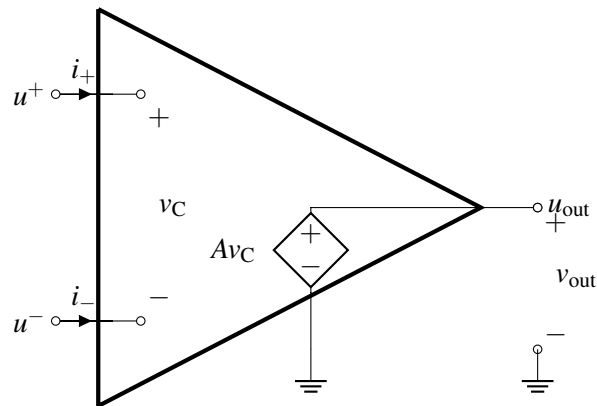


EECS 16A Designing Information Devices and Systems I

Fall 2021 Discussion 10A

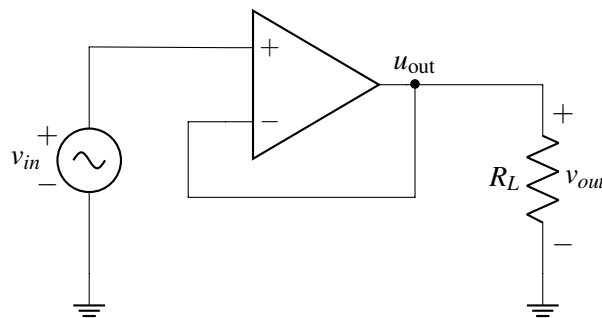
1. Op-Amp Rules

Here is an equivalent circuit of an op-amp (where we are assuming that $V_{SS} = -V_{DD}$) for reference:



- What are the currents flowing into the positive and negative terminals of the op-amp (i.e., what are I^+ and I^-)? Based on this answer, what are some of the advantages of using an op-amp in your circuit designs?
- Suppose we add a resistor of value R_L between u_{out} and ground. What is the value of v_{out} ? Does your answer depend on R_L ? In other words, how does R_L affect Av_C ? What are the implications of this with respect to using op-amps in circuit design?

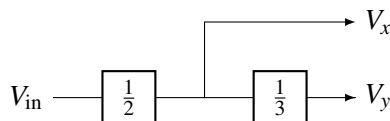
For the rest of the problem, consider the following op-amp circuit in negative feedback:



- Assuming that this is an ideal op-amp, what is v_{out} ?
- Draw the equivalent circuit for this op-amp and calculate v_{out} in terms of A , v_{in} , and R_L for the circuit in negative feedback. Does v_{out} depend on R_L ? What is v_{out} in the limit as $A \rightarrow \infty$?

2. Modular Circuit Buffer

Let's try designing circuits that perform a set of mathematical operations using op-amps. While voltage dividers on their own cannot be combined without altering their behavior, op-amps can preserve their behavior when combined and thus are a perfect tool for modular circuit design. We would like to implement the block diagram shown below:



In other words, create a circuit with two outputs V_x and V_y , where $V_x = \frac{1}{2}V_{in}$ and $V_y = \frac{1}{3}V_x = \frac{1}{6}V_{in}$.

- (a) Draw two voltage dividers, one for each operation (the $1/2$ and $1/3$ scalings). What relationships hold for the resistor values for the $1/2$ divider, and for the resistor values for the $1/3$ divider?

Answer: Recall our voltage divider consists of V_{in} connected to two resistors (R_1, R_2) in series with the output voltage between ground and the central node. This yields the formula

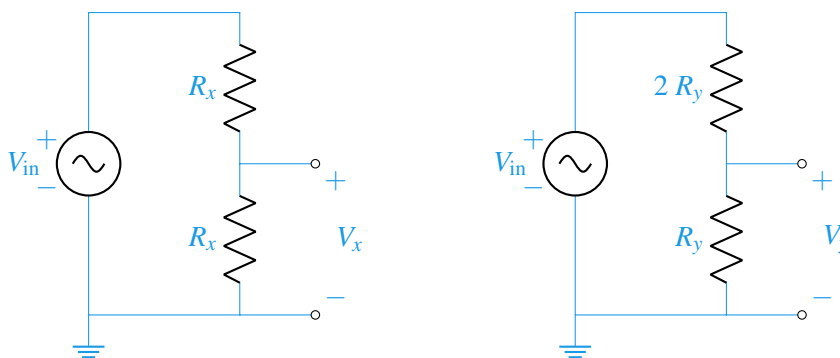
$$V_{out} = \left(\frac{R_2}{R_1 + R_2} \right) V_{in}.$$

