

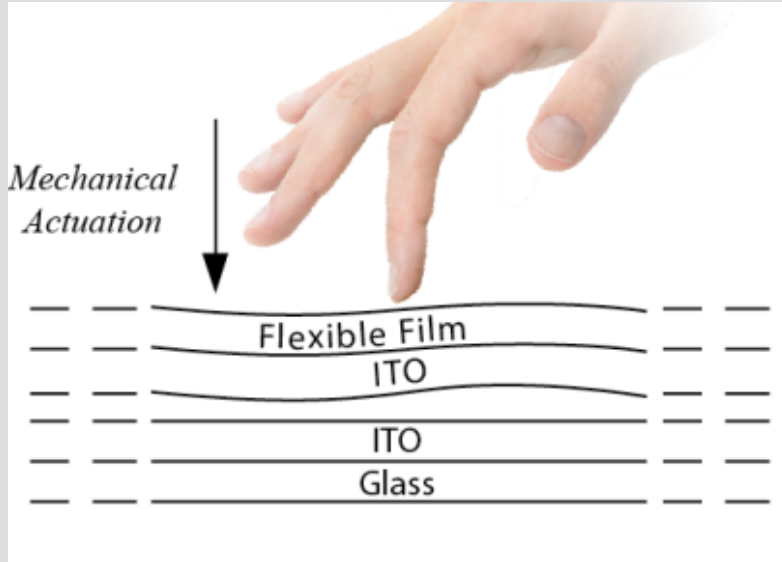
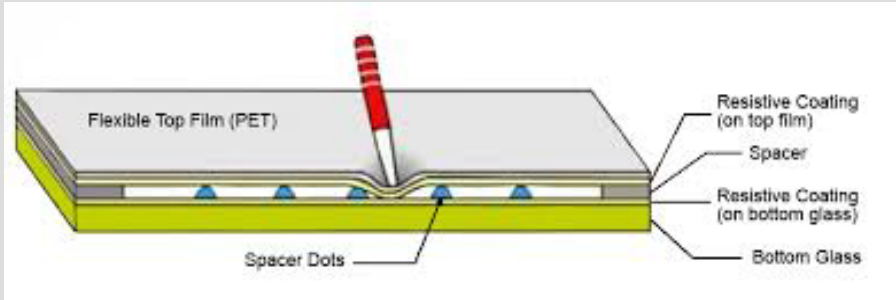
# We **CS 16A!** Designing Information Devices and Systems I

**Ana Claudia Arias and Miki Lustig**  
Fall 2022

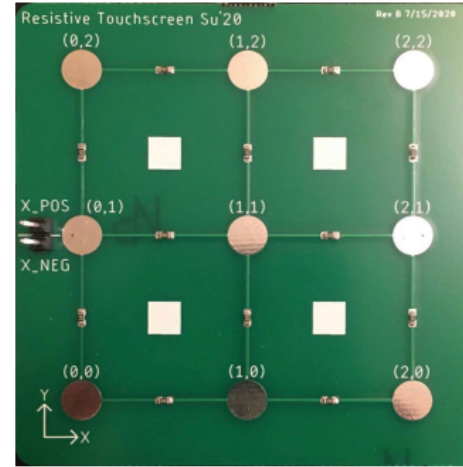
Module 2  
Lecture 4  
2D Touchscreen  
(Note 14)



