EECS 42 Intro. electronics for CS Spring 2003 Handout on RC Circuits. A.R. Neureuther

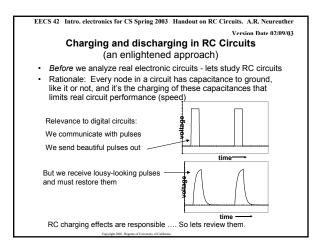
Version Date 02/09/03

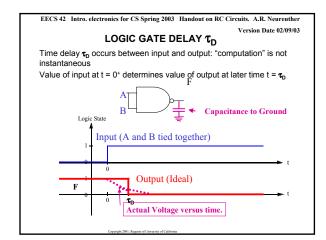
Charging and Discharging RC Circuits Handout for EECS 42

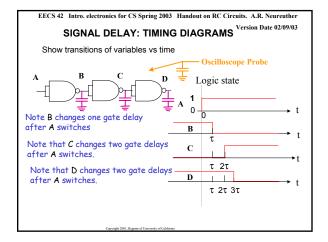
Developed by Professor W.G. Oldham to provide understanding of transient issues in computer logic.

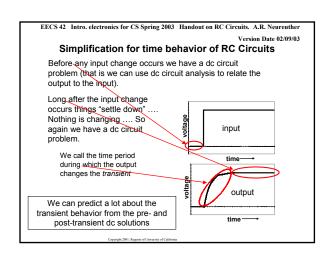
Extensions by Professor A.R. Neureuther in Spring 2003 to include sequential switching of logic gates as occurs in the EECS 43 logic gate experiment.

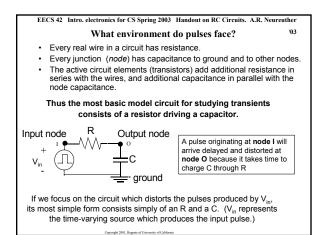
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The RC Circuit to Study

(All single-capacitor circuits reduce to this one)

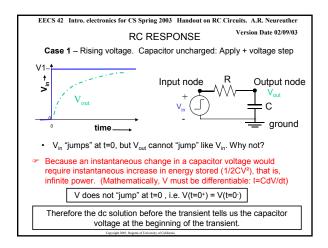
Input node

R Output node

ground

R represents total resistance (wire plus whatever drives the input node)

C represents the total capacitance from node to the outside world (from devices, nearby wires, ground etc)



EECS 42 Intro. electronics for CS Spring 2003 Handout on RC Circuits. A.R. Neureuther RC RESPONSE

Case 1 Continued – Capacitor uncharged: Apply voltage step

Input node

Vout

out

vin

vout

output node

Vout

ground

Vout

Vout

Vout

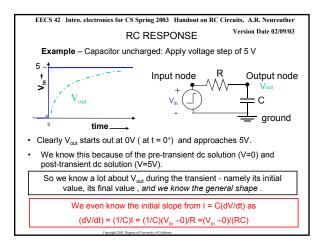
Vout

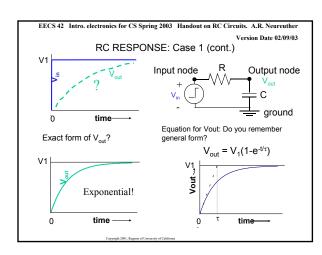
After the transient is over (nothing changing anymore) it means d(V)/dt

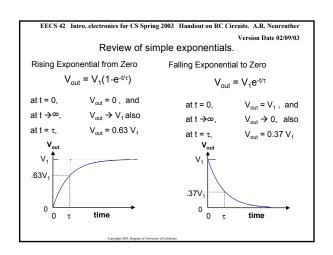
= 0; that is all currents must be zero. From Ohm's law, the voltage across R must be zero, i.e. V_{in} = V_{out}.

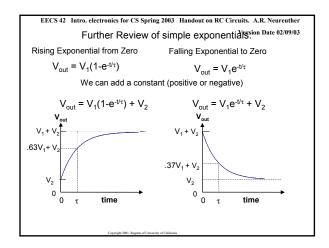
That is, V_{out} → V1 as t → ∞. (Asymptotic behavior)

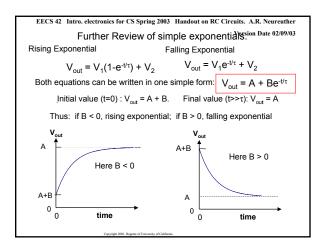
Again the dc solution (after the transient) tells us (the asymptotic limit of) the capacitor voltage during the transient.

