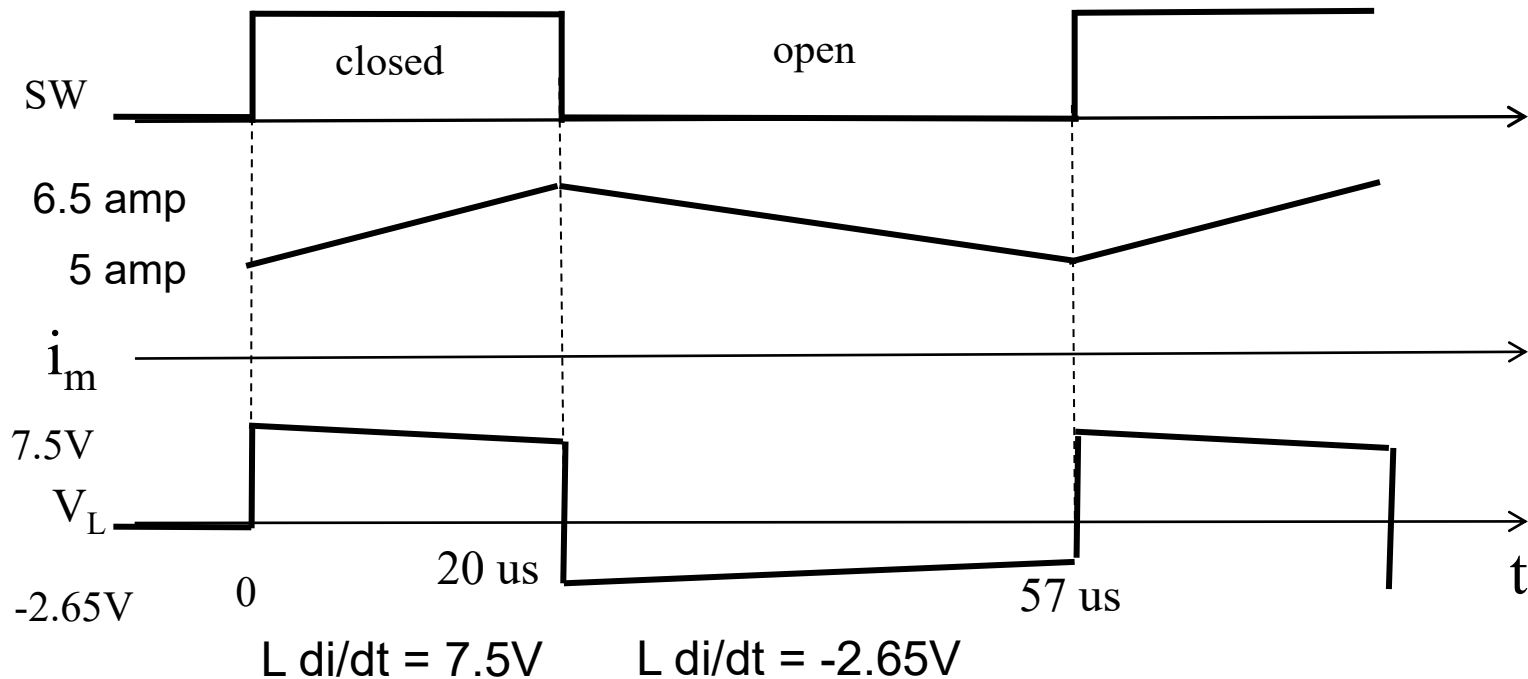
Assume ideal diode,
 17 kHz
 ideal switch, $L = 100 \mu\text{H}$.
 Time constant $\tau = 1 \text{ ms}$.
 Steady state,
 constant velocity.
 Initial rate:
 $V/L = +8 \times 10^4 \text{ amp/sec}$



