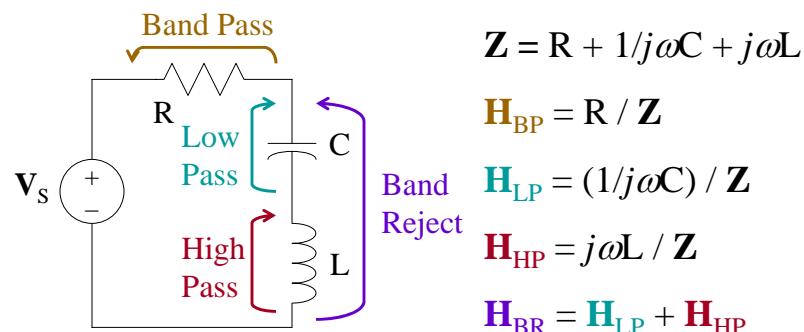


## Midterm 1 Announcements

- Review session: 5-8pm TONIGHT 277 Cory
- Midterm 1:
  - 11:30-1pm on Tuesday, July 12 in Dwinelle 145.
  - Material covered in HW1-3
- Attend only your second lab slot this week

## Review: Second-Order Filter Circuits



## Lecture #9

### OUTLINE

- The operational amplifier (“op amp”)
- Ideal op amp
- Feedback
- Unity-gain voltage follower circuit
- Summing, difference, integrator, differentiator, active filter

### Reading

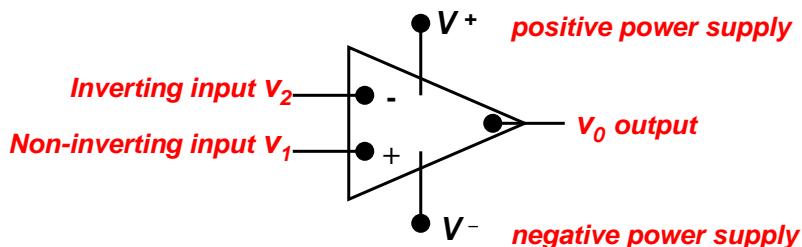
Ch. 14

## The Operational Amplifier

- The ***operational amplifier*** (“***op amp***”) is a basic building block used in analog circuits.
  - Its behavior is modeled using a dependent source.
  - When combined with resistors, capacitors, and inductors, it can perform various useful functions:
    - **amplification/scaling** of an input signal
    - **sign changing** (inversion) of an input signal
    - **addition** of multiple input signals
    - **subtraction** of one input signal from another
    - **integration** (over time) of an input signal
    - **differentiation** (with respect to time) of an input signal
    - **analog filtering**
    - **nonlinear functions** like exponential, log, sqrt, etc

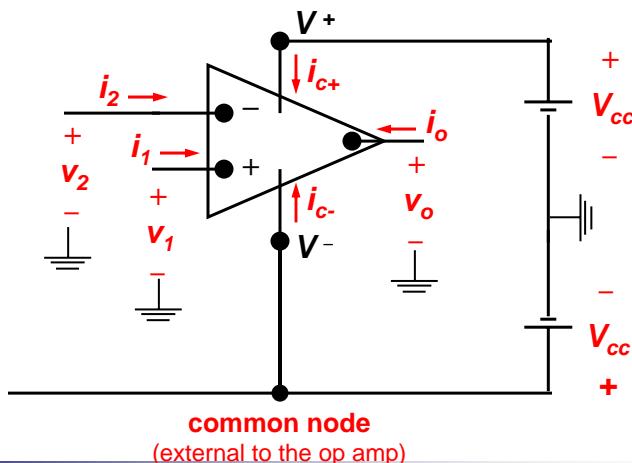
## Op Amp Terminals

- 3 signal terminals: 2 inputs and 1 output
- IC op amps have 2 additional terminals for DC power supplies
- Common-mode signal =  $(v_1 + v_2)/2$
- Differential signal =  $v_1 - v_2$



## Op Amp Terminal Voltages and Currents

- All voltages are referenced to a common node.
- Current reference directions are into the op amp.



