EE247 Lecture 7

- Automatic on-chip filter tuning (continued from last lecture)
 - Continuous tuning (continued)
 - Replica single integrator in a feedback loop locked to a reference frequency
 - · DC tuning of resistive timing element
 - Periodic digitally assisted filter tuning
 - Systems where filter is followed by ADC & DSP, existing hardware can be used to periodically update filter freq. response
- Continuous-time filter design considerations
 - Monolithic highpass filters
 - Active bandpass filter design
 - · Lowpass to bandpass transformation
 - Example: 6th order bandpass filter

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Lecture 7: Filters

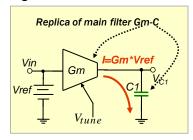
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Summary last lecture

- Continuous-time filters (continued)
 - -Opamp MOSFET-C filters
 - -Opamp MOSFET-RC filters
 - -Gm-C filters
- Frequency tuning for continuous-time filters
 - -Trimming via fuses or laser
 - -Automatic on-chip filter tuning
 - Continuous tuning
 - -Master-slave tuning (to be continued)

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Master-Slave Frequency Tuning 3-Reference Integrator Locked to Reference Frequency



- Replica of main filter integrator e.g. Gm-C building block used
- Utilizes the fact that a DC voltage source connected to the input of the Gm cell generates a constant current at the output proportional to the transconductance and the voltage reference

$$I = Gm.Vref$$

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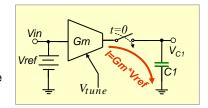
Lecture 6: Filters

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Reference Integrator Locked to Reference Frequency

•Consider the following sequence:

- Integrating capacitor is fully discharged @ t =0
- At t=0 the capacitor is connected to the output of the Gm cell then:



$$VCI$$
 T $VCI = Gm \times V_{ref} \times T / CI$
 $t=0$ time

$$\begin{aligned} &Q_{C1} \!=\! V_{C1} \!\times\! C1 \!=\! Gm \!\times\! V_{ref} \!\times\! T \\ &\rightarrow\! V_{C1} \!=\! Gm \!\times\! V_{ref} \!\times\! T \left/\!\!\!\! C1 \right. \end{aligned}$$

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Reference Integrator Locked to Reference Frequency

Since at the end of the period T:

$$V_{C1} \approx Gm \times V_{ref} \times T /_{C1}$$

If V_{CI} is forced to be equal to V_{ref} then:

$$Vref = V_{tune}$$

$$V_{tune}$$

$$V_{CI} \approx Gm \times V_{ref} \times T / CI$$

time

$$\frac{C1}{Gm} = T = \frac{N}{f_{c1k}}$$

How do we manage to force $V_{CI} = V_{ref}$?

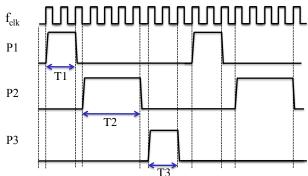
→ Use feedback!!

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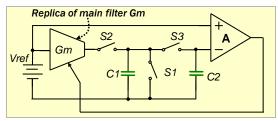
Reference Integrator Locked to Reference Frequency Clocking Scheme



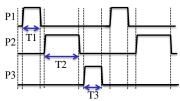
- Three clock phase operation
- Non-overlapping signals P1, P2, P3 derived from a master clock (f_{clk})
- Note: $T2=4/f_{clk}$ and therefore accurate

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Reference Integrator Locked to Reference Frequency



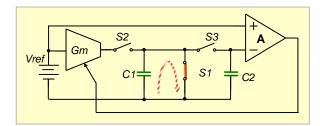
- Three clock phase operation
- To analyze → study one phase at a time

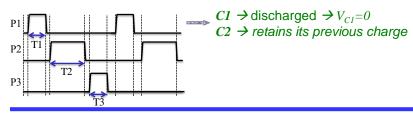


Ref: A. Durham, J. Hughes, and W. Redman-White, "Circuit Architectures for High Linearity Monolithic Continuous-Time Filtering," *IEEE Transactions on Circuits and Systems*, pp. 651-657, Sept. 1992.

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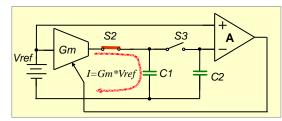
Reference Integrator Locked to Reference Frequency P1 high→ S1 closed



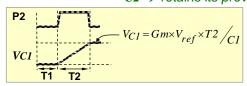


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Reference Integrator Locked to Reference Frequency P2 high → S2 closed



C1 \rightarrow charged with constant current: I=Gm*VrefC2 \rightarrow retains its previous charge

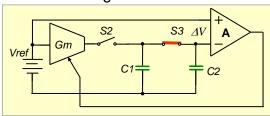


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Reference Integrator Locked to Reference Frequency P3 high → S3 closed