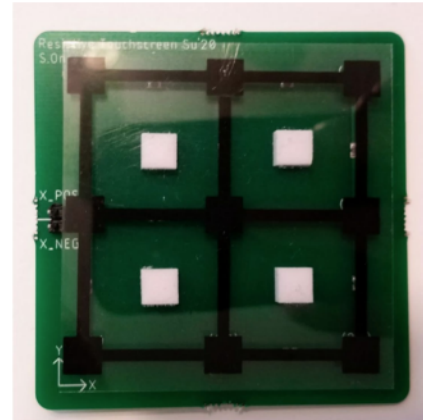
# Resistive Touch Screen



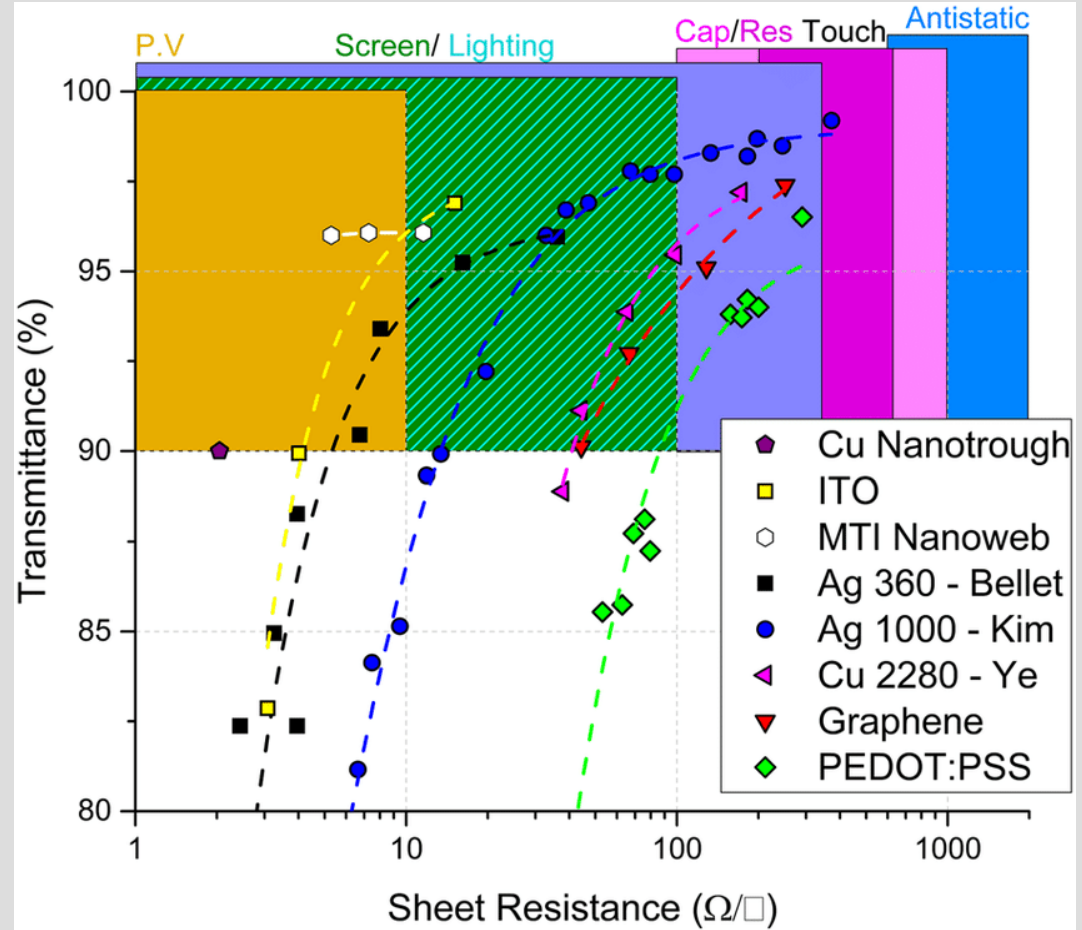
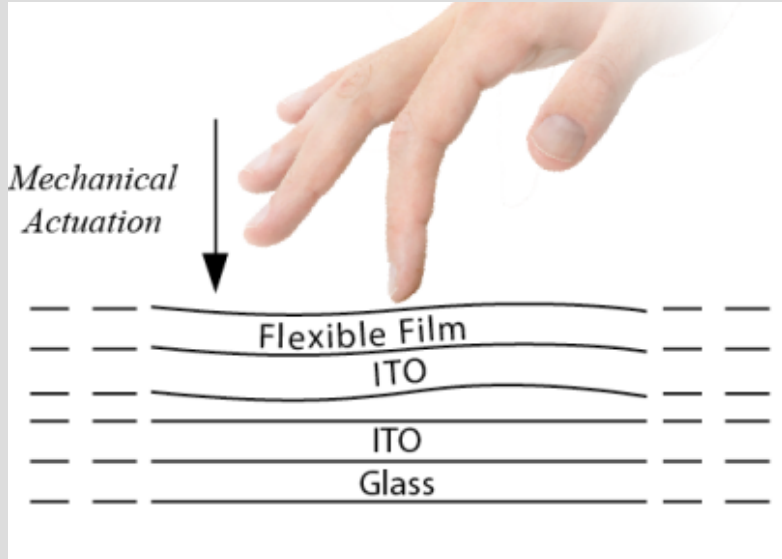
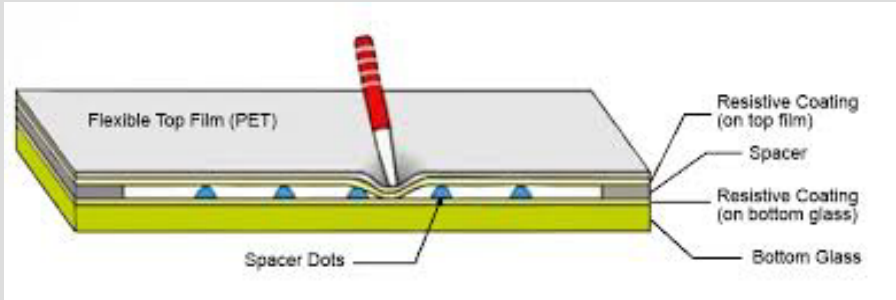
## Bottom Layer: Resistive Layer