## Model

- A is differential gain or open loop gain
- Ideal op amp

$$A \rightarrow \infty$$

$$R_i \rightarrow \infty$$

$$R_o = 0$$

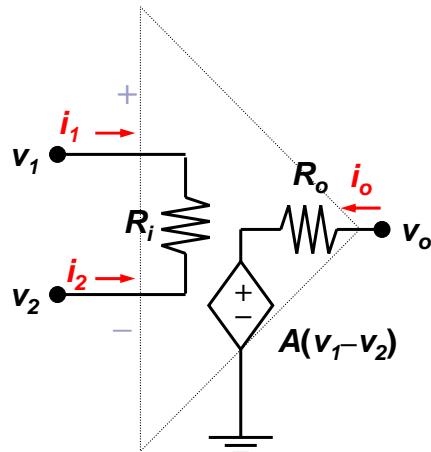
- Common mode gain = 0

$$v_{cm} = \frac{(v_1 + v_2)}{2}, v_d = v_1 - v_2$$

$$v_o = A_{cm} v_{cm} + A_d v_d$$

$$\text{Since } v_o = A(v_1 - v_2), A_{cm} = 0$$

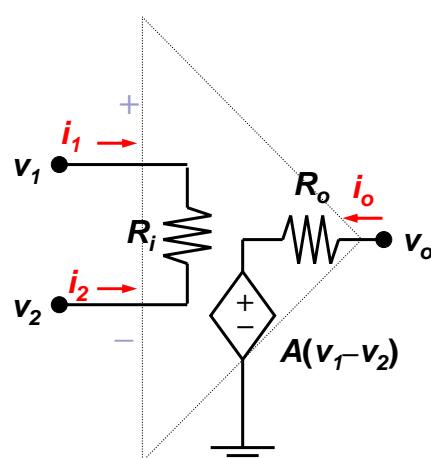
### Circuit Model



## Model and Feedback

- Negative feedback
  - connecting the output port to the negative input (port 2)
- Positive feedback
  - connecting the output port to the positive input (port 1)

### Circuit Model

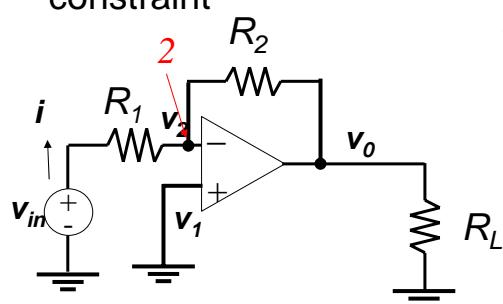


## Summing-Point Constraint

- Check if under negative feedback
  - Small  $v_i$  result in large  $v_o$
  - Output  $v_o$  is connected to the inverting input to reduce  $v_i$
  - Resulting in  $v_i=0$
- Summing-point constraint
  - $v_1 = v_2$
  - $i_1 = i_2 = 0$
- Virtual short circuit
  - Not only voltage drop is 0 (which is short circuit), input current is 0
  - This is different from short circuit, hence called "virtual" short circuit.

## Inverting Amplifier

- Negative feedback → checked
- Use summing-point constraint



$$\text{Closed loop gain} = A_v = \frac{v_o}{v_{in}}$$

$$v_1 = v_2 = 0, i_1 = i_2 = 0$$

Use KCL At Node 2.