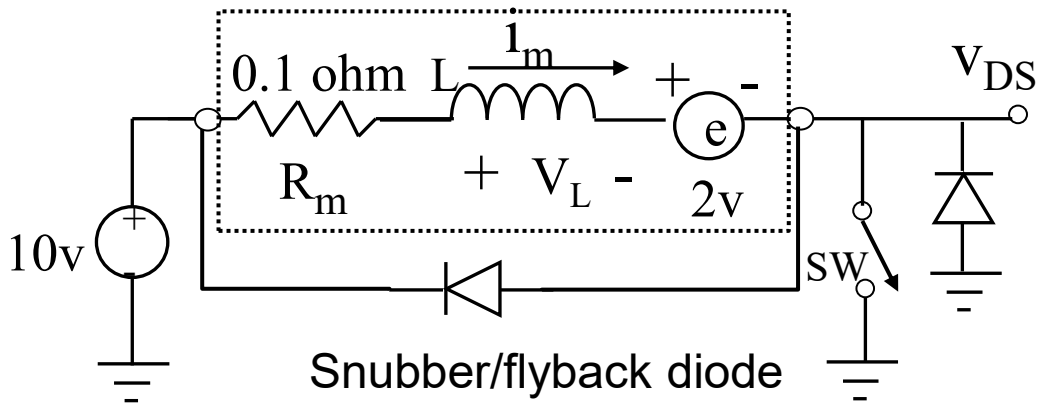
Motor+flywheel diode



Assume ideal diode,
ideal switch, $L = 100 \mu\text{H}$.
Time constant $\tau = 1 \text{ ms}$.
Steady state,
constant velocity.
Assume $i_{\min} = 5 \text{ amp}$



Note: 25 kHz PWM reduces peak current



$$V_{DS} = 10V - V_{DIODE}$$

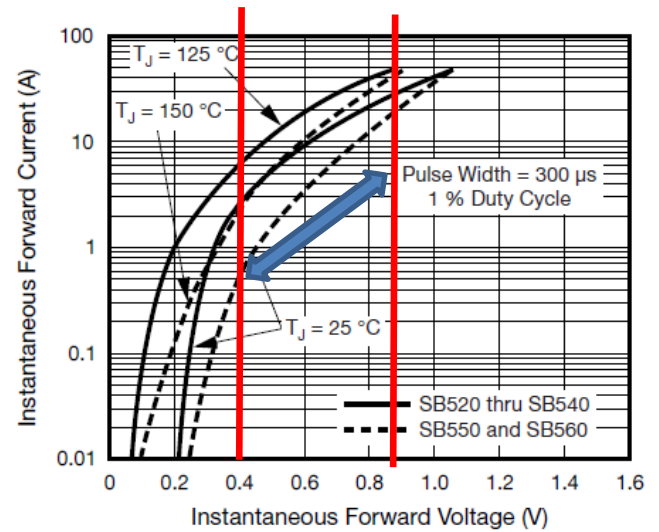
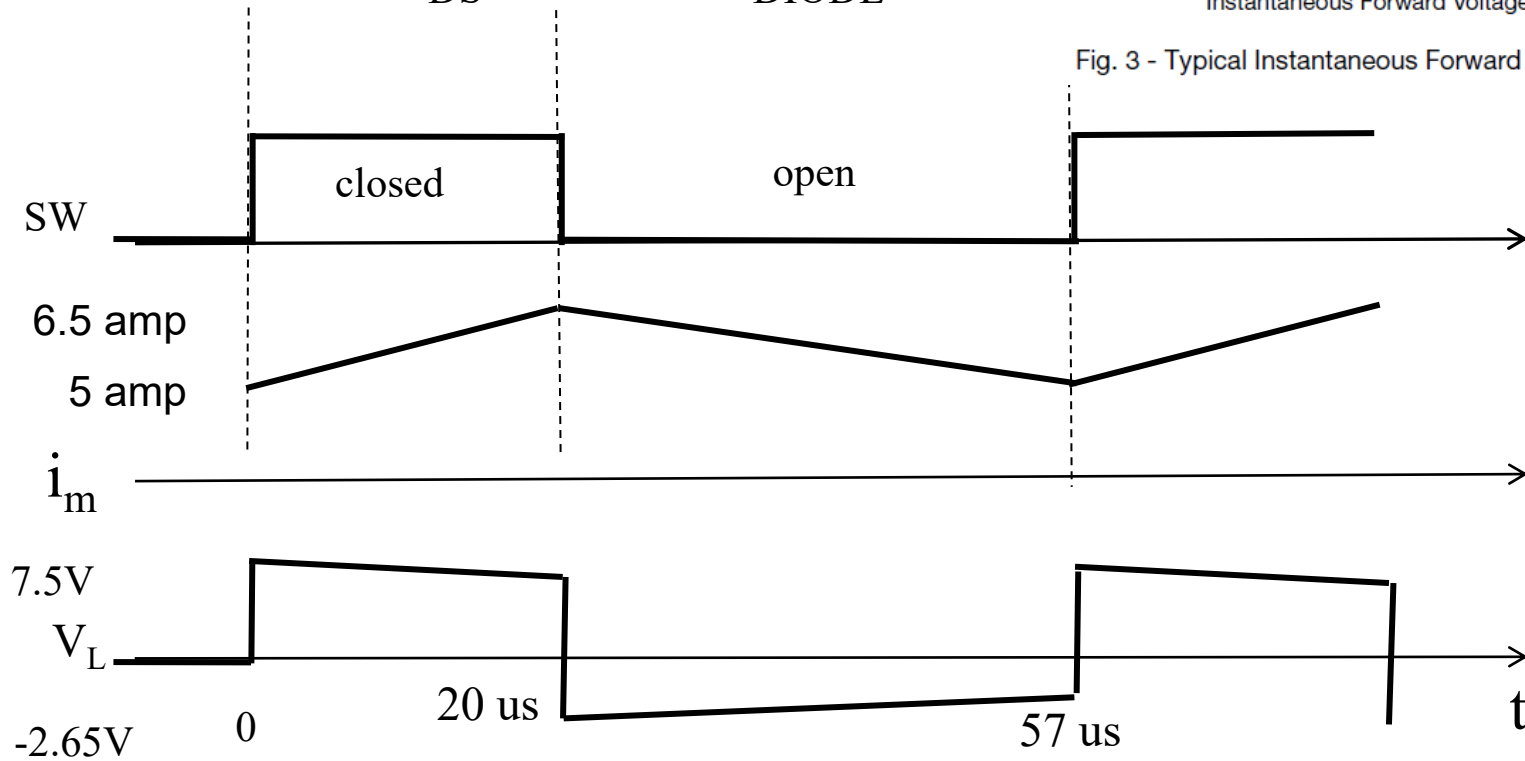