## Top Layer: Flexible Resistive Layer

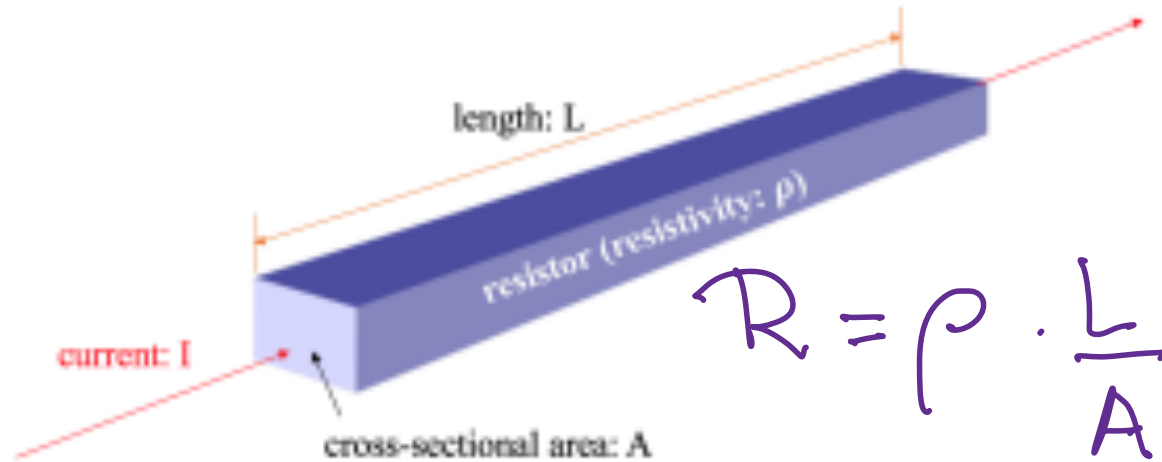


# Resistive Touch Screen



# Resistance, Resistivity, Conductivity – Properties of Materials

Material	Electrical characteristics	
	Electrical Resistivity ( $\Omega \times \text{cm}$ )	Electrical Conductivity ( $\Omega^{-1} \times \text{cm}^{-1}$ )
Cu	$0.034 \times 10^{-5}$	$29 \times 10^5$
Fe	$32.54 \times 10^{-5}$	$0.031 \times 10^5$
Ag	$0.36 \times 10^{-5}$	$2.8 \times 10^5$
Al	$0.03 \times 10^{-5}$	$33.3 \times 10^5$
Ni	$0.046 \times 10^{-5}$	$21.7 \times 10^5$
Cu-Fe	$33.37 \times 10^{-5}$	$0.030 \times 10^5$
Cu-Ag	$2.71 \times 10^{-5}$	$0.37 \times 10^5$
Al-Ni	$0.564 \times 10^{-5}$	$1.77 \times 10^5$



$$R = \rho \cdot \frac{L}{A}$$

Note 12

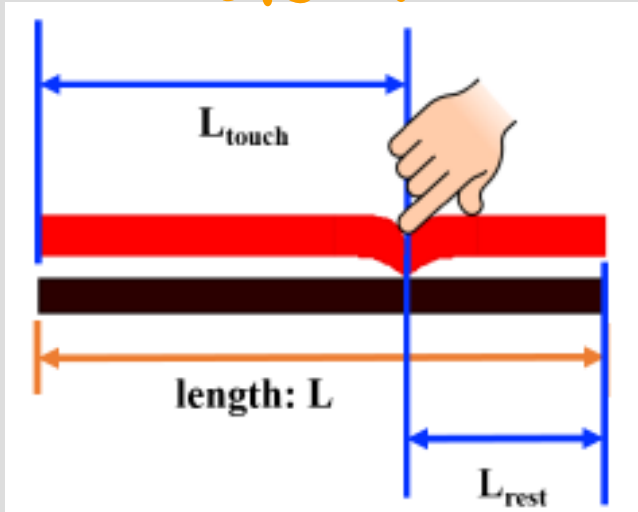
- longer the wire  $\rightarrow$  the more E is lost
- Wide wires  $\rightarrow$  lower resistance
- Wire properties depend on materials choice.

$\rho$  = resistivity  
(property of materials)

$\frac{L}{A}$   $\therefore$  geometric parameters  
(property of the wire)

# Resistive Touch Screen

Problem: to find the location of touch.