C1 charge shares with C2

$$V_{C1}^{T2}C1 + V_{C2}^{T2}C2 = (C1 + C2)V_{C1,2}^{T3}$$

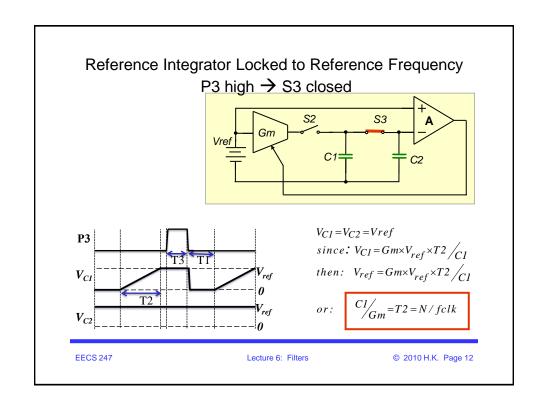
$$V_{C1,2}^{T3} = V_{C1}^{T2}\frac{C1}{C1 + C2} + V_{C2}^{T2}\frac{C2}{C1 + C2}$$

Few cycles following startup system approaches steady state:

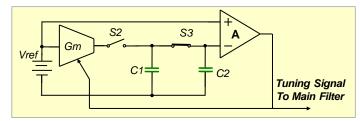
$$V_{C1,2}^{T3} = V_{C1}^{T2} = V_{C2}^{T2}$$

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Reference Integrator Locked to Reference Frequency P3 high → S3 closed Gm C1 C1 charge shares with C2 **P3** Few cycles following startup Assuming A is large, feedback V_{CI} forces: $\Delta V \rightarrow 0$ $\rightarrow V_{C2} = V_{ref}$ V_{C2} **EECS 247** Lecture 6: Filters © 2010 H.K. Page 11



Summary Replica Integrator Locked to Reference Frequency



Feedback forces Gm to assume a value so that:

- Integrator time constant locked to an accurate frequency
- Tuning signal used to adjust the time constant of the main filter integrators

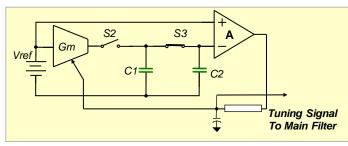
$$\tau_{intg} = \frac{CI}{Gm} = N/fclk$$
or
$$\omega_0^{intg} = \frac{Gm}{CI} = fclk/N$$

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Issues 1- Loop Stability



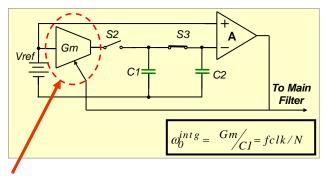
- · Note: Need to pay attention to loop stability
 - √ C1 chosen to be smaller than C2 tradeoff between stability and speed of lock acquisition
 - ✓ Lowpass filter at the output of amplifier (A) helps stabilize the loop

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Issues 2- GM-Cell DC Offset Induced Error

Problems to be aware of:



→ Tuning error due to master integrator DC offset

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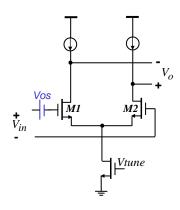
Issues Gm Cell DC Offset

What is DC offset?

Simple example:

For the differential pair shown here, mismatch in input device or load characteristics would cause DC offset: $\rightarrow Vo = 0$ requires a non-zero input voltage

Offset could be modeled as a small DC voltage source at the input for which with shorted inputs $\rightarrow V_0 = 0$



Example: Differential Pair

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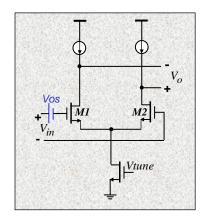
Simple Gm-Cell DC Offset

Mismatch associated with the diff. pair: M1 & M2

→ DC offset

$$V_{os} = (V_{thI} - V_{th2}) - \frac{1}{2}V_{ovI,2} \frac{\Delta(W/L)_{MI,2}}{(W/L)_{MI,2}}$$

Assuming offset due to load device mismatch is negligible



Ref: Gray, Hurst, Lewis, Meyer, Analysis & Design of Analog Integrated Circuits, Wiley 2001, page 335

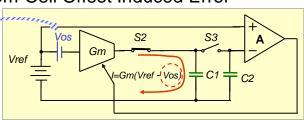
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Gm-Cell Offset Induced Error

Voltage source representing DC offset



•Effect of Gm-cell DC offset:

$$V_{CI} = V_{C2} = V_{ref}$$

$$Ideal: V_{CI} = Gm \times V_{ref} \times T2 / C1$$

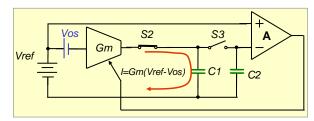
$$with offset: V_{CI} = Gm \times \left(V_{ref} - V_{os}\right) \times T2 / C1$$

$$or: CI / Gm = T2 \left(1 - \frac{V_{os}}{V_{ref}}\right)$$

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Gm-Cell Offset Induced Error



• Example:

$$\frac{Cl}{Gm} = T2 \left(1 - \frac{V_{os}}{V_{ref}} \right) \quad f_{critical} \propto \frac{Gm}{Cl}$$

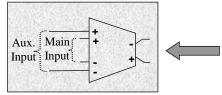
$$for \ \frac{V_{os}}{V_{ref}} = 1/10$$

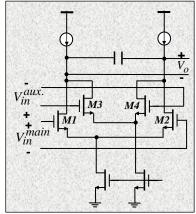
10% error in tuning!

