

Suspension Beam in Tension



* Bending contribution:

$$k_b^{-1} = (1/k_e + 1/k_e) = 2 \left[\frac{(L/2)^3}{3E(Wh^3/12)} \right] = \frac{L^3}{EWh^3} = 4.2 \,\mu\text{m}/\mu\text{N}$$

• Stretching contribution:

$$k_{nt}^{-1} = L/S = \frac{L}{\sigma_{n}Wh} = 1.14\mu m/\mu N$$

$$S = \frac{1}{F_{y}} = S \sin\theta \approx S(x/L) = (\frac{S}{L})x$$

• Total spring constant: add bending to stretching (sine they are in parallel)

$$k = 4(k_b + k_{st}) = 4(0.24 + 0.88) = 4.5 \mu N / \mu m$$

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ADXL-50 Resonance Frequency

Using a lumped mass-spring approximation:

$$f = \frac{1}{2\pi} \sqrt{\frac{k}{M}} = \frac{1}{2\pi} \sqrt{\frac{4.48N/m}{162x10^{-12} kg}} = 26.5kHz$$

- On the ADXL-50 Data Sheet: $f_0 = 24 \text{ kHz}$
 - ♦ Why the 10% difference?
 - ♥ Well, it's approximate ... plus ...
 - ♦ Above analysis does not include the frequency-pulling effect of the DC bias voltage across the plate sense fingers and stationary sense fingers ... something we'll cover later on ...

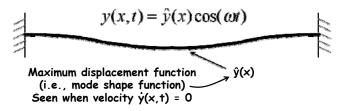
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Distributed Mechanical Structures

* Vibrating structure displacement function:



- Procedure for determining resonance frequency:
 - Use the static displacement of the structure as a trial function and find the strain energy W_{max} at the point of maximum displacement (e.g., when t=0, π/ω , ...)
 - Determine the maximum kinetic energy when the beam is at zero displacement (e.g., when it experiences its maximum velocity)
 - Sequate energies and solve for frequency

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Maximum Kinetic Energy

- Displacement: $y(x,t) = \hat{y}(x)\cos[\omega t]$
- Velocity: $v(x,t) = \frac{\partial y(x,t)}{\partial t} = -\omega \hat{y}(x) \sin[\omega t]$
- At times t = $\pi/(2\omega)$, $3\pi/(2\omega)$, ...



Velocity topographical mapping

- \heartsuit The displacement of the structure is y(x,t) = 0
- $\$ The velocity is maximum and all of the energy in the structure is kinetic (since W=0):

$$v(x,(2n+1)\pi/(2\omega)) = -\omega \hat{y}(x)$$

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