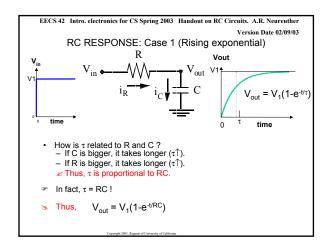


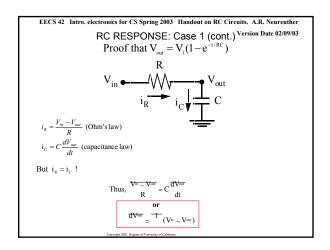


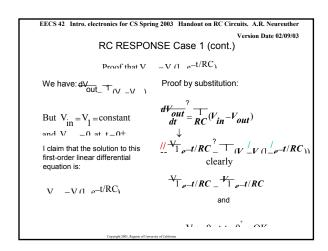


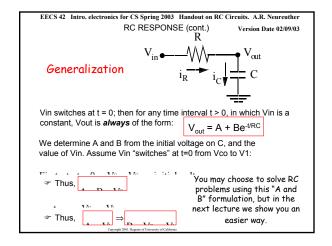




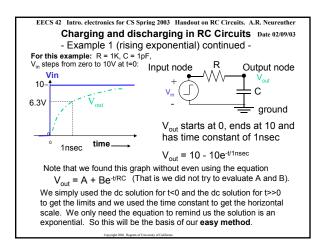




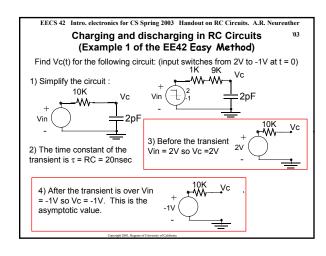




EECS 42 Intro. electronics for CS Spring 2003 Handout on RC Circuits. A.R. Neureuther Version Date 02/09/03 Re-Cap: Charging and discharging in RC Circuits Last Time: Input node Output node We learned that simple the simple RC circuit with a step С input has a universal exponential solution of the form: $V_{out} = A + Be^{-t/RC}$ ground Example 0: R = 1K, C = 1pF, V_{in} steps from zero to 10V at t=0: 10. 1) Initial value of Vout is 0 2) Final value of Vout is 10V 6.3V 3) Time constant is RC = 10-9 sec 4) V_{out} reaches 0.63 X 10 in 10⁻⁹ sec time 1nsec



EECS 42 Intro. electronics for CS Spring 2003 Handout on RC Circuits. A.R. Neureuther Charging and discharging in RC Circuits (The official EE42 Easy Method) Method of solving for any node voltage in a single capacitor circuit. 1) Simplify the circuit so it looks like one resistor, a source, and a capacitor (it will take another two weeks to learn all the tricks to do this.) But then the circuit looks like this: 2) The time constant of the Input node Output node transient is τ = RC. Vout 3) Solve the dc problem for the С capacitor voltage before the transient. This is the starting value (initial value) around for the transient voltage. 4) Solve the dc problem for the capacitor voltage after the transient is over. This is the asymptotic value. 5) Sketch the Transient. It is 63% complete after one time constant. 6) Write the equation by inspection.



EECS 42 Intro. electronics for CS Spring 2003 Handout on RC Circuits. A.R. Neureuther Charging and discharging in RC Circuits (Example 1 of the EE42 Easy Method) Find Vc(t) for the following circuit: (input switches from 2V to -1V at t = 0) 1K 9K Vc We have : Initial value of Vc is 2V, -₩-₩final value is -1V and τ = 20nsec 2pF 5) Sketch Vc (t): What is the equation for an exponential beginning at 2V, Initial value decaying to -1V, with τ = 20nsec? 60 $V_c(t) = -1 + 3e^{-t/20nsec}$ 37% of transient remaining at one time constant