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Gm-Cell Offset Induced Error Solution Example

- Assume differential integrator
- Add a pair of auxiliary inputs to the input stage of the <u>master</u> Gm-cell for offset cancellation purposes

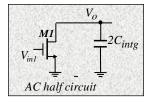


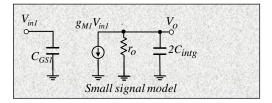


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Simple Gm-Cell AC Small Signal Model





$$V_o = \left(g_m^{M\,I} V_{inI}\right) \left(r_o \ || \ \frac{1}{s} \times 2C_{int\,g} \ \right) \ \ r_o \ \ is \ parallel \ combination \ of \ r_o \ of \ M1 \ \& \ load$$

$$V_o = \frac{-g_m^M I_{r_o}}{I + s \times 2C_{int} \, g_r^o} V_{in1} \qquad \& \ g_m^{MI} r_o = aI \rightarrow Integrator \, finite \ DC \, gain$$

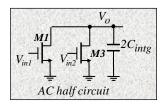
$$V_{o} = \frac{-a1}{1 + \frac{a1 \times s \times 2C_{intg}}{s}} V_{in1} \qquad Note: a1 \to \infty, \qquad V_{o} = \frac{-g_{m}^{M1}}{s \times 2C_{intg}} V_{in1}$$

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Simple Gm-Cell + Auxiliary Inputs AC Small Signal Model



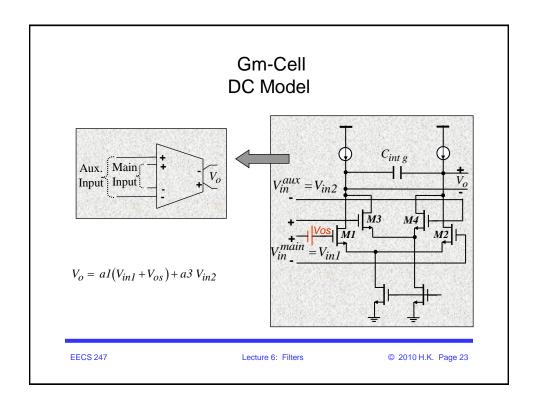
$$V_{o} = \left(g_{m}^{MI}V_{in1} + g_{m}^{M3}V_{in2}\right)\left(r_{o} \mid\mid \frac{1}{s} \times 2C_{int g}\right) \quad r_{o} \text{ parallel combination of } r_{o} \text{ of } M1, M3, \& \text{ current source}$$

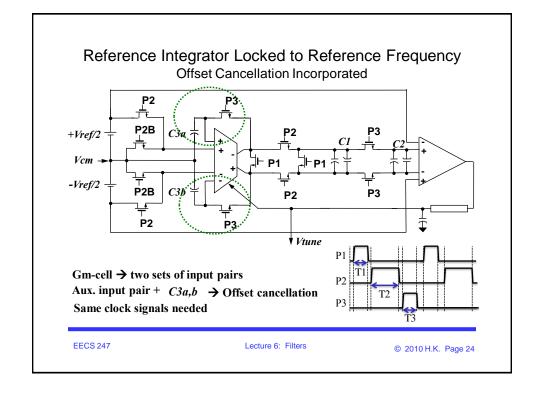
$$V_{o} = \frac{-g_{m}^{MI}r_{o}}{1 + s \times 2C_{int g}r_{o}} V_{in1} - \frac{g_{m}^{M3}r_{o}}{1 + s \times 2C_{int g}r_{o}} V_{in2}$$

$$V_{o} = -\frac{a1}{1 + \frac{a1 \times s \times 2C_{int} g}{1 + \frac{a3 \times s \times 2C_{int} g}{g_{m}^{M 3}}}} V_{in1} - \frac{a3}{1 + \frac{a3 \times s \times 2C_{int} g}{g_{m}^{M 3}}} V_{in2}$$

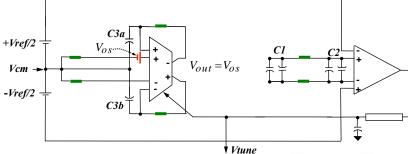
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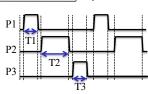


Reference Integrator Locked to Reference Frequency P3 High (Update & Store offset)



 $\operatorname{Gm-cell} \Rightarrow \operatorname{Unity}$ gain configuration via aux. inputs Main inputs shorted

C1, C2 \rightarrow Charge sharing



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Reference Integrator During Offset Cancellation Phase

