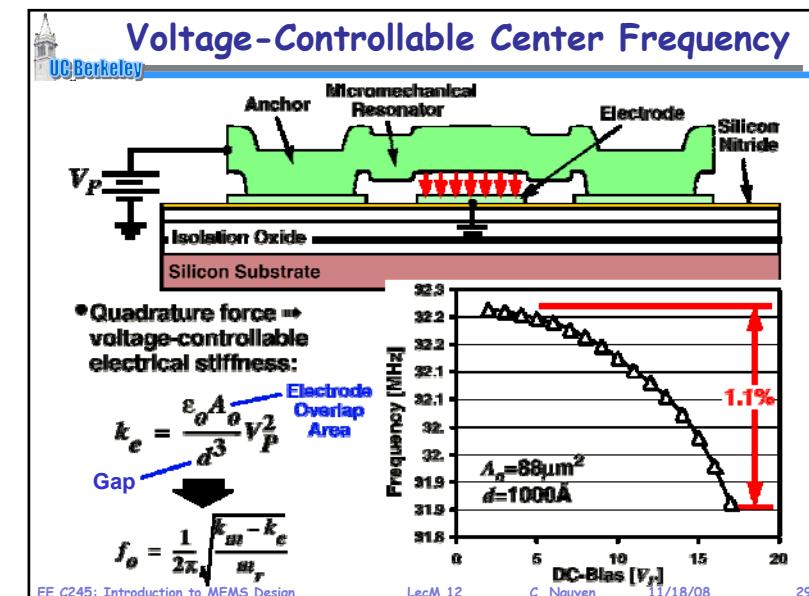
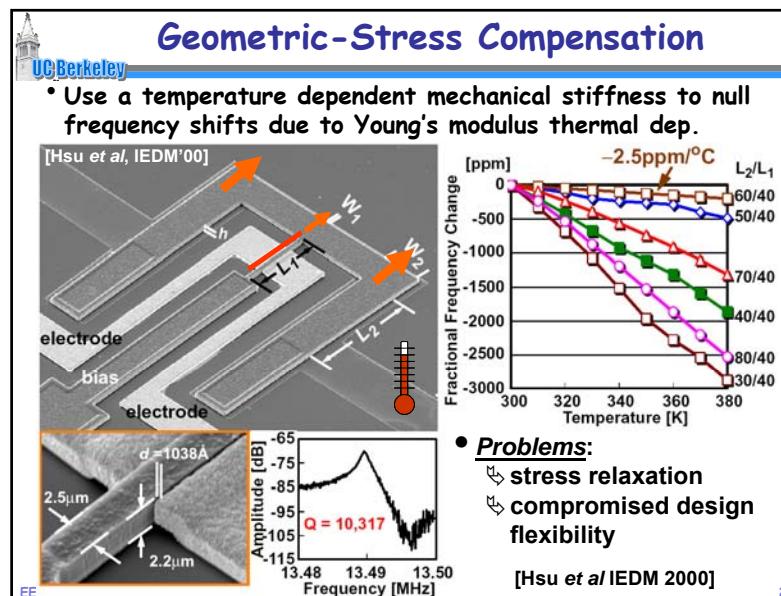
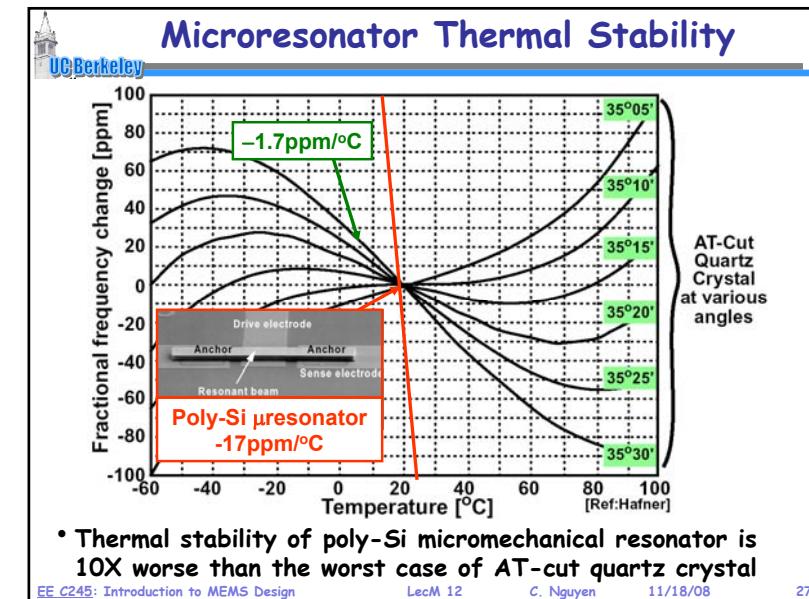