Fig. 3 - Typical Instantaneous Forward Characteristics



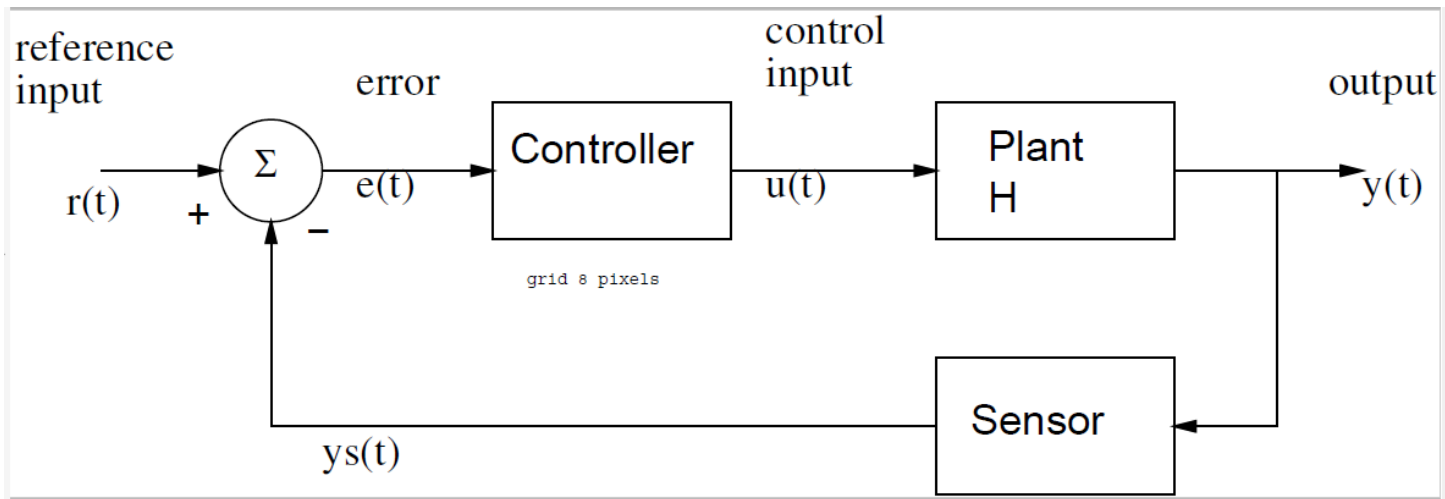
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Control Synopsis