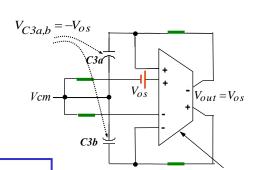
$$V_o = a1 \left(V_{in1} + V_{os} \right) + a3 V_{in2}$$

$$V_{in2} = -V_o$$

$$V_o = a1 \times V_{os} - a3 \times V_o$$

$$\to V_o = \frac{a1}{1+a3} \times V_{os}$$

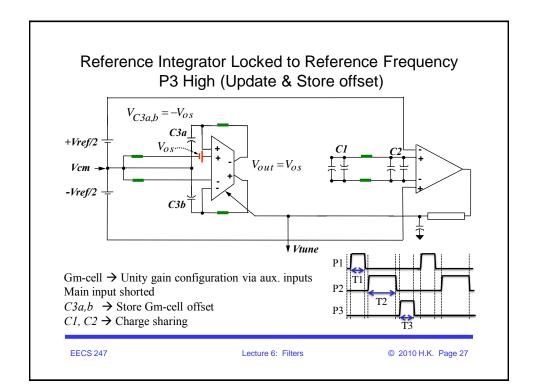
Assuming $a1 = a3 \gg 1$

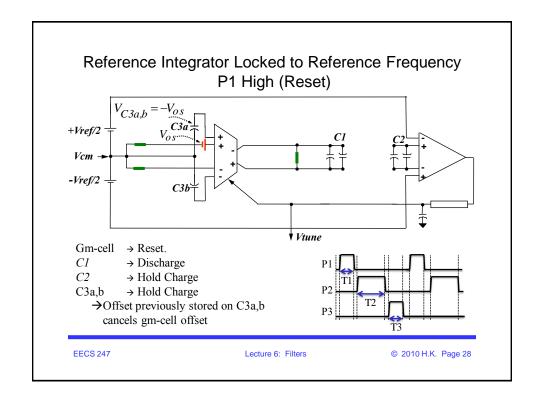


$$V_O = V_{OS}$$
 &

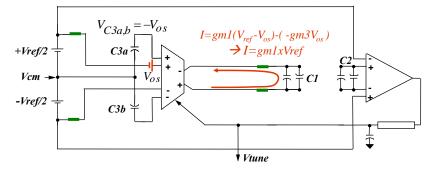
& $V_{in2} = -V_{os}$

 $C3a,b \rightarrow Store main Gm-cell offset$





Reference Integrator Locked to Reference Frequency P2 High (Charge)



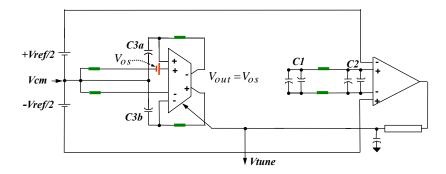
Gm-cell → Charging C1

 $C3a,b \rightarrow \text{Store/hold Gm-cell offset}$

 $C2 \rightarrow Hold charge$

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Summary Reference Integrator Locked to Reference Frequency



Key point: Tuning error due to Gm-cell offset cancelled

*Note: Same offset compensation technique can be used in many other applications

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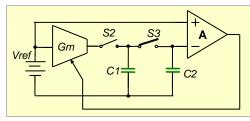
Summary Reference Integrator Locked to Reference Frequency

Tuning error due to gm-cell offset voltage resolved

Advantage over previous schemes:

 $\rightarrow f_{clk}$ can be chosen to be at much higher frequencies compared to filter bandwidth (N>I)

→ Feedthru of clock falls out of band and thus attenuated by filter however, beware of feedthru of the three phase clock signals



Feedback forces Gm to vary so that:

$$\tau_{intg} = \frac{Cl}{Gm} = N/fclk$$
or
$$\omega_0^{intg} = \frac{Gm}{Cl} = fclk/N$$

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DC Tuning of Resistive Timing Element

Tuning circuit Gm → replica of Gm used in filter

Rext used to lock Gm to accurate off-chip R

Feedback forces: *IxRext* @ Gm-cell input Current flowing in Gm-Cell → *I Gm=1/Rext*

Issues with DC offset

Account for capacitor variations in this Gm-C implementation by trimming C in the factory

Vrune

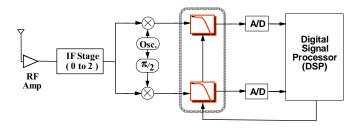
| Gm | Gm | Final Property | Fina

Ref: C. Laber and P.R. Gray, "A 20MHz 6th Order BiCMOS Parasitic Insensitive Continuous-time Filter and Second Order Equalizer Optimized for Disk Drive Read Channels," *IEEE Journal of Solid State Circuits*, Vol. 28, pp. 462-470, April 1993

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Digitally Assisted Frequency Tuning Example: Wireless Receiver Baseband Filters



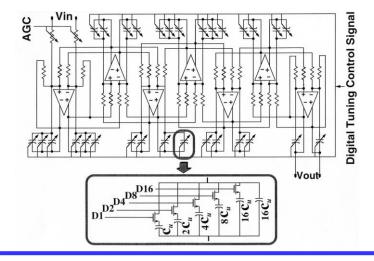
- · Systems where filter is followed by ADC & DSP
 - Take advantage of existing digital signal processor capabilities to periodically test & if needed update the filter critical frequency
 - Filter tuned only at the outset of each data transmission session (off-line/periodic tuning) can be fine tuned during times data is not transmitted or received

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Example: Seventh Order Tunable Low-Pass OpAmp-RC Filter



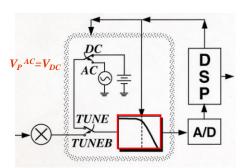
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Digitally Assisted Filter Tuning Concept

Assumptions:

- System allows a period of time for the filter to undergo tuning (e.g. for a wireless transceiver during idle periods)
- An AC (e.g. a sinusoid) signal can be generated on-chip whose amplitude is a function of an on-chip DC voltage
 - AC signal generator outputs a sinusoid with peak voltage equal to the DC signal source
 - AC Signal Power =1/2 DC signal power @ the input of the filter

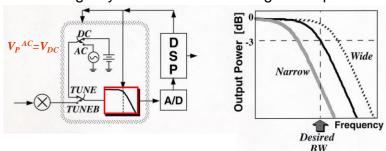


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Digitally Assisted Filter Tuning Concept



AC signal @ a frequency on the roll-off of the desired filter frequency response (e.g. -3dB frequency) $V_{AC} = V_{DC} \times sin \left(2\pi f \frac{desired}{-3dB} t \right)$

Provision can be made \rightarrow during the tuning cycle, the input of the filter is disconnected from the previous stage (e.g. mixer) and connected to:

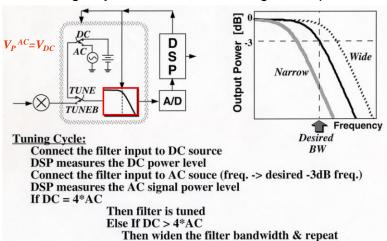
- 1. DC source
- 2. AC source

under the control of the DSP

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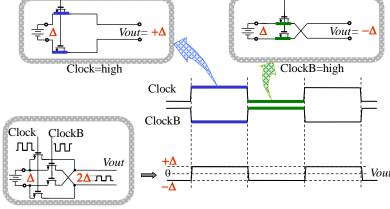
Digitally Assisted Filter Tuning Concept



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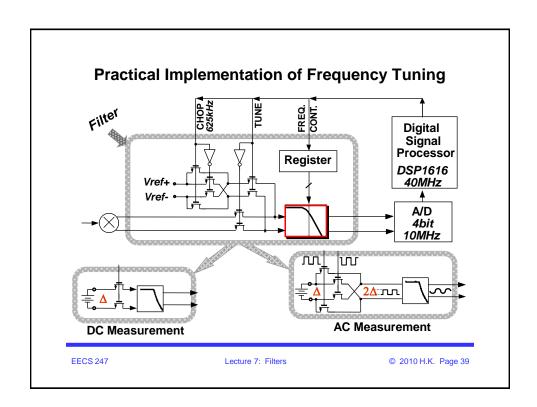
Else narrow the filter bandwidth & repeat

Practical Implementation of Frequency Tuning AC Signal Generation From DC Source

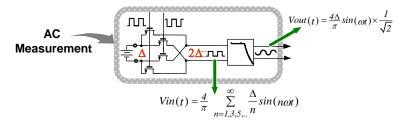


Square waveform generated $\rightarrow 2\Delta$ peak to peak magnitude and @ frequency= f_{clock}

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Practical Implementation of Frequency Tuning Effect of Using a Square Waveform

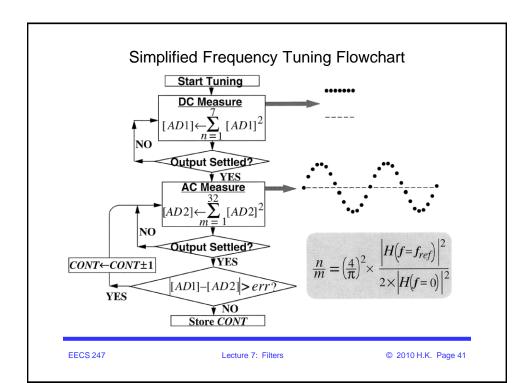


- Input signal chosen to be a square wave due to ease of generation
- Filter input signal comprises a sinusoidal waveform @ the fundamental frequency + its odd harmonics:

Key Point: The filter itself attenuates unwanted odd harmonics → Inaccuracy incurred by the harmonics negligible

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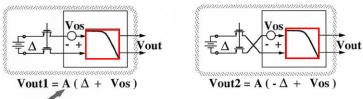
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Digitally Assisted Offset Compensation

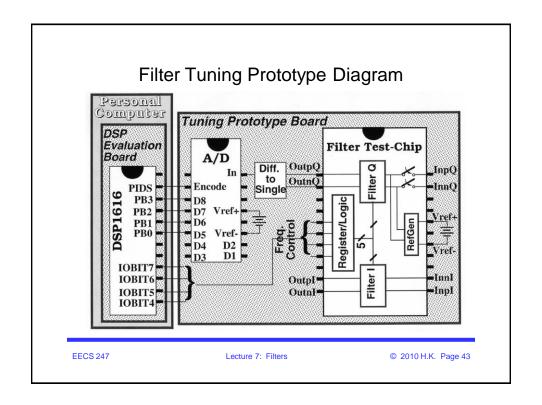
In cases where the filter DC offset cause significant error in tuning (i.e. high passband gain)