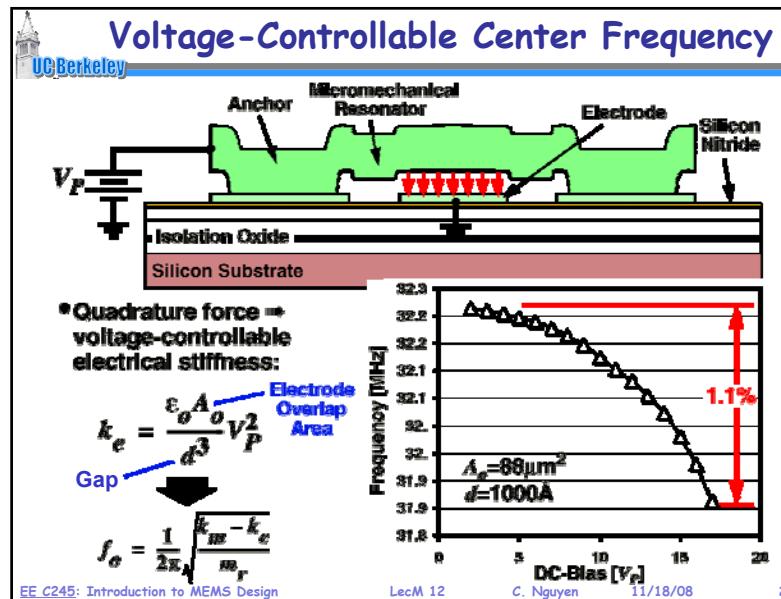
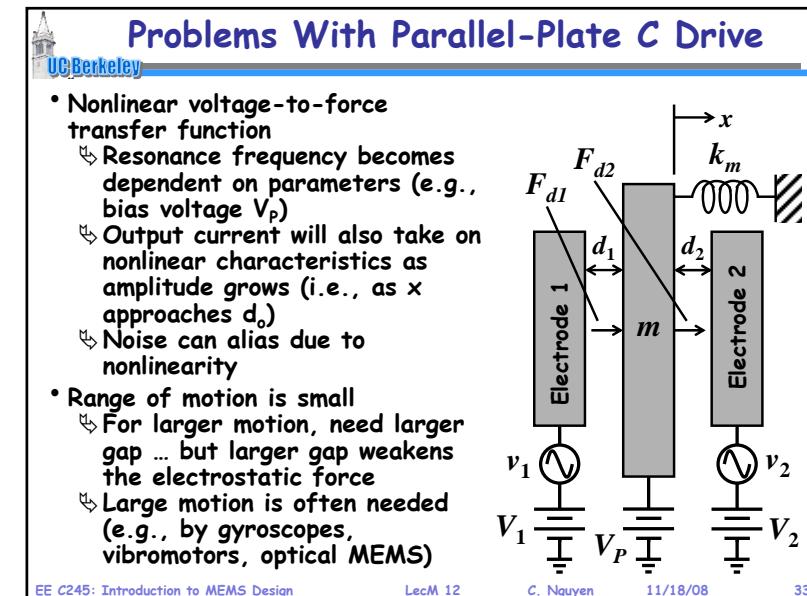