State equations: $\dot{x}(t) = ax(t) + bu(t)$

Output equations: $y(t) = cx(t) + du(t)$

Control Law (P): $u(t) = k_p e(t) = k_p (r(t) - y(t)).$

Control Synopsis

Control Law (P): $u(t) = k_p e(t) = k_p (r(t) - y(t)).$

New state equations:

$$\dot{x} = ax + bk_p e(t) = ax + bk_p (r - x) = (a - bk_p)x + bk_p r.$$

Zero Input Response (non-zero init condx):

$$x(t) = x(0)e^{(a-bk_p)t} \quad \text{for } t \geq 0.$$

$$a' = a - b k_p \quad b' = b k_p$$

Total Response (non-zero init condx) by convolution:

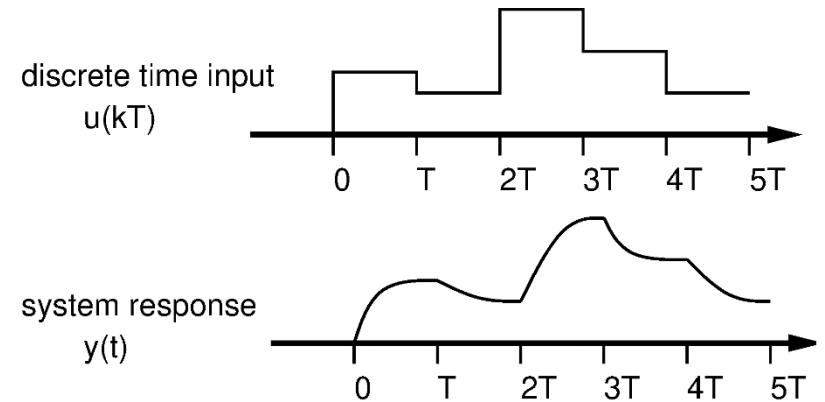
$$x(t_o) = e^{a't_o} x(0) + \int_0^{t_o} e^{a'(t_o-\tau)} b' r(\tau) d\tau . \quad (10)$$

Step Response (zero init condx) by convolution:

$$x(t_o) = b' \int_0^{t_o} e^{a't_o} e^{-a'\tau} d\tau = \frac{-b'e^{a't_o}}{a'} e^{-a'\tau} \Big|_0^{t_o} = \frac{b'}{a'} (1 - e^{-a't_o}) . \quad (11)_{20}$$

Control Synopsis- Discrete Time

Superposition of Step Responses



$$x((k+1)T) = e^{a(k+1)T}x(0) + e^{a(k+1)T} \int_0^{(k+1)T} e^{-a\tau}bu(\tau)d\tau . \quad (15)$$

$$x(kT) = e^{akT}x(0) + e^{akT} \int_0^{kT} e^{-a\tau}bu(\tau)d\tau . \quad (14)$$

$$x((k+1)T) = e^{aT}x(kT) + e^{a(k+1)T} \int_{kT}^{(k+1)T} e^{-a\tau}bu(\tau)d\tau = e^{aT}x(kT) + \int_0^T e^{a\lambda}bu(kT)d\lambda , \quad (16)$$

Control Synopsis- Discrete Time

$$G(T) \equiv e^{aT} \quad \text{and} \quad H(T) \equiv b \int_0^T e^{a\lambda} d\lambda . \quad (17)$$

State equations:

$$x((k + 1)T) = G(T)x(kT) + H(T)u(kT) \quad (18)$$

Output equations:

$$y(kT) = Cx(kT) + Du(kT) . \quad (19)$$

Total Response (non-zero init condx) by convolution:

$$x(k) = G^k x(0) + \sum_{j=0}^{k-1} G^{k-j-1} H u(j) . \quad (23)$$

Control Synopsis- Discrete Time

Control Law (P):

$$U(kT) = k_p [r(kT) - x(kT)]$$

New state equations:

$$x((k + 1)T) = G(T)x(kT) + H(T)k_p(r(kT) - x(kT)) = [G - Hk_p]x(kT) + Hk_pr(kT) . \quad (24)$$

$$x((k + 1)T) = [e^{aT} + \frac{k_p}{a}(1 - e^{aT})]x(kT) + Hk_pr(kT) = G'x(kT) + Hk_pr(kT) . \quad (25)$$

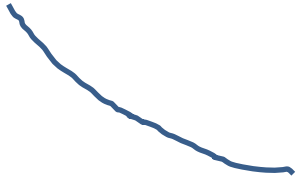
For stability:

$$|e^{aT} - \frac{k_p}{a}(e^{aT} - 1)| < 1. \quad (26)$$

Notes: stability depends on gain **and** T!