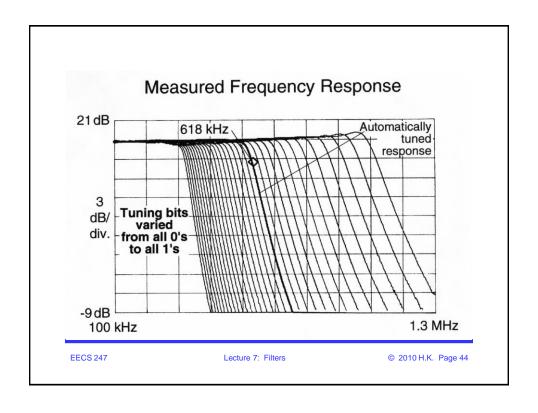
- Offset compensation needed:
- DC measurement performed in two steps:



Passband Gain

- ArrDSP extracts: Offset component → 1/2(Vout1 + Vout2) = A . Vos
 DC component → 1/2(Vout1 Vout2) = A . Δ
- CDSP substracts Vos from all subsequent AC measurement





Measured Tuning Characteristics

Tunable frequency range (nom. process) Variations due to process		370kHz to 1.1M ±50%
I/Q bandwidth imbalance		0.1%
Tuning resolution (620kHz frequency range)	Measured Expected	3.8% 2-5%
Tuning time	Coarse+Fine Fine only	max. 800μsec min. 50μsec
Memory space required for tuning routine		250 byte

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Off-line Digitally Assisted Tuning

- Advantages:
 - No reference signal feedthrough since tuning does not take place during data transmission (off-line)
 - Minimal additional hardware
 - Small amount of programming
- Disadvantages:
 - If acute temperature change during data transmission, filter may slip out of tune!
 - Can add fine tuning cycles during periods when data is not transmitted or received

Ref: H. Khorramabadi, M. Tarsia and N.Woo, "Baseband Filters for IS-95 CDMA Receiver Applications Featuring Digital Automatic Frequency Tuning," 1996 International Solid State Circuits Conference, pp. 172-173.

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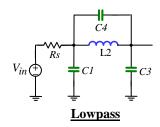
Summary: Continuous-Time Filter Frequency Tuning

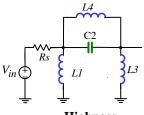
- Trimming
 - □ Expensive & does not account for temperature and supply etc... variations
- · Automatic frequency tuning
 - Continuous tuning
 - □ Master VCF used in tuning loop, same tuning signal used to tune the slave (main) filter
 - Tuning quite accurate
 - Issue → reference signal feedthrough to the filter output
 - □ Master VCO used in tuning loop
 - Design of reliable & stable VCO challenging
 - Issue → reference signal feedthrough
 - □ Single integrator in negative feedback loop forces time-constant to be a function of accurate clock frequency
 - More flexibility in choice of reference frequency → less feedthrough issues
 - DC locking of a replica of the integrator to an external resistor
 - DC offset issues & does not account for integrating capacitor variations
 - Periodic digitally assisted tuning
 - Requires digital capability + minimal additional hardware
 - Advantage of no reference signal feedthrough since tuning performed off-line

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RLC Highpass Filters

- Any RLC lowpass and values derived from tables can be converted to highpass by:
 - -Replacing all Cs by Ls and $L_{Norm}^{HP} = 1/C_{Norm}^{LP}$
 - -Replacing all Ls by Cs and $C_{Norm}^{HP} = 1/L_{Norm}^{LP}$
 - $-L^{HP}=L_r/C_{Norm}^{LP}$, $C^{HP}=C_r/L_{Norm}^{LP}$ where $L_r=R_r/\omega_r$ and $C_r=1/(R_r\omega_r)$



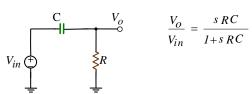


Highpass

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Integrator Based High-Pass Filters 1st Order

Conversion of simple high-pass RC filter to integrator-based type by using signal flowgraph technique



$$\frac{V_O}{V_{in}} = \frac{s\,RC}{1 + s\,RC}$$

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> 1st Order Integrator Based High-Pass Filter Signal Flowgraph

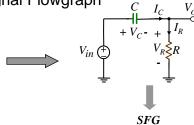
$$V_R = V_{in} - V_C$$

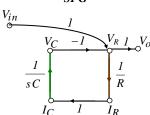
$$V_C = I_C \times \frac{1}{sC}$$

$$V_O = V_R$$

$$I_R = V_R \times \frac{1}{R}$$

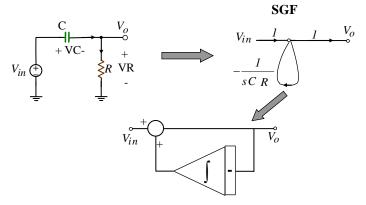
$$I_C = I_R$$





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1st Order Integrator Based High-Pass Filter SGF



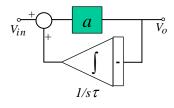
Note: Addition of an integrator in the feedback path → High pass frequency shaping

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Addition of Integrator in Feedback Path

Let us assume flat gain in forward path (a) Effect of addition of an integrator in the feedback path:

$$\begin{split} \frac{V_o}{V_{in}} &= \frac{a}{I + af} \\ \frac{V_o}{V_{in}} &= \frac{a}{I + a/s\,\tau} = \frac{s\,\tau}{I + s\,\tau/a} \end{split}$$



$$\rightarrow$$
 zero@DC & pole@ $\omega_{pole} = -\frac{a}{\tau} = -a \times a_o^{intg}$