$$i = \frac{(v_{in} - v_2)}{R_1} = \frac{(v_{out} - v_2)}{R_2}$$

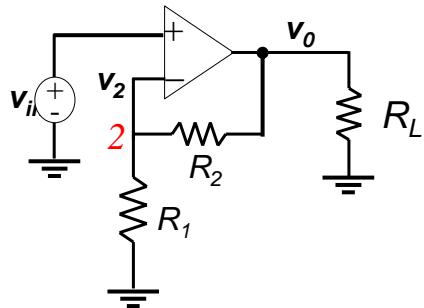
$$v_o = -\frac{R_2 v_o}{R_1}$$

$$\text{Input impedance} = \frac{v_{in}}{i} = R_1$$

Ideal voltage source – independent of load resistor

## Non-Inverting Amplifier

### ■ Ideal voltage amplifier



$$\text{Closed loop gain} = A_v = \frac{v_o}{v_{in}}$$

$$v_1 = v_2 = v_{in}, i_1 = i_2 = 0$$

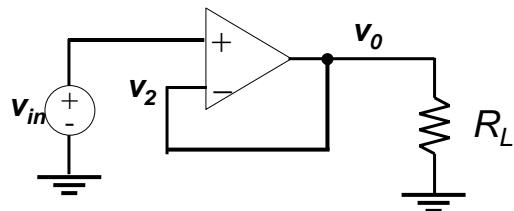
Use KCL At Node 2.

$$i = \frac{(v_o - v_2)}{R_2} = \frac{(v_2 - 0)}{R_1}$$

$$A = \frac{v_o}{v_{in}} = \frac{(R_1 + R_2)}{R_1}$$

$$\text{Input impedance} = \frac{v_{in}}{i} \rightarrow \infty$$

## Voltage Follower



$$R_2 = 0$$

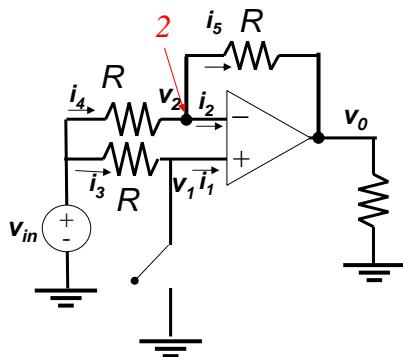
$$R_1 \rightarrow \infty$$

$$i = \frac{(v_o - v_2)}{R_2} = \frac{(v_2 - 0)}{R_1}$$

$$A = \frac{v_o}{v_{in}} = \frac{(R_1 + R_2)}{R_1} = 1 + \frac{R_2}{R_1} = 1$$

## Example 1

### ■ Switch is open



$$v_1 = v_2, i_1 = 0 \rightarrow i_3 = 0$$

$$i_3 = \frac{(v_{in} - v_1)}{R} \rightarrow v_1 = v_2 = v_{in} \rightarrow i_4 = 0 \rightarrow i_5 = 0$$

$$i_5 = \frac{(v_0 - v_2)}{R} \rightarrow v_0 = v_2 = v_{in}$$

$$A = \frac{v_o}{v_{in}} = 1, R_{in} \rightarrow \infty$$

### ■ Switch is closed

$$v_1 = v_2 = 0, i_1 = 0 \rightarrow i_3 = 0$$

$$i_4 = \frac{(v_{in} - v_2)}{R} = i_5 = -\frac{(v_0 - v_2)}{R}$$

$$v_0 = -v_{in}$$

$$A = \frac{v_o}{v_{in}} = -1, R_{in} = R/2$$

## Example 2

### ■ Design an analog front end

circuit to an instrument system

- Requires to work with 3 full-scale of input signals (by manual switch):

