Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

EECS 42 Introduction to Electronics for Computer Science Andrew R. Neureuther

Lecture #4

- Capacitors and Inductors
- Energy Stored in C and L
- Equivalent Circuits
 - Thevenin
 - Norton

http://inst.EECS.Berkeley.EDU/~ee42/

Copyright 2001, Regents of University of California

EECS 42 Intro. electronics for CS Spring 2003

Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

Game Plan 02/03/03

Monday 02/03/03

☐ Capacitors and Inductors; Equivalent Sources Schwarz and Oldham: 5.1-5.2, 3.1

Wednesday 02/05/03

□ N-L Elements; Graphical Solutions; Power Schwarz and Oldham: 3.2-3.4

Next (4th) Week

□ RC Transient

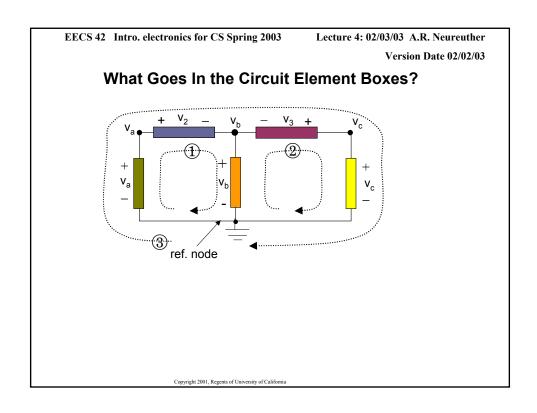
Schwarz and Oldham: 8.1 plus Handouts

Problem Set #2 – Out 1/27/03 - Due 2/5/03 2:30 in box near 275 Cory

2.1 Flow; 2.2 KCL; 2.3 KVL; 2.4 resistor circuit; 2.5 Power

Problem Set #3 – Out 2/2/03 - Due 2/12/03 2:30 in box near 275 Cory

3.1 and 3.2 charging capacitors; 3.3 –3.5; Equivalent Circuits;



Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

BASIC CIRCUIT ELEMENTS

• Voltage Source (always supplies some constant given voltage - like ideal battery)

• Current Source (always supplies some constant given current)

• Resistor (Ohm's law)

• Wire ("short" – no voltage drop)

• Capacitor (capacitor law – based on energy storage in electric field of a dielectric S&O 5.1)

• Inductor (inductor law – based on energy storage in magnetic field in space S&O 5.1)

Lecture 4: 02/03/03 A.R. Neureuther

CAPACITOR

Version Date 02/02/03

Any two conductors a and b separated by an insulator with a difference in voltage V_{ab} will have an equal and opposite charge on their surfaces whose value is given by $Q = CV_{ab}$, where C is the **capacitance** of the structure, and the + charge is on the more positive electrode.

A simple parallel-plate capacitor is shown. If the area of the plate is A, the separation d, and the *dielectric* constant of the insulator is ϵ , the capacitance equals C = A ϵ /d.

Symbol — or — (—

Constitutive relationship: $Q = C (V_a - V_b)$. (Q is positive on plate a if $V_a > V_b$)

But $i = \frac{dQ_a}{dt}$ so $i = C\frac{dv}{dt}$ equivalent to Q = C v

where we use the associated reference directions.

Copyright 2001, Regents of University of California

EECS 42 Intro. electronics for CS Spring 2003

Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

ENERGY STORED IN A CAPACITOR

You might think the energy (in Joules) is QV, which has the dimension of joules. But during charging the average voltage was only half the final value of V.

Thus, energy is
$$\frac{1}{2}QV = \boxed{\frac{1}{2}CV^2}$$

Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

ENERGY STORED IN A CAPACITOR (cont.)

More rigorous derivation: During charging, the power flow is $v \cdot i$ into the capacitor, where i is into + terminal. We integrate the power from t = 0 (v = 0) to t = end (v = V). The integrated power is the energy

$$E = \int\limits_{t = t_{Initial}}^{t = t_{Final}} v \cdot i \, dt = \int\limits_{v = V_{Initial}}^{v = V_{Final}} \frac{dq}{dt} \, dt = \int\limits_{v = V_{Initial}}^{v = V_{Final}} v \cdot dq - \int\limits_{v = V_{Initial}}^{v = t_{Initial}} v \cdot dq - \int\limits_{v = V_{Initial}}^{v = t_{Initial}} v \cdot dq - \int\limits_{v = V_{Initial}}^{v = t_{Initial}} v \cdot dq - \int\limits_{v = t_{Initial$$

but dq = C dv. (We are using small q instead of Q to remind us that it is time varying . Most texts use Q.)