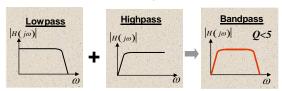
Note: For large forward path gain, a, can implement high pass function with high corner frequency

Addition of an integrator in the feedback path \Rightarrow zero @ DC + pole @ $ax\omega_0^{intg}$ This technique used for offset cancellation in systems where the low frequency content is not important and thus disposable

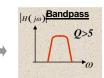
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Bandpass Filters

- Bandpass filters → two cases:
 - 1- Low Q or wideband (Q < 5)
 - → Combination of lowpass & highpass



- 2- High Q or narrow-band (Q > 5)
 - → Direct implementation



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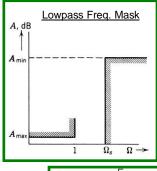
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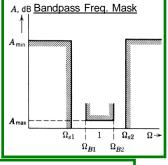
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Narrow-Band Bandpass Filters Direct Implementation

- Direct Implementation

 Narrow-band BP filters → Design based on lowpass prototype
- Same tables used for LPFs are also used for BPFs





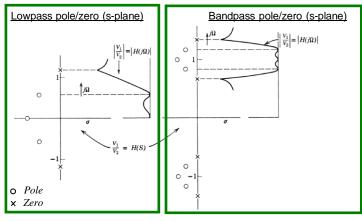
 $s \Rightarrow Q \times \left[\frac{s}{\omega_c} + \frac{\omega_c}{s} \right]$

 $\frac{\Omega_s}{\Omega_c} \Rightarrow \frac{\Omega_{s2} - \Omega_{s1}}{\Omega_{B2} - \Omega_{B1}}$

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Lowpass to Bandpass Transformation S-plane Comparison



From: Zverev, Handbook of filter synthesis, Wiley, 1967- p.156.

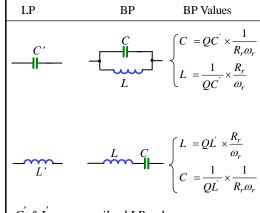
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Lowpass to Bandpass Transformation Table

Lowpass RLC filter structures & tables used to derive bandpass filters

$$Q = Q_{filter}$$

From: Zverev, *Handbook of filter synthesis*, Wiley, 1967- p.157.



C' & L' are normilzed LP values

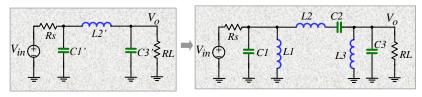
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Lowpass to Bandpass Transformation Example: 3rd Order LPF → 6th Order BPF

Lowpass

Bandpass



- · Each capacitor replaced by parallel L& C
- Each inductor replaced by series L&C

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Lowpass to Bandpass Transformation Example: 3rd Order LPF → 6th Order BPF

$$C_1 = QC_1^{'} \times \frac{1}{R\omega_0}$$

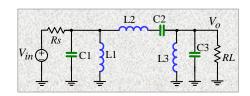
$$L_1 = \frac{1}{QC_1'} \times \frac{R}{\omega_0}$$

$$C_2 = \frac{1}{Q \dot{L_2}} \times \frac{1}{R \omega_0}$$

$$L_2 = QL_2 \times \frac{R}{\omega_0}$$

$$C_3 = QC_3' \times \frac{1}{R\omega_0}$$

$$L_3 = \frac{1}{OC_3} \times \frac{R}{\omega_0}$$

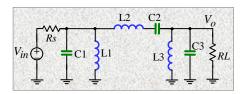


Where:

$$C_1$$
, L_2 , C_3

- $C_1^{'}$, $L_2^{'}$, $C_3^{'}$ \rightarrow Normalized lowpass values
 - → Bandpass filter quality factor
 - → Filter center frequency

Lowpass to Bandpass Transformation Signal Flowgraph

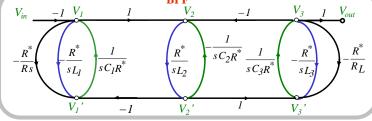


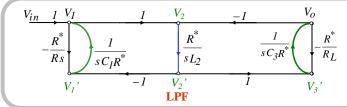
- 1- Voltages & currents named for all components
- 2- Use KCL & KVL to derive state space description
- 3- To have BMFs in the integrator form
 Cap. voltage expressed as function of its current $V_C = f(I_C)$ Ind. current as a function of its voltage $I_L = f(V_L)$
- 4- Use state space description to draw SFG
- 5- Convert all current nodes to voltage

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Signal Flowgraph 6th Order BPF versus 3rd Order LPF BPF V₂ -1 V₃

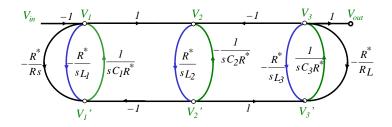




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Signal Flowgraph 6th Order Bandpass Filter



Note: each C & L in the original lowpass prototype \Rightarrow replaced by a *resonator* Substituting the bandpass $L1, C1, \ldots$ by their normalized lowpass equivalent from page 58