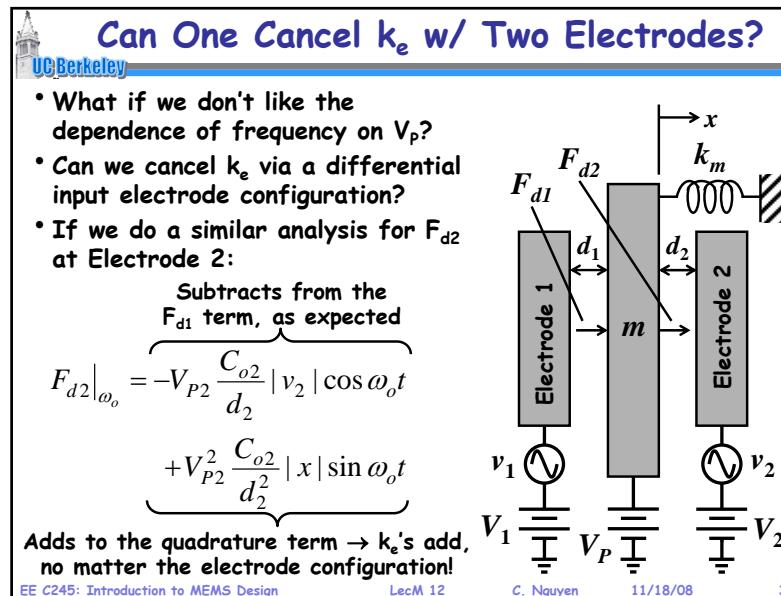
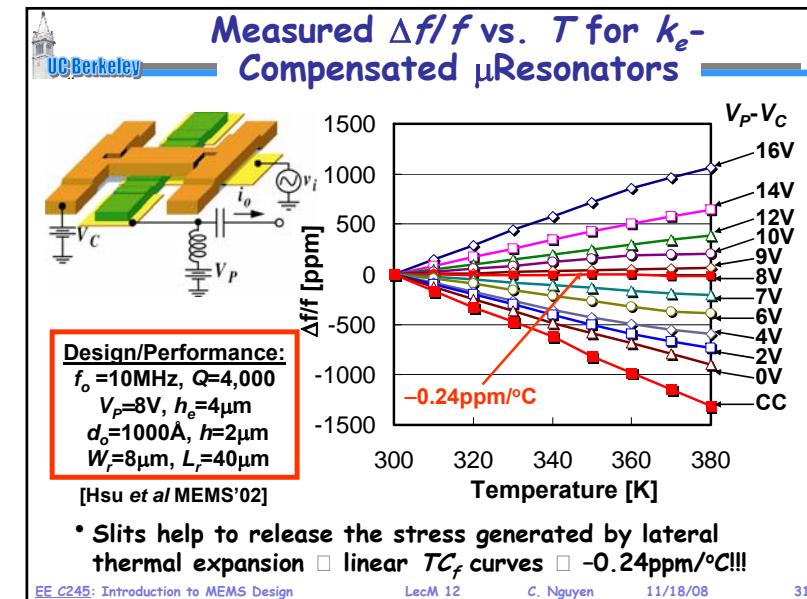
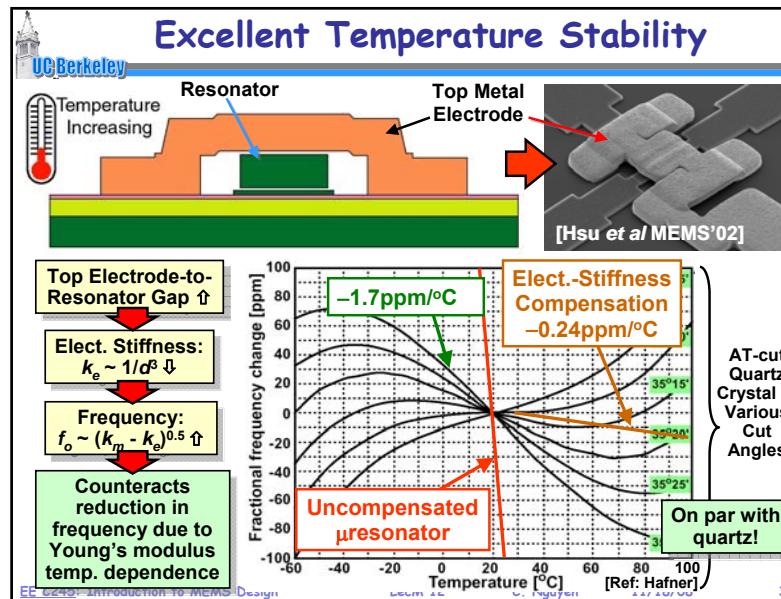


