

**PROBLEM SET #5**

Issued: Tuesday, Oct. 18, 2011,

Due (at 7 p.m.): Tuesday, Oct. 25, 2011, in the EE C245 HW box in 240 Cory.

1. This problem concerns the comb-drive structures made in the following two-mask surface micromachining process:

- i) Deposit 2.0  $\mu\text{m}$  of SiGe on a fused quartz (glass) wafer using LPCVD
- ii) Lithographically define and then etch anchor openings in SiGe (anisotropic)
- iii) Deposit 2.0  $\mu\text{m}$  of polysilicon using LPCVD @ 650°C
- iv) Lithographically define and then etch polysilicon structure (anisotropic)
- v) Etch SiGe completely using an  $\text{H}_2\text{O}_2$  etch, releasing structure (isotropic)

(a) Calculate the biaxial strain in the final polysilicon structures due to linear thermal expansion. For all of problem 1 you may assume all materials are isotropic and use the materials properties from *Senturia Table 8.1*, reproduced below.

Material	$\rho_m$ kg/m <sup>3</sup>	$E$ GPa	$\nu$	$\alpha_T$ $\mu\text{strain/K}$	$\sigma_o$ MPa	Comment
Silicon	2331	page 193		2.8		Cubic
$\alpha$ -Quartz	2648	page 573		7.4, 13.6		Hexagonal
Quartz (fused)	2196	72	.16	0.5		Amorphous
Polysilicon	2331	160	$\sim 0.2$	2.8	Varies	Random grains
Silicon dioxide	2200	69	.17	0.7	-300	Thermal
Silicon nitride	3170	270	.27	2.3	+1100	Stoichiometric
	3000	270	.27	2.3	-50 – +800	Silicon rich
Aluminum	2697	70	$\sim .3$	23.1	varies	Polycrystalline

(b) For the comb-drive resonator structure in Figure 1.1 where  $L_1 = 100 \mu\text{m}$  and  $W = 2 \mu\text{m}$ , calculate the stress on the flexure beams  $L_1$ . Is it compressive or tensile? If the stress is compressive, at what polysilicon deposition temperature would beam buckling occur? Assume the comb-drive shuttle is perfectly rigid.

(c) For the comb-drive resonator structure in Figure 1.2 where  $L_1 = 100 \mu\text{m}$ ,  $L_2 = 90 \mu\text{m}$ , and  $W = 2 \mu\text{m}$ , calculate the stress on the flexure beams  $L_1$  and  $L_2$ . For each case, indicate whether the stress is compressive or tensile. Assume the comb-drive shuttle and trusses are perfectly rigid.

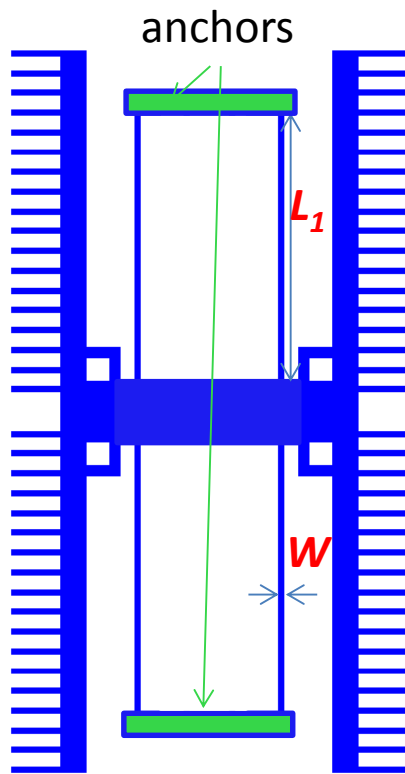


Figure 1.1

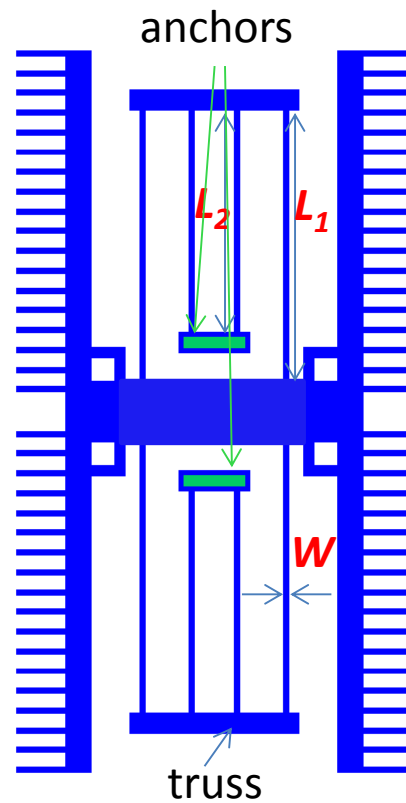


Figure 1.2

(d) Satisfied with the performance of the resonator used for part c, you decide to couple two resonators to make a simple filter as shown in Figure 1.3. For  $L_c = 80 \mu\text{m}$  and  $W_c = 2 \mu\text{m}$ , calculate the stress in the coupling beam. Use the same resonators and assumptions as in part (c).