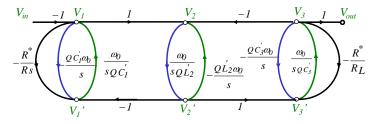
The resulting SFG is:

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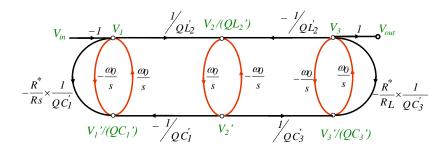
Signal Flowgraph 6th Order Bandpass Filter



- Note the integrators → different time constants
 - Ratio of time constants for two integrator in each resonator loop~ Q^2
 - → Typically, requires high component ratios
 - → Poor matching
- Desirable to modify SFG so that <u>all integrators have equal time constants for optimum matching.</u>
 - To obtain equal integrator time constant \rightarrow use node scaling

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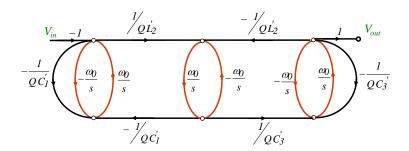
Signal Flowgraph 6th Order Bandpass Filter



- All integrator time-constants → equal
- To simplify implementation \rightarrow choose $RL=Rs=R^*$

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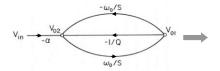
Signal Flowgraph 6th Order Bandpass Filter



Let us try to build this bandpass filter using the simple Gm-C structure

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Second Order Gm-C Filter Using Simple Source-Couple Pair Gm-Cell

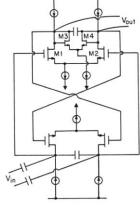


· Center frequency:

$$\omega_o = \frac{g_m^{M1,2}}{2 \times C_{intg}}$$

• Q function of:

$$Q = \frac{g_m^{M1,2}}{g_m^{M3,4}}$$



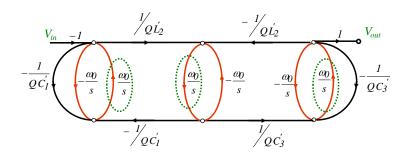
Use this structure for the 1^{st} and the 3^{rd} resonator Use similar structure w/o M3, M4 for the 2^{nd} resonator How to couple the resonators?

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Coupling of the Resonators 1- Additional Set of Input Devices



Coupling of resonators:

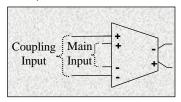
Use additional input source coupled pairs for the highlighted integrators For example, the middle integrator requires 3 sets of inputs

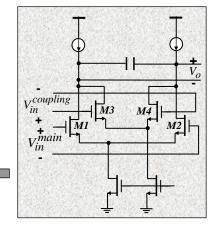
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Example: Coupling of the Resonators 1- Additional Set of Input Devices

- Add one source couple pair for each additional input
- ■Coupling level → ratio of device widths
- ■Disadvantage → extra power dissipation



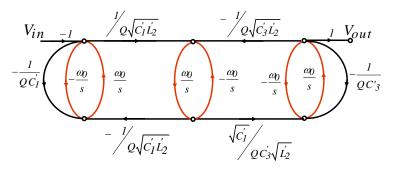


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Coupling of the Resonators 2- Modify SFG → Bidirectional Coupling Paths

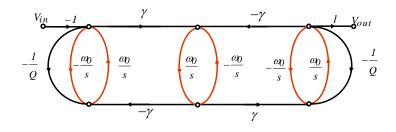


Modified signal flowgraph to have equal coupling between resonators

- In most filter cases $C_I = C_3$
- Example: For a butterworth lowpass filter $C_1' = C_3' = 1 \& L_2' = 2$
- Assume desired overall bandpass filter Q=10

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Sixth Order Bandpass Filter Signal Flowgraph



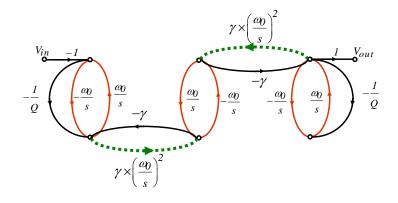
- Where for a Butterworth shape $\gamma = \frac{1}{Q\sqrt{2}}$
- Since in this example Q=10 then: $\gamma \approx \frac{1}{14}$

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Sixth Order Bandpass Filter Signal Flowgraph SFG Modification



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Sixth Order Bandpass Filter Signal Flowgraph SFG Modification

For narrow band filters (high Q) where frequencies within the passband are close to ω_0 narrow-band approximation can be used:

Within filter passband:

$$\left(\frac{\omega_0}{\omega}\right)^2 \approx 1$$

$$\gamma \times \left(\frac{\omega_0}{s}\right)^2 = \gamma \times \left(\frac{\omega_0}{j\omega}\right)^2 \approx -\gamma$$

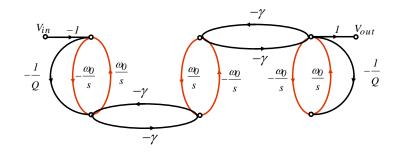
The resulting SFG:

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Sixth Order Bandpass Filter Signal Flowgraph SFG Modification



Bidirectional coupling paths, can easily be implemented with coupling capacitors → no extra power dissipation

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