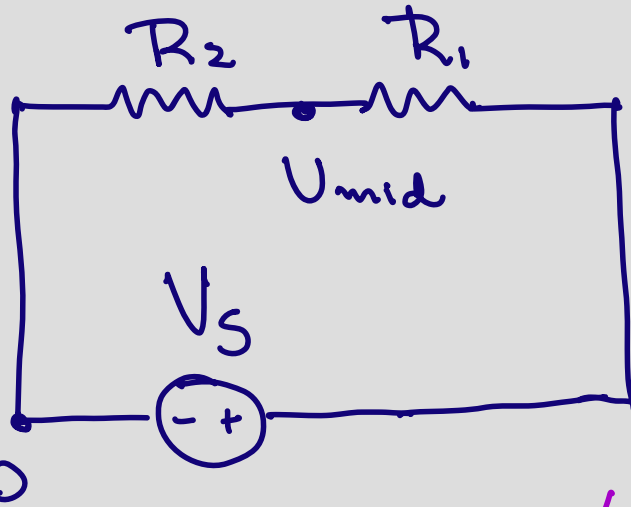
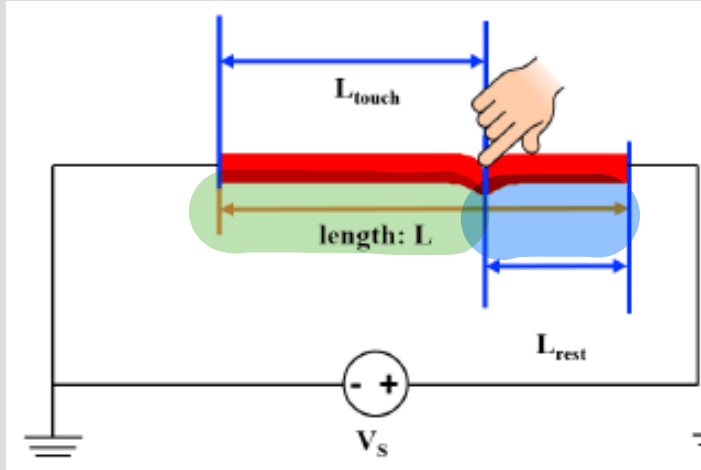
Go from mechanical to electrical quantity.

Want to measure  $\frac{l_{\text{touch}}}{L}$

$l_{\text{touch}}$  is unknown

# Resistive Touch Screen – First model

$U_{mid} \approx ?$



$$U_{mid} = \frac{R_2}{R_2 + R_1} \cdot V_s \quad (\text{Voltage Divider})^*$$

$$R_1 = \rho \cdot \frac{L_{rest}}{A}$$

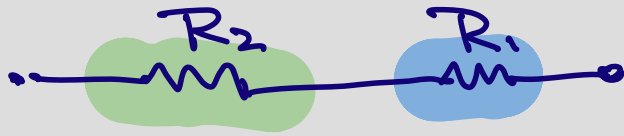
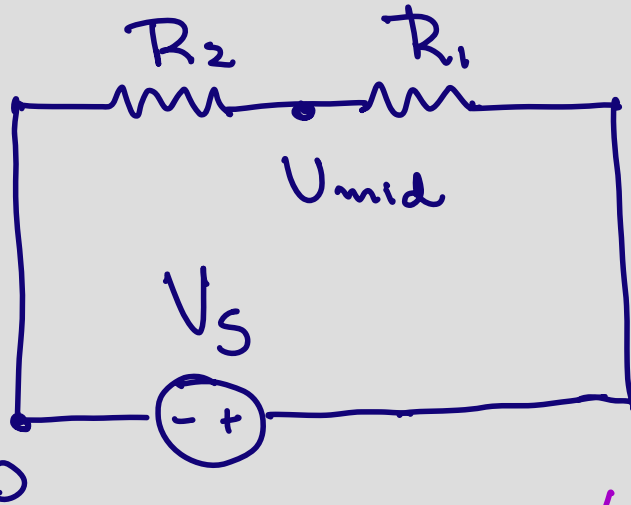
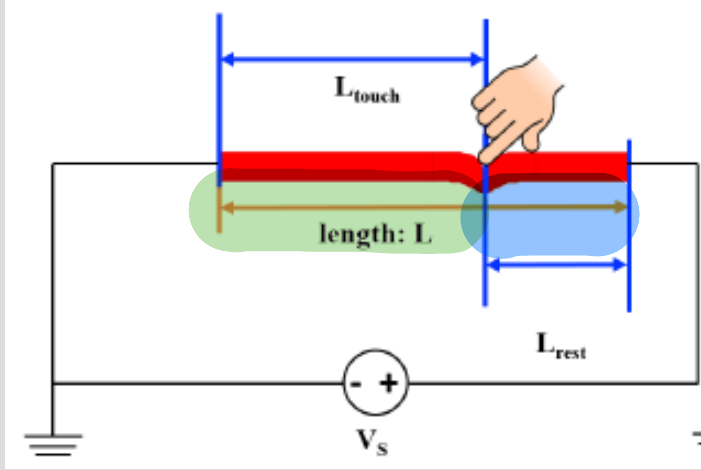
$$U_{mid} = \frac{\cancel{\rho} \cdot L_{touch} / \cancel{A}}{\cancel{\rho} \cdot \frac{L_{touch}}{\cancel{A}} + \cancel{\rho} \cdot \frac{L_{rest}}{\cancel{A}}} \cdot V_s$$

$$R_2 = \rho \cdot \frac{L_{touch}}{A}$$

$$U_{mid} = \frac{L_{touch}}{L_{touch} + L_{rest}} \cdot V_s = \frac{L_{touch}}{L} \cdot V_s$$

