Problem 1: Logic Warm-up

Identify the Boolean logic function that is equivalent to the operation of each of the following circuits. Please make sure to write your answer clearly in the box on the assignment. The answer in each box will be a standard Boolean operator that is operating on the inputs $A$ and $B$. For example, if the circuit output, $Q$, were to be the NAND($A$, $B$), you should write $\text{NAND}$ in the box.

(a) 

(b) 

A \quad Q

A \quad B \quad Q
(c) 

(d) 

```
A  
B  
Q  
A  
B  
Q  
```
Problem 2: Boolean Algebra

(a) Simplify the following expression: 
\((A + B) + \overline{A}B + A\)

Simplified Expression: 

(b) Simplify the following expression: 
\((A + BC)(A + B)\)

Simplified Expression: 

(c) Simplify the following expression: 
\((\overline{A}B + A)(\overline{A}(\overline{B}) + C)(\overline{B} + AC)\)

Simplified Expression: 

Problem 3: More Boolean Logic

(a) Consider the given circuit. All inputs (A, B, C0, C1, C2, C3) must be either 0 or 1. What must C0, C1, C2, and C3 be such that the circuit computes the function AND(A, B)?

(b) For the following logic circuit, write out the truth table. What is the equivalent Boolean operation of this circuit?

Boolean operator: [Blank Box]
(c) Consider the following truth table. Write out the sum-of-products expression and simplify it, recording your simplified expression in the box at the bottom of the page. Write the name of the useful digital block that the truth table is equivalent to.

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
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<th>Out</th>
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<tbody>
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Simplified Expression: 

Name of block: 
Problem 4. Elementary Verilog

(a) For each of the following Verilog modules, write yes in the box below it if it will compile, or no in the box if it will not compile.

module module_1(
    input a, b,
    output reg out
);
    assign out = a & b;
endmodule

module module_2(
    input a, b,
    output out
);
    always @(*) begin
        assign out = a & b;
    end
endmodule

module module_3(
    input a, b,
    output reg out
);
    always @(*) begin
        out = a | b;
    end
endmodule
(b) Fill in the following blanks in the following snippet of Verilog on the dotted lines (eg. ______________) so that out matches the output of a 2-to-1 mux with inputs a and b, and a select bit, sel, equal to AND(c, d). Each blank should have one word or symbol.

```verilog
defmodule mux2to1(  
  input a, b, c, d,  
  output __________ out  
);  
  __________ sel;  
  __________ sel = c __________ d;  
always @(*) begin  
  if(sel)  
    out __________ a;  
  else  
    out __________ b;  
  end  
endmodule
```