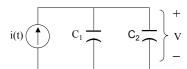
Copyright 2001, Regents of University of California

EECS 42 Intro. electronics for CS Spring 2003

Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

CAPACITORS IN PARALLEL

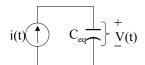


Add Currents

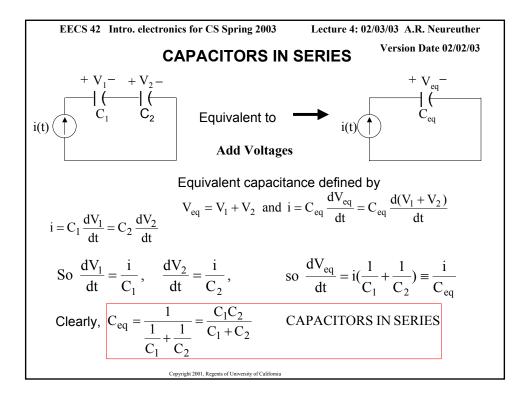
$$i(t) = C_1 \frac{dV}{dt} + C_2 \frac{dV}{dt}$$

Equivalent capacitance defined by

$$i = C \text{eq}^{} \overline{d} \overline{V}$$



Clearly,



Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

Capacitance and Inductance

- Capacitors: two plate example; Store energy in the electric field Q = CV, I = C dV/dt and V = (1/C) integral of voltage
- Computer example 1 mA current charging 1 pF $V(t) = (I/C)t = (10-3 \text{ A}/10^{-12} \text{ F}) t = 10^9 \text{ V/s t}$
- At D.C. time derivatives are zero => C is open circuit
- C in parallel add; series $1/C = \text{sum } (1/C_i)$; short together (infinite current but conserve charge)
- Inductors: coil example; Store energy in the magnetic field; Flux = LI, V = L dI/dt and I = (1/L) (integral of voltage)
- At D.C. time derivatives are zero => L is short circuit
- L in parallel 1/L = sum (1/L_i); series add; connect in series when have different currents => $L_1I_1+L_2I_2 = (L_1+L_2)I_{NEW}$

Lecture 4: 02/03/03 A.R. Neureuther

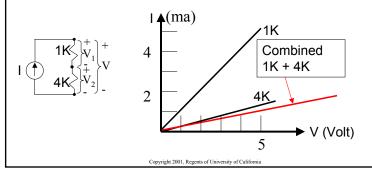
Example of I-V Graphs Version Date 02/02/03

Resistors in Series

If two resistors are in series the current is the same; clearly the total voltage will be the sum of the two IR values i.e. $I(R_1+R_2)$.

Thus the equivalent resistance is R_1+R_2 and the I-V graph of the series pair is the same as that of the equivalent resistance.

Of course we can also find the I-V graph of the combination by adding the voltages directly on the I-V axes. Lets do an example for 1K + 4K resistors



EECS 42 Intro. electronics for CS Spring 2003

Lecture 4: 02/03/03 A.R. Neureuther

Example of I-V Graphs

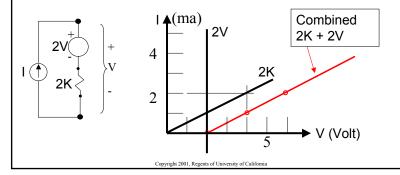
Version Date 02/02/03

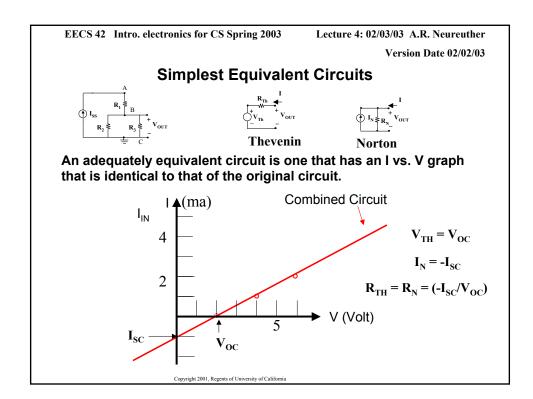
Simple Circuit, e.g. voltage source + resistor.

If two circuit elements are in series the current is the same; clearly the total voltage will be the sum of the voltages i.e. V_S + IR.

We can graph this on the I-V plane. We find the I-V graph of the combination by adding the voltages $V_{\rm S}$ and I R at each current I.

Lets do an example for =2V, R=2K





Lecture 4: 02/03/03 A.R. Neureuther

Version Date 02/02/03

I vs. V and Equivalent Circuits

- I vs. V for ideal voltage source is a vertical line at $V = V_{SV}$
- I vs. V for ideal current source is a horizontal line at $I = I_{SC}$
- I vs. V for a circuit made up of ideal independent sources and resistors is a straight line.
- The simplest circuit for a straight line is an ideal voltage source and a resistor (Thevenin) or a current source and a parallel resistor (Norton)
- The easiest way to find the I vs. V line is to find the intercepts where I = 0 (open circuit voltage V_T) and where V = 0 (Short circuit current I_N)
- The short-cut for finding the (slope) $^{-1} = R_T = R_N$ is to turn off all of the dependent sources to zero and find the remaining equivalent resistance between the terminals of the elements.