# Resistive Touch Screen – First model

$U_{mid} \approx ?$



$$U_{mid} = \frac{R_2}{R_2 + R_1} \cdot V_s \quad (\text{Voltage Divider})^*$$

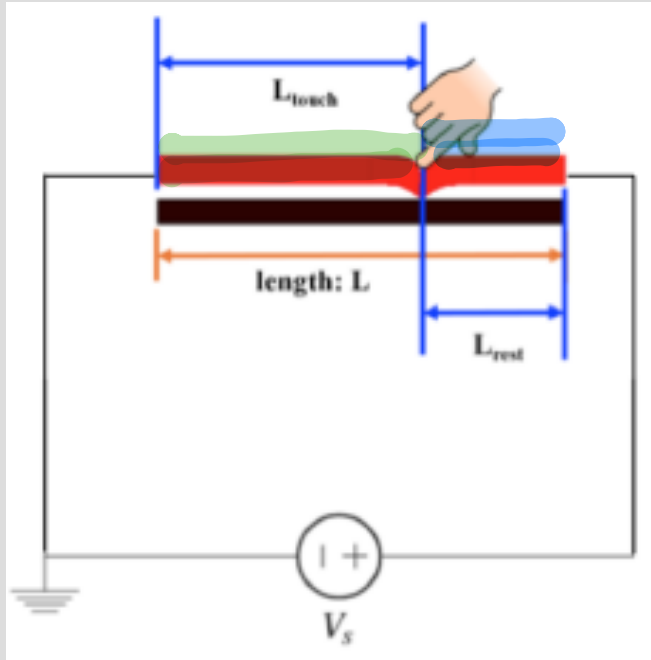
$$R_1 = \rho \cdot \frac{L_{rest}}{A}$$

$$U_{mid} = \frac{\cancel{\rho} \cdot L_{touch} / \cancel{A}}{\cancel{\rho} \cdot L_{touch} / \cancel{A} + \cancel{\rho} \cdot L_{rest} / \cancel{A}} \cdot V_s$$

$$R_2 = \rho \cdot \frac{L_{touch}}{A}$$

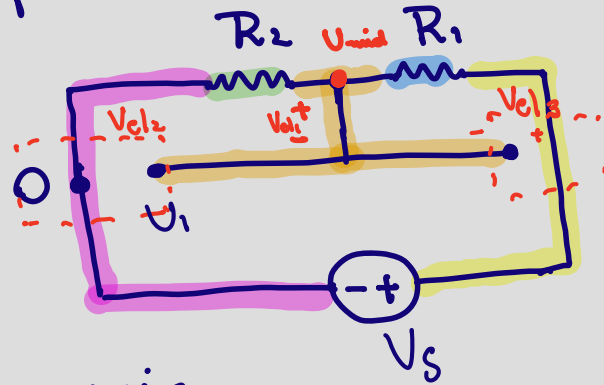
$$U_{mid} = \frac{L_{touch}}{L_{touch} + L_{rest}} \cdot V_s = \frac{L_{touch}}{L} \cdot V_s$$

# Resistive Touch Screen – More realistic model



⇒ Model 1

- Add ideal wire to represent bottom plate



$e_1$  : wire

$e_2$  : open-circuit ( $V_{el_2}$ )

$e_3$  : open-circuit ( $V_{el_3}$ )

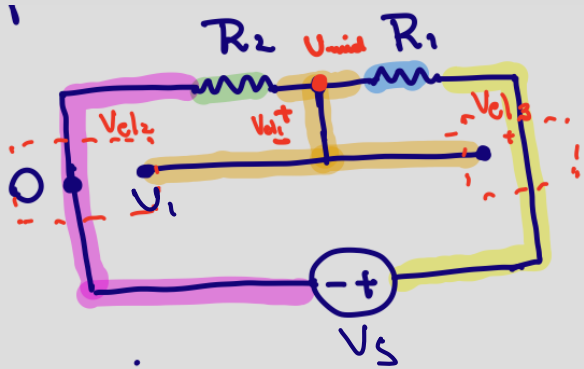
Model 0

$$U_{mid} = \frac{R_2}{R_1 + R_2} \cdot V_s$$

Voltage Divider



# Resistive Touch Screen – More realistic model



$e_1$  : wire

$e_2$  : open-circuit ( $V_{e2}$ )

$e_3$  : open-circuit ( $V_{e3}$ )