$0 : \pm 1, 0 : \pm 10, 0 : \pm 100 \text{ V}$

- For each input range, the output needs to be  $0 : \pm 10 \text{ V}$

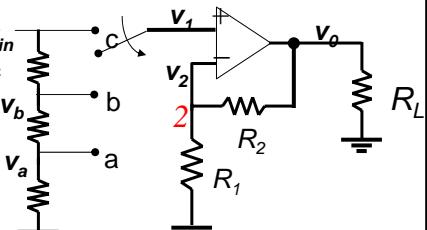
- The input resistance is  $1M\Omega$

$$v_o = \left(1 + \frac{R_2}{R_1}\right)v_1$$

$v_1 = v_{in}$  Switch at c

$$v_1 = \frac{R_a + R_b}{R_a + R_b + R_c} v_{in} \text{ Switch at b}$$

$$v_1 = \frac{R_a}{R_a + R_b + R_c} v_{in} \text{ Switch at a}$$



## Example 2 (cont'd)

$$R_{in} = R_a + R_b + R_c = 1M\Omega$$

Max  $A_v = 10 = (1 + \frac{R_2}{R_1})$  Switch at c

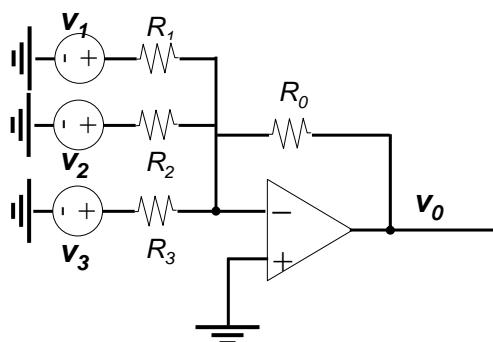
$$A_v = 1 = \frac{R_a + R_b}{R_a + R_b + R_c} (1 + \frac{R_2}{R_1}) \text{ Switch at b} \therefore \frac{R_a + R_b}{R_a + R_b + R_c} = 0.1$$

$$A_v = 0.1 = \frac{R_a}{R_a + R_b + R_c} (1 + \frac{R_2}{R_1}) \text{ Switch at a} \therefore \frac{R_a}{R_a + R_b + R_c} = 0.01$$

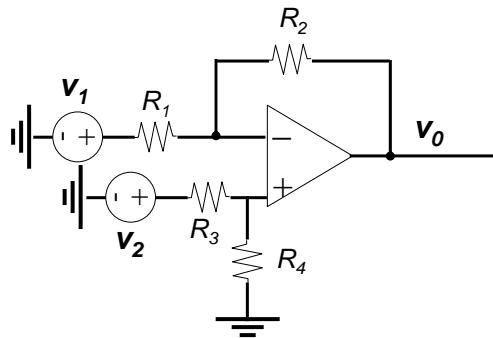
$$\therefore R_a = 10k\Omega, R_b = 90k\Omega, R_c = 900k\Omega$$

$$R_2 = 9R_1$$

## Summing Amplifier



## Difference Amplifier



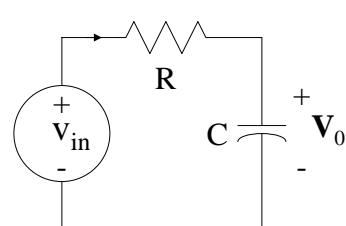
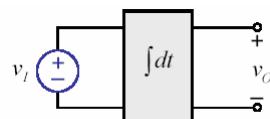
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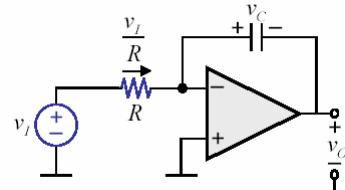
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## Integrator

- Want  $v_o = K \int v_{in} dt$
- What is the difference between:



$$v_o \approx \frac{1}{RC} \int_{-\infty}^t v_i dt$$



$$v_o = -\frac{1}{C} \int_{-\infty}^t v_i dt$$

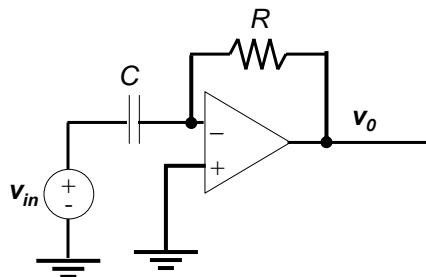
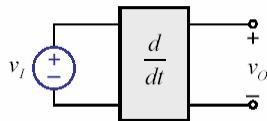
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## Differentiator