For the $1/2$ operation (V_x output) we recognize

$$\frac{1}{2} = \left(\frac{R_2}{R_1 + R_2} \right) \rightarrow R_1 + R_2 = 2R_2 \rightarrow R_1 = R_2 \equiv R_x.$$

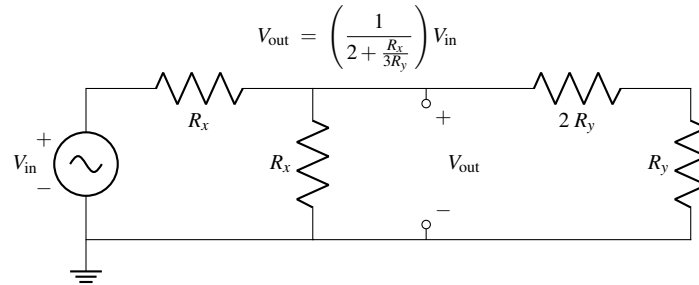
For the $1/3$ operation (V_y output) we recognize

$$\frac{1}{3} = \left(\frac{R_2}{R_1 + R_2} \right) \rightarrow R_1 + R_2 = 3R_2 \rightarrow \frac{R_1}{2} = R_2 \equiv R_y.$$

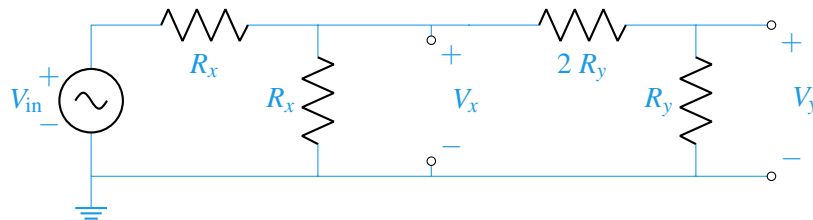


- (b) If you combine the voltage dividers, made in part (a), as shown by the block diagram (output of the $1/2$ voltage divider becomes the source for the $1/3$ voltage divider circuit), do they behave as we hope (meaning $6V_{in} = 3V_x = V_y$)?

HINT: The following circuit and formula may be handy:



Answer: Combining the voltage divider circuits yield



To quickly access this combined system, we may identify V_x as the result of a new equivalent voltage divider (recognizing the R_y resistors in series and that series is in parallel with R_x). The load resistor becomes $R_{eq} = \frac{3R_x R_y}{R_x + 3R_y}$. This yields

$$V_x = \left(\frac{R_{eq}}{R_x + R_{eq}} \right) V_{in} = \left(\frac{1}{2 + \frac{R_x}{3R_y}} \right) V_{in} \quad V_y = \frac{1}{3} V_x = \left(\frac{1}{6 + \frac{R_x}{R_y}} \right) V_{in}$$

From this stage it is evident that combining our dividers changes their behavior (although they preserve behavior in the limit $R_y \gg R_x$).

The new values for V_x, V_y are dependent on values from both dividers, which means they can't be treated independently! □.

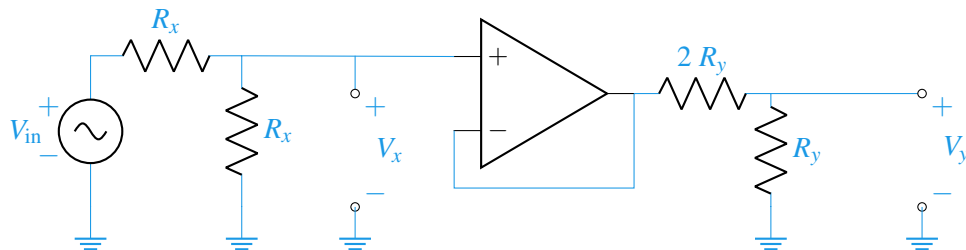
(c) Perhaps we could use an op-amp (in negative-feedback) to achieve our desired behavior.

Modify the implementation you tried in part (b) using a negative feedback op-amp in order to achieve the desired V_x, V_y relations $V_x = (1/2)V_{in}$ and $V_y = (1/3)V_x = (1/6)V_{in}$.

HINT: Place the op-amp in between the dividers such that the V_x node is an input into the op-amp, while the source of the 2nd divider is the output of the op-amp!

Answer: Use the op-amp as a voltage buffer.

This means we short the op-amp's negative input to its output, since the positive input must now match its output (by the golden rules).



Since no current flow into the positive op-amp input, we've successfully isolated the dividers so they can be used in a modular fashion! □

NOTE: The V_x, V_y outputs from this configuration would change with the addition of a load on either terminal. As a follow-up, think about ways to make each output agnostic to the loads attached!