Lecture 23m1: Capacitive Transducers



Lecture 23m1: Capacitive Transducers



Lecture 23m1: Capacitive Transducers

Electrostatic Comb Drive

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Electrostatic Comb Drive

- Use of comb-capacitive transducers brings many benefits
 - ↳ Linearizes voltage-generated input forces
 - ↳ (Ideally) eliminates dependence of frequency on dc-bias
 - ↳ Allows a large range of motion

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Comb-Drive Force Equation (1st Pass)

Top View Side View

$$C(x) = \frac{2\epsilon_0 x h}{d} \rightarrow \left[\frac{\partial C}{\partial x} = \frac{2\epsilon_0 h}{d} \right]$$

$$F_d = \frac{\partial W}{\partial x} = \frac{1}{2} \frac{\partial C}{\partial x} (V_p - V_i)^2 = \frac{1}{2} \frac{\epsilon_0 h}{d} (V_p^2 - 2V_p V_i + V_i^2) \approx -2V_p \frac{\epsilon_0 h}{d} V_i = F_d$$

When $V_i = (t)$ $\rightarrow F_d = (-)$ ✓

But wait! This ignores other practical effects! (No dependence on t ! LINEAR!)

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Lateral Comb-Drive Electrical Stiffness

Top View Side View

Again: $C(x) = \frac{2N\epsilon_0 h x}{d} \rightarrow \frac{\partial C}{\partial x} = \frac{2N\epsilon_0 h}{d}$

- No $(\partial C / \partial x)$ x-dependence \rightarrow no electrical stiffness: $k_e = 0!$
- Frequency immune to changes in V_p or gap spacing!

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Lecture 23m1: Capacitive Transducers

Typical Drive & Sense Configuration

Simple Analysis:

$$F_{d1} = \frac{1}{2} \frac{\partial C_1}{\partial x} (V_1 - V_{p1})^2 = \frac{1}{2} \left(\frac{\epsilon_0 h}{d_1} \right) (V_1^2 - 2V_{p1}V_1 + V_{p1}^2)(2N_f)$$

$$F_{d2} = \frac{1}{2} \frac{\partial C_2}{\partial x} (V_2 - V_{p2})^2 = \frac{1}{2} \left(\frac{\epsilon_0 h}{d_2} \right) (V_2^2 - 2V_{p2}V_2 + V_{p2}^2)(2N_f)$$

$$\therefore F_{net} = F_{d1} + F_{d2} = \frac{1}{2} \left(\frac{\epsilon_0 h}{d} \right) (V_2^2 - V_1^2 - 2(V_{p2}V_2 - V_{p1}V_1) + V_{p2}^2 - V_{p1}^2)(2N_f)$$

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Comb-Drive Force Equation (2nd Pass)

- In our 1st pass, we accounted for
 - Parallel-plate capacitance between stator and rotor
- ... but neglected:
 - Fringing fields
 - Capacitance to the substrate
- All of these capacitors must be included when evaluating the energy expression!

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Comb-Drive Force With Ground Plane Correction

- Finger displacement changes not only the capacitance between stator and rotor, but also between these structures and the ground plane → modifies the capacitive energy

$$F_{e,x} = \frac{\partial W'}{\partial x} = \frac{1}{2} \frac{dC_{sp}}{dx} V_s^2 + \frac{1}{2} \frac{dC_{rp}}{dx} V_r^2 + \frac{1}{2} \frac{dC_{ns}}{dx} (V_s - V_r)^2$$

[Gary Fedder, Ph.D., UC Berkeley, 1994]

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Capacitance Expressions

- Case: $V_r = V_p = 0V$
- C_{sp} depends on whether or not fingers are engaged

$$C_{sp} = N[C'_{sp,e}x + C'_{sp,n}(L-x)]$$

$$C_{ns} = NC'_{ns}x$$

Capacitance per unit length

Region 2

Region 3

[Gary Fedder, Ph.D., UC Berkeley, 1994]

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UC Berkeley

Comb-Drive Force With Ground Plane Correction

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$$F_{e,x} = \frac{N}{2} (C'_{rs} + C'_{sp,e} - C'_{sp,g}) V_s^2 \quad (\text{for } V_r = V_p = 0)$$

[Gary Fedder, Ph.D., UC Berkeley, 1994]