- Want



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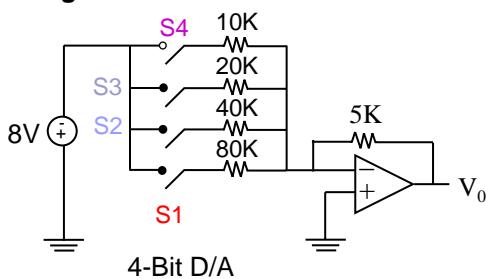
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## Application: Digital-to-Analog Conversion

A DAC can be used to convert the digital representation of an audio signal into an analog voltage that is then used to drive speakers -- so that you can hear it!

### “Weighted-adder D/A converter”



(Transistors are used  
as electronic switches)

S1 closed if LSB = 1

S2 " if next bit = 1

S3 " " = 1

S4 " if MSB = 1

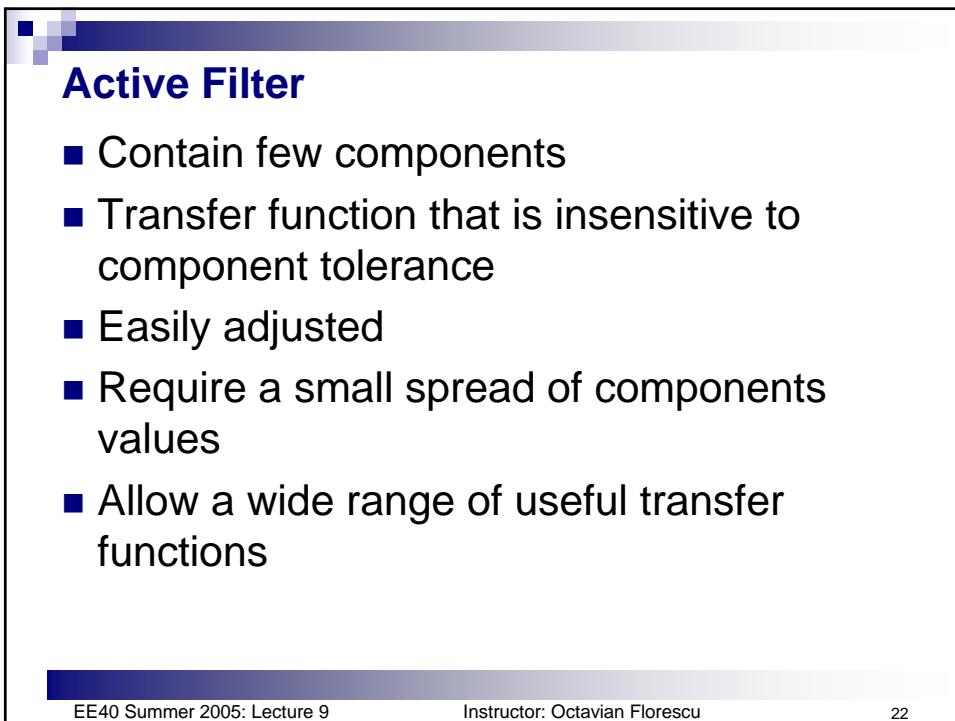
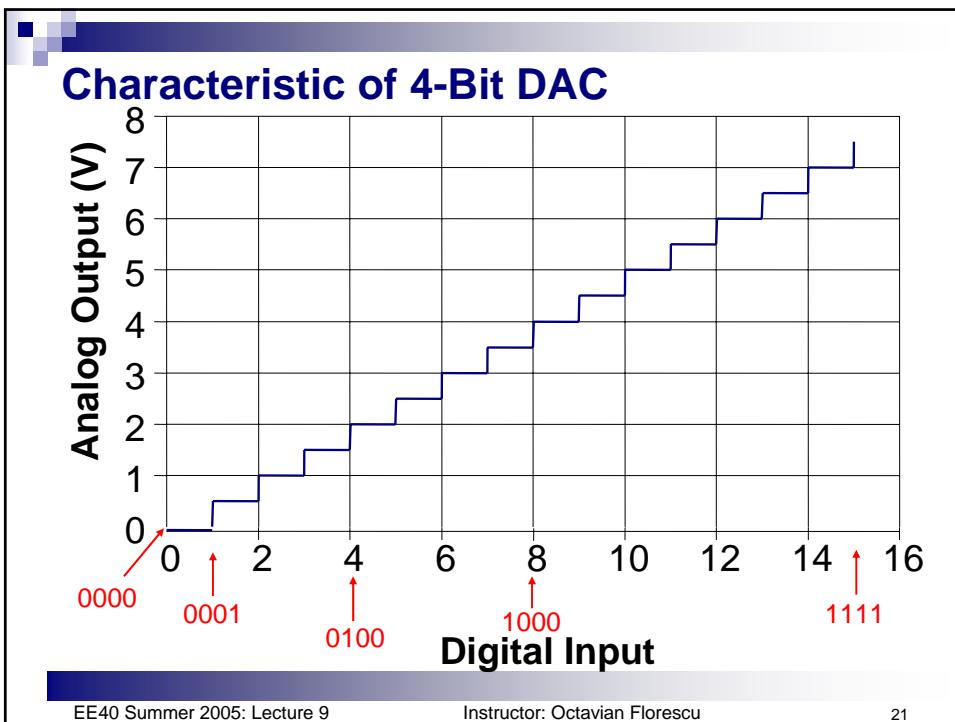
Binary number	Analog output (volts)
0 0 0 0	0
0 0 0 1	.5
0 0 1 0	1
0 0 1 1	1.5
0 1 0 0	2
0 1 0 1	2.5
0 1 1 0	3
0 1 1 1	3.5
1 0 0 0	4
1 0 0 1	4.5
1 0 1 0	5
1 0 1 1	5.5
1 1 0 0	6
1 1 0 1	6.5
1 1 1 0	7
1 1 1 1	7.5