Voltage Definition

$$E_2 \therefore V_{e2} = U_1 - 0$$

$$E_1 \therefore V_{e1} = U_{mid} - U_1$$

KVh

$$U_{mid} - 0 = V_{e2} + V_{e1}$$

$$U_{mid} = V_{e2} + V_{e1}^0$$

$$U_{mid} = V_{e1}^0 + U_1$$

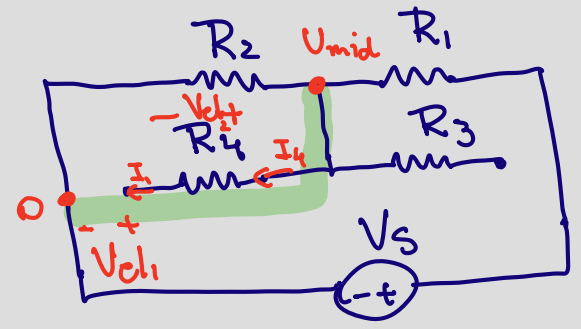
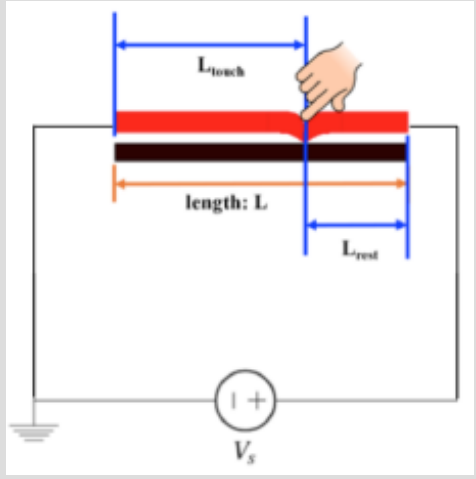
$e_1$  is a wire  $\therefore V_{e1} = 0$

$$U_{mid} = U_1$$

$\hookrightarrow$  By measuring  $V_{e2}$   
We get  $U_{mid}$  for  
any  $\hookrightarrow$  touch

# Resistive Touch Screen – More realistic and better model

Model 2 - imperfect conductor (resistor) (top and bottom plates)



KCL for  $e_{l2}$

$$I_1 = I_4$$

$$I_1 = 0 \therefore I_4 = 0$$

In this model we added:

$e_{l1}$ : open-circuit

$e_{l2}$ : resistor ( $R_4$ )

KVL

$$V_{cl1} + V_{cl2} = U_{mid} - 0$$

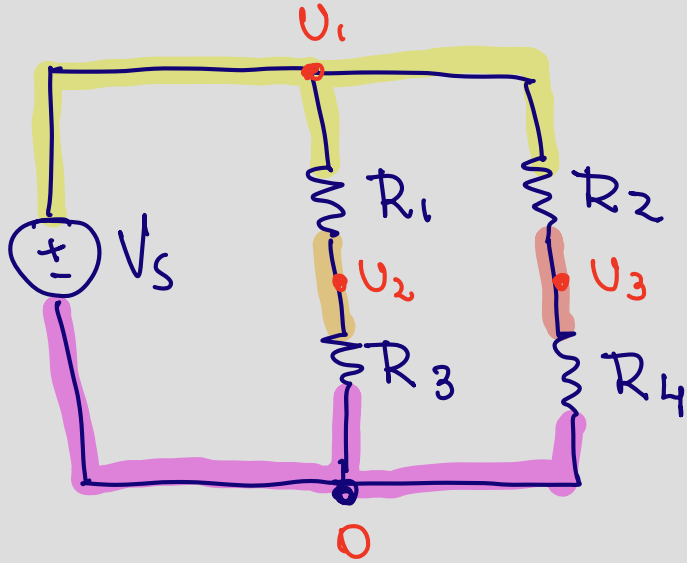
$$V_{cl1} + R_4 \cdot I_4 = U_{mid}$$

$$V_{cl2} = R_4 \cdot I_4 \text{ (Ohm's Law)}$$

$$U_{mid} = V_{cl1}$$

\* By measuring  $V_{cl1}$  we get  $U_{mid}$  for any  $h_{touch}$ ; independent of materials used in bottom lane!

# An interesting circuit



- What are  $U_2$  and  $U_3$ ?

$$U_2 = \frac{R_3}{R_1 + R_3} \cdot V_S$$

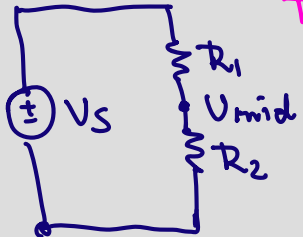
$$U_3 = \frac{R_4}{R_2 + R_4} \cdot V_S$$