Discrete Time Control

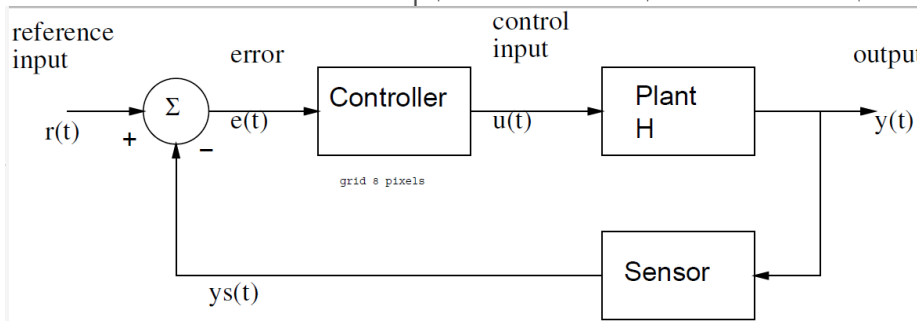
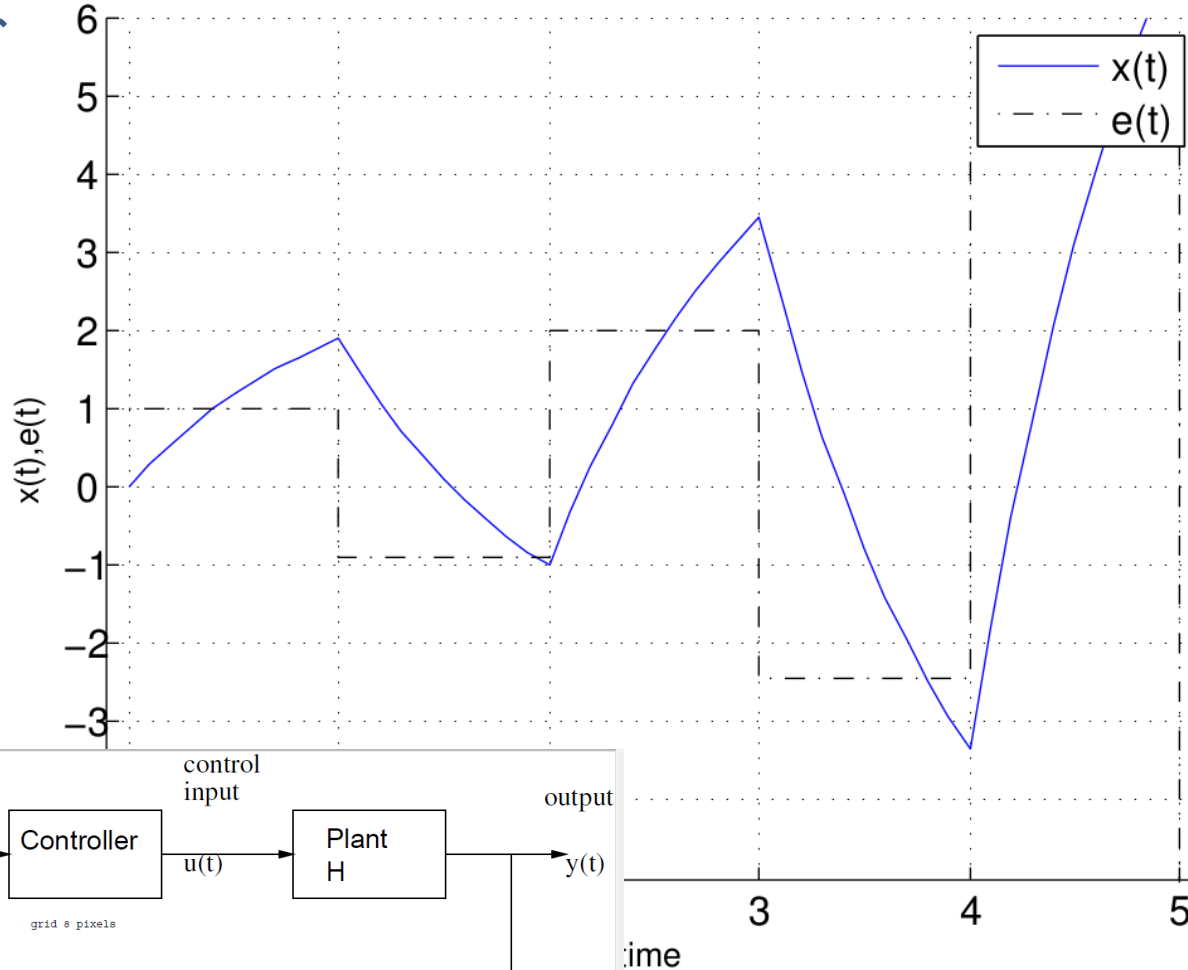
$e(t), u=K_p e(t)$