MSB      LSB

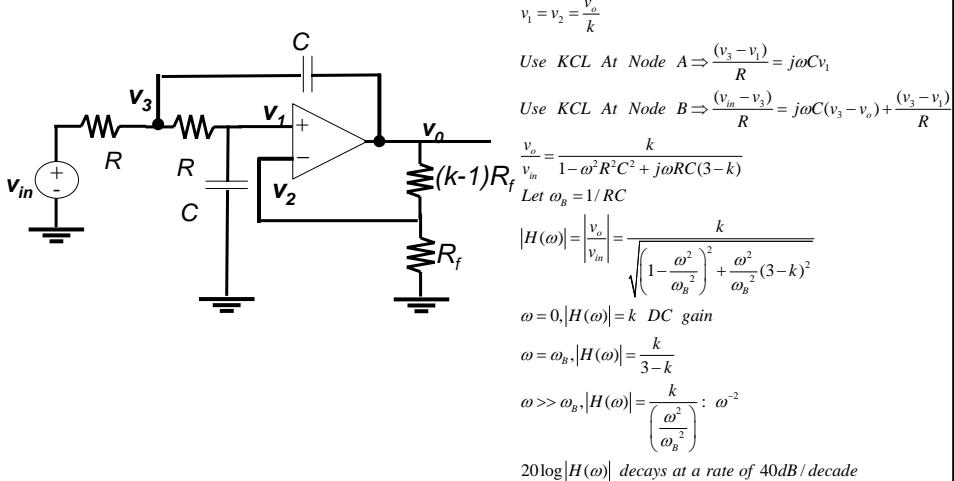
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## Active Filter Example