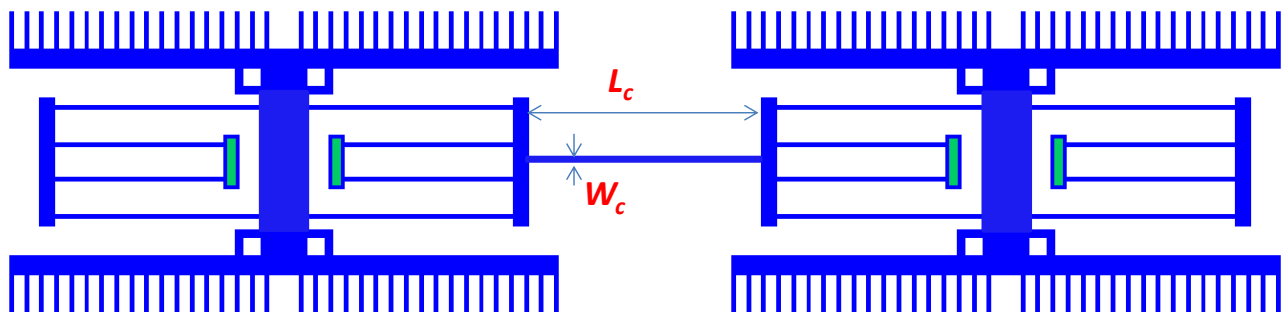
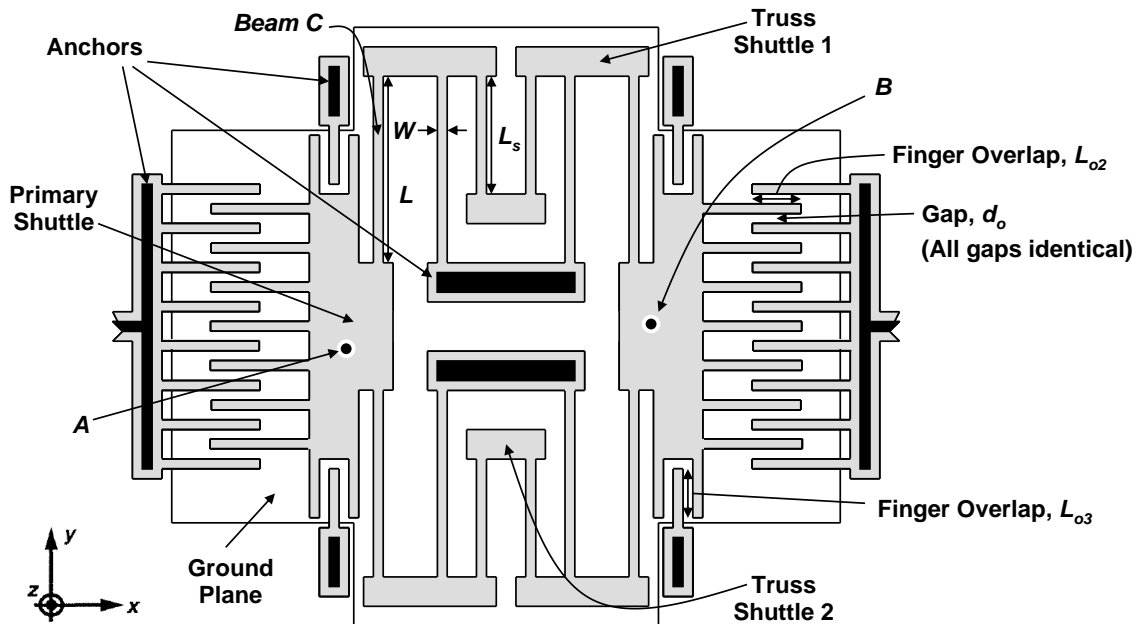


Figure 1.3

2. The figure below presents the top view of a micromechanical device constructed in a  $2\mu\text{m}$ -thick structural layer with numerous ports. Here, everything is suspended  $2\mu\text{m}$  above the substrate except for the anchoring locations indicated as the darkly shaded regions. Data on the structural material used in this problem and on specific geometric dimensions are given in the box below the figure. Also, assume that all folding trusses and shuttles are rigid in all directions, including the vertical (i.e.,  $z$ ) direction. In addition, all suspension beam widths are  $2\mu\text{m}$ .



Structural Material Properties:

Young's Modulus,  $E = 150\text{ GPa}$ ; Density,  $\rho = 2,300\text{ kg/m}^3$

Poisson ratio,  $\nu = 0.226$

Geometric Dimensions: (all beams are width  $W$ )

$L = 50\mu\text{m}$ ;  $W = 2\mu\text{m}$ ;  $L_s = 25\mu\text{m}$ ; Thickness,  $h = 2\mu\text{m}$ ; All Finger Gaps,  $d_o = 1\mu\text{m}$

All Finger Overlaps,  $L_o = 10\mu\text{m}$ , Truss Shuttle 1 Area =  $300\mu\text{m}^2$

Truss Shuttle 2 Area =  $100\mu\text{m}^2$ , Primary Shuttle Area =  $4,000\mu\text{m}^2$

- (a) Write an expression for the stiffness of beam C.
- (b) Write an expression for the stiffness at point A (assuming no voltages are applied).
- (c) If point A moves  $x_A = 1\mu\text{m}$  in the  $x$ -direction due to a force applied at A, how much does point B move? Provide an expression for  $x_B$  in terms of  $x_A$  and spring constants, and calculate a numerical value.
- (d) Suppose the HF/DI water release etch for this structure was insufficient to release the primary shuttle masses, but long enough to release everything else. Will the remaining released portions of this structure be stuck to the substrate after release and drying? Assume the contact angle of water between the underside of the structure and the substrate is  $30^\circ$ , and the room-temperature surface tension of a water-air interface is  $72.75 \times 10^{-3}\text{ N/m}$ .