$$U_2 - 0 = \frac{R_3}{R_1 + R_3} \cdot (U_1 - 0) \quad V_S$$

$$U_3 - 0 = \frac{R_4}{R_2 + R_4} \cdot (U_1 - 0) \quad V_S$$

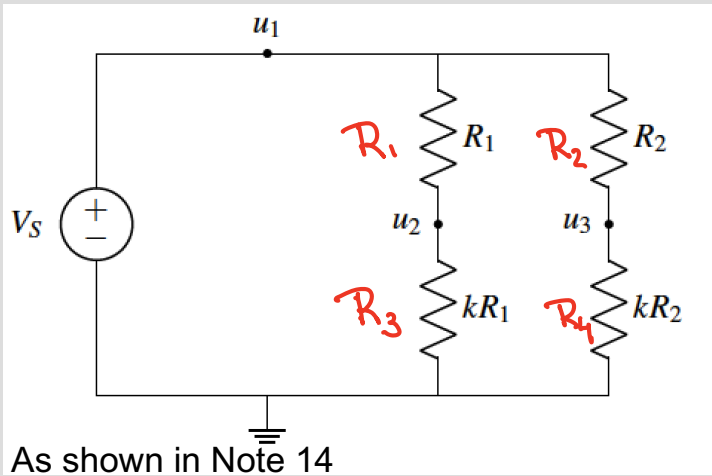
$$U_1 - 0 = V_S$$

Tool box



$$U_{mid} = \frac{R_2}{R_1 + R_2} \cdot V_S$$

# An interesting circuit



Power supply keeps  $U$  in wires equal to  $V_S$  regardless of how many branches we have!

$$U_2 = \frac{R_3}{R_1 + R_3} \cdot V_S$$

$$U_3 = \frac{R_4}{R_2 + R_4} \cdot V_S$$

$$U_2 = \frac{kR_1}{R_1 + kR_1} \cdot V_S \quad \therefore U_2 = \frac{k}{1+k} V_S$$

$$U_3 = \frac{kR_2}{R_2 + kR_2} \cdot V_S \quad \therefore U_3 = \frac{k}{1+k} V_S$$

$$U_2 = U_3$$

Wow!

# Let's add on more resistor



Elem<sub>5</sub> = resistor ( $R_5$ )

V<sub>els</sub> =  $U_2 - U_3$  (Voltage Def.)

**Bold Assumption**

$$V_{els} = 0$$

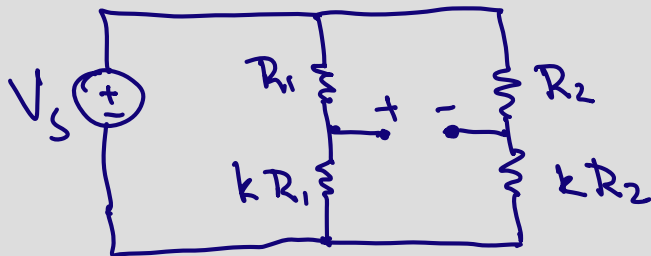
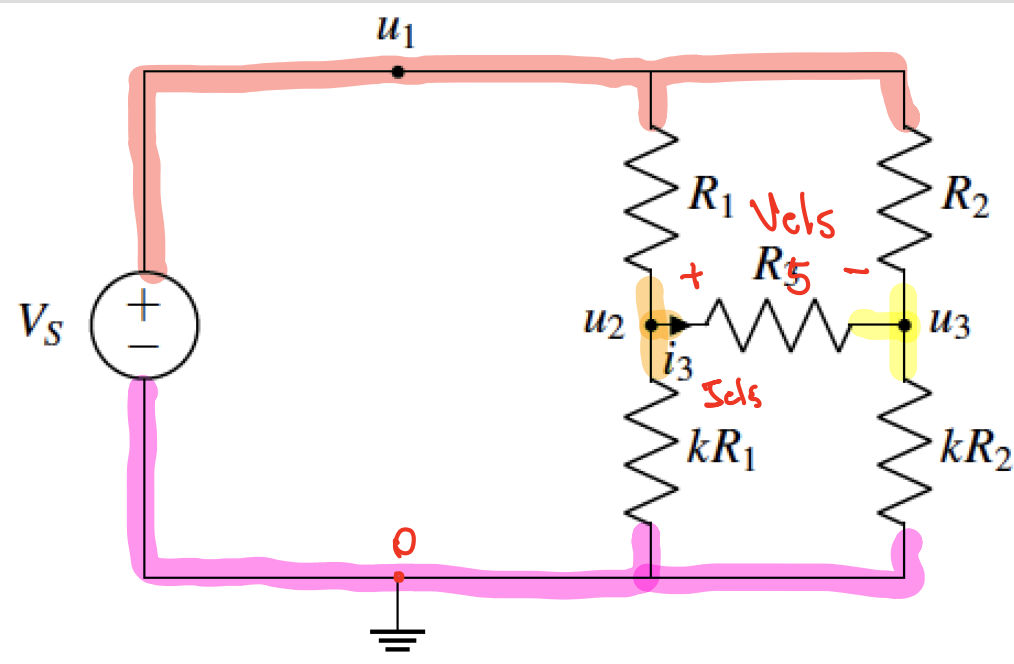
if  $V_{els} = 0 \Rightarrow I_{els} = \frac{V_{els}}{R_5} = 0$