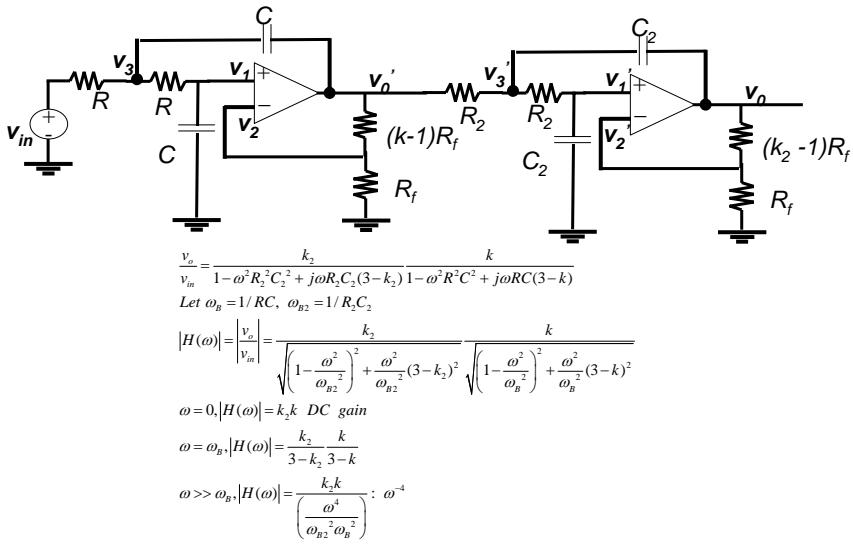


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## Cascaded Active Filter Example



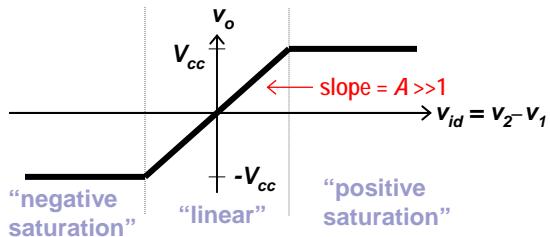
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## Op Amp Voltage Transfer Characteristic

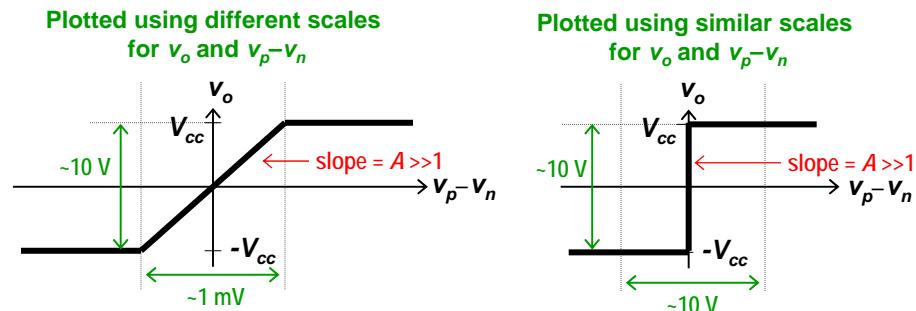
The op amp is a differentiating amplifier:



- In the linear region,  $V_o = A(v_2 - v_1) = A v_{id}$ 
  - $A$  is the open-loop gain
- Typically,  $V_{cc} \leq 20$  V and  $A > 10^4$ 
  - linear range:  $-2$  mV  $\leq v_{id} = (v_2 - v_1) \leq 2$  mV
- Thus, for an op amp to operate in the linear region,
  - $v_2 \approx v_1$
  - There is a “virtual short” between the input terminals.)

## Achieving a “Virtual Short”

- Recall the voltage transfer characteristic of an op amp:



**Q:** How does a circuit maintain a virtual short at the input of an op amp, to ensure operation in the linear region?

**A:** By using **negative feedback**. A signal is fed back from the output to the inverting input terminal, effecting a **stable** circuit connection. Operation in the **linear region** enforces the virtual short circuit.