

PROBLEM SET 4

(Due Thursday, April 10, 2008)

1. Effective mass mayhem:

a) There are 6 “ellipsoidal” conduction band minima in silicon. At each minimum, there is a two-fold symmetric transverse effective mass, m_t^* , and a longitudinal effective mass, m_l^* .

Show that the acceleration, $\frac{\vec{dv}}{dt}$ is always along the direction of the force, \vec{F} , and that the “mobility” mass is given by:

$$\frac{1}{m_\mu^*} = \frac{1}{3} \left(\frac{2}{m_t^*} + \frac{1}{m_l^*} \right)$$

b) Show that the effective mass to use in the density of states expression is:

$$m_N^* = 6^{2/3} [m_l^* (m_t^*)^2]^{1/3}$$

2. The conduction band of germanium consists of $\langle 111 \rangle$ valleys at the extreme of the Brillouin zone, a “direct” $\langle 000 \rangle$ valley 0.15 eV above the conduction band minimum, and six $\langle 100 \rangle$ valleys 0.18 eV above the conduction band minimum. The longitudinal and transverse effective masses are:

$\langle 111 \rangle$	$m_l = 1.58m_0$	$m_t = 0.082m_0$
$\langle 000 \rangle$	$m_l = 0.036m_0$	$m_t = 0.036m_0$
$\langle 100 \rangle$	$m_l = 0.19m_0$	$m_t = 0.97m_0$

The valence band consists of a set of two isotropic bands (“light hole” and “heavy hole”), degenerate at $\mathbf{k} = 0$, with effective masses $m_{lh} = 0.044m_0$, and $m_{hh} = 0.28m_0$. The band gap E_g is 0.66 eV.

a) Calculate n_i to an accuracy of better than 1% at $T = 300\text{K}$, and $T = 900\text{K}$, assuming that the band edges do not shift with temperature.

b) Find the position of E_F at $T = 300\text{K}$, and $T = 900\text{K}$, under the same assumption.

c) For $T = 0\text{K}$, suppose E_F lies at 0.25 eV above the conduction band minimum. Calculate the electron density in each of these conduction band valleys.

Be careful to consider population only within the first Brillouin zone when counting the number of $\langle 111 \rangle$ valleys.

3. For a 3D, non-degenerate electron gas, the average kinetic energy per carrier is $3kT/2$. Derive the corresponding result for a 2D non-degenerate electron gas.
4. Show that for a Maxwell-Boltzmann distribution, the flux directed outward along one of the three coordinate axes is:

$$\frac{J}{(-q)} = n \sqrt{\frac{kT}{2\pi m^*}}$$

5. Literature search. The parameter n_i is very important in device modelling, but is actually not that easy to measure accurately. There has been quite a bit of discussion about the correct value of this quantity for silicon in the relatively recent literature (90s). Values from the mid-1970's are obsolete. Your assignment is to critically review this literature. Describe the various experimental methods for measuring n_i and their strengths and weaknesses. Decide for yourself what value is the best one to use for n_i at 300K in silicon and explain why.