$$u[k] = K_p(r[k] - x[k])$$

Let $x[k] = y[k]$

Time Series Plot:unnamed



Example control- discrete time

First order CT system $\dot{x} = -x + u$

Let x = car velocity

Reference $r=1$ m/s unit step, $k=3$

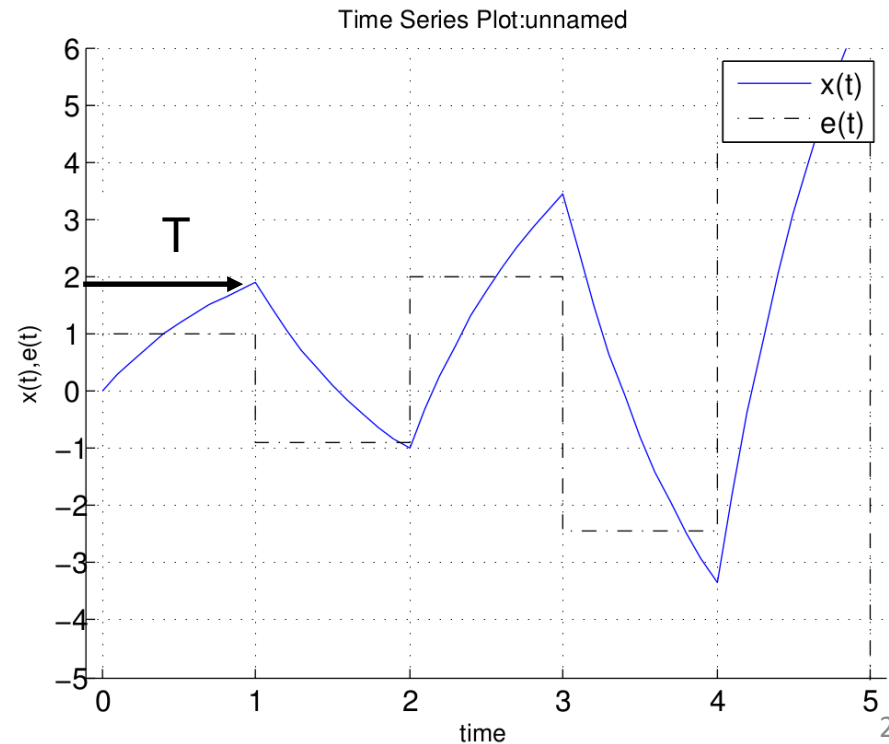
$e(t) = r(t) - x(t)$

Let control input $u[n]=3(r[n]-x[n]) = 3e[n]$,

Watch out for delay!

Watch out for excess gain!

t (sec)	x(t)	e(t) = r(t) - x(t)	u(t)
0^-	0	0	0
0	0	1	3
1	2	-1	-3
2	-1	2	6
3	3.5	-2.5	-7.5
4	-3.5	4.5	13.5



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NATCAR Notes

Cones +2 second

Finish line: The start/finish line will be marked with two 4-inch-long segments of 1-inch-wide white tape that are parallel to the track with 1-inch spacing, as shown in the figure below.

The car must automatically stop within 6 feet of the finish line after finishing the race.

A penalty of 4 seconds will be added to the lap time for any car that does not automatically stop within the required region.