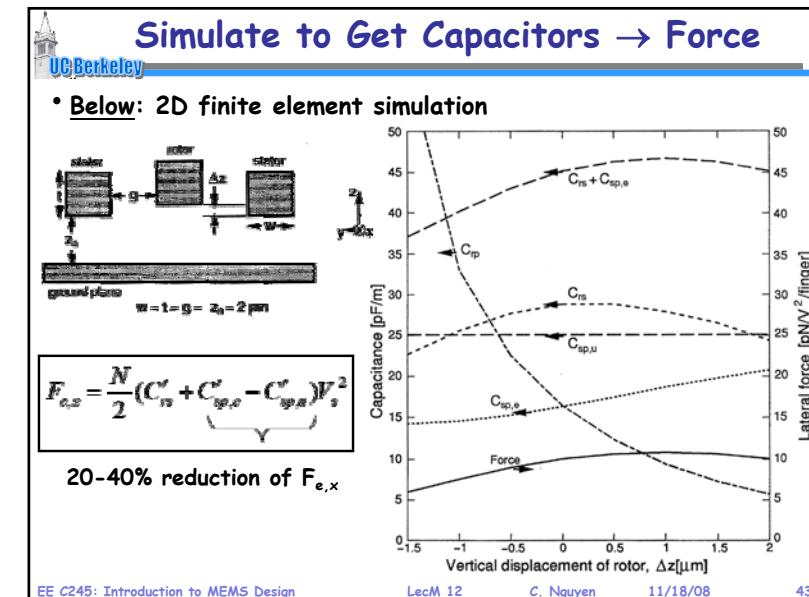
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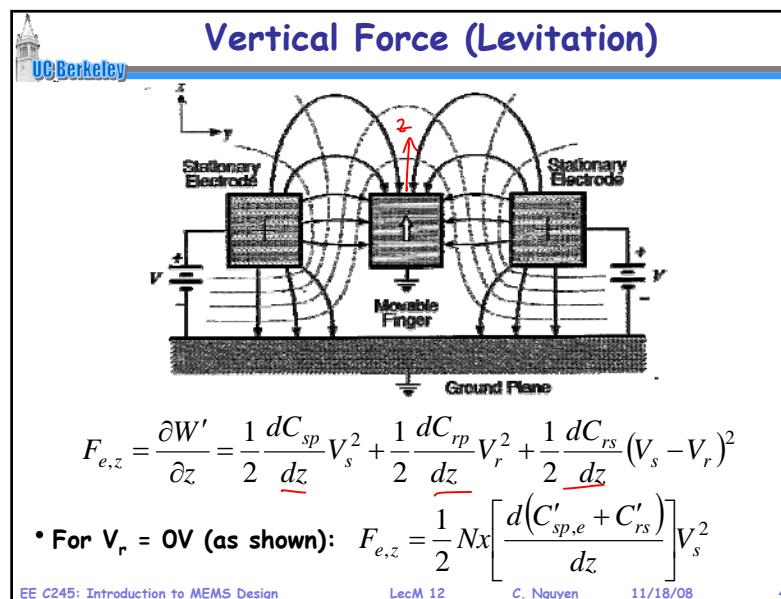
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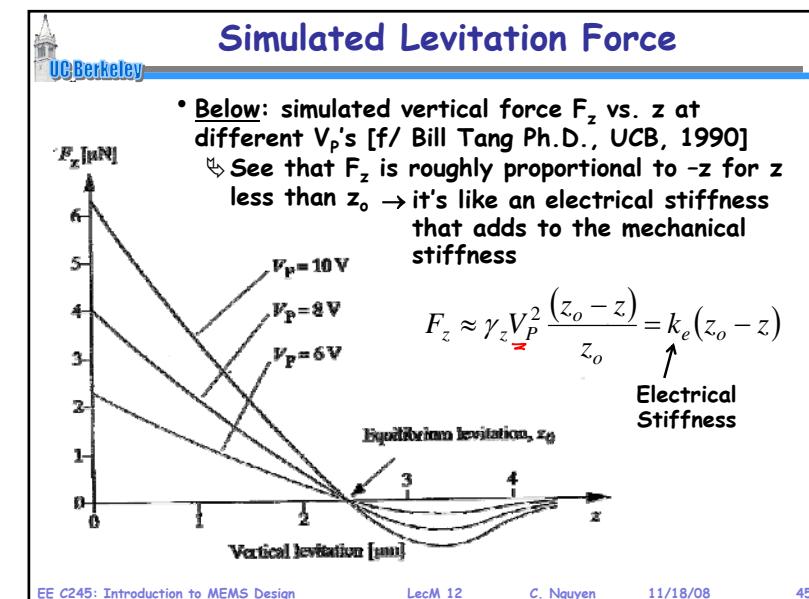
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