if  $I_{els} = 0$

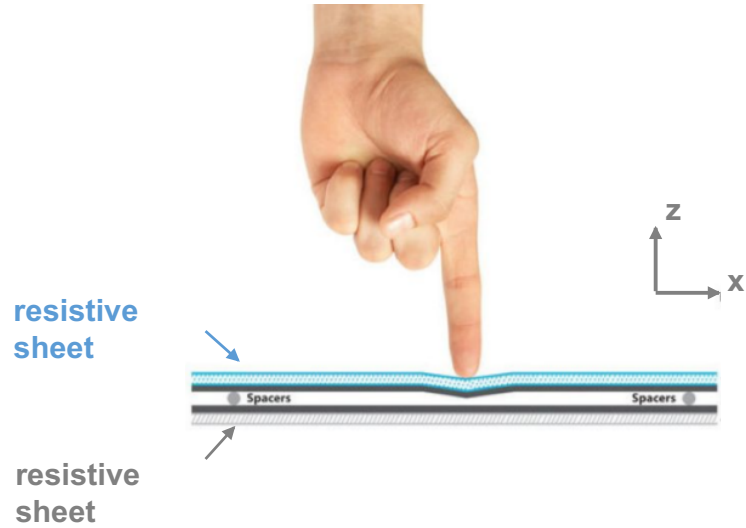
The circuit is the same as the one we already analysed without  $R_5$ .

We showed :  $U_2 = U_3$

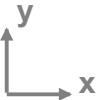
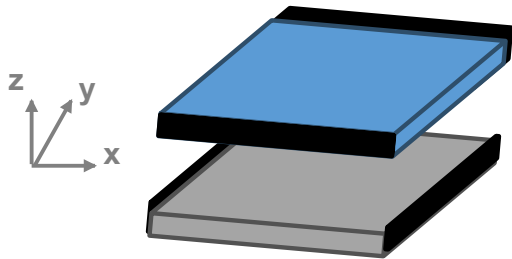
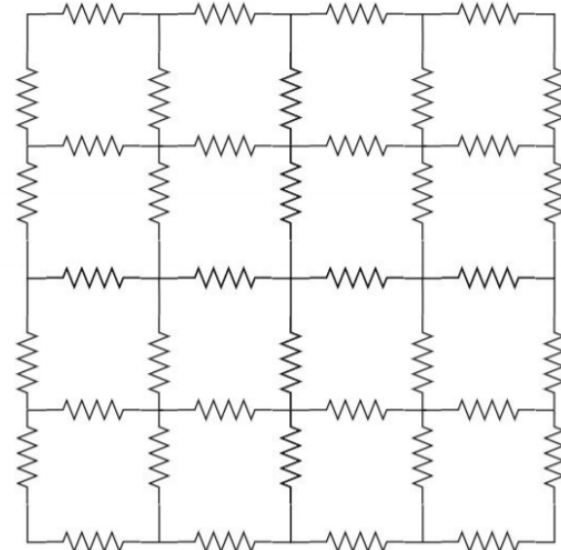
$$V_{els} = U_2 - U_3 = 0$$



# 2D resistive Touchscreen circuit model

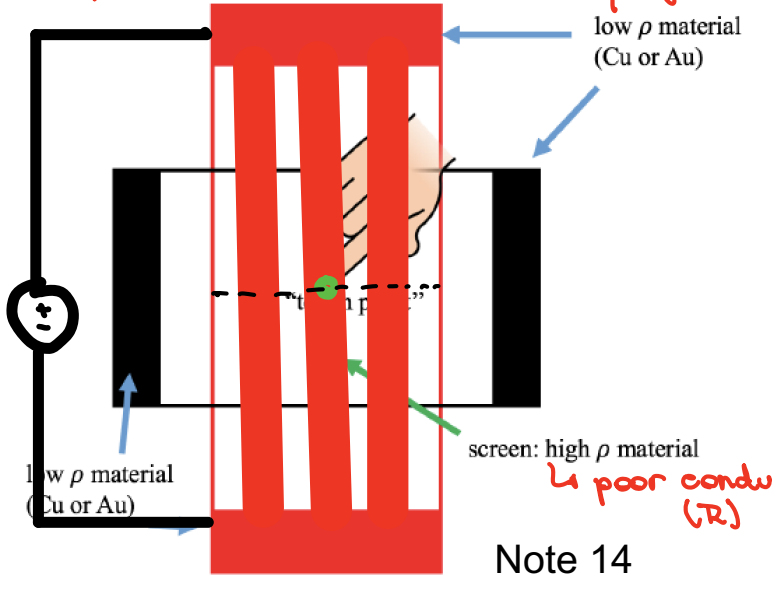


Our circuit model for each resistive sheet is a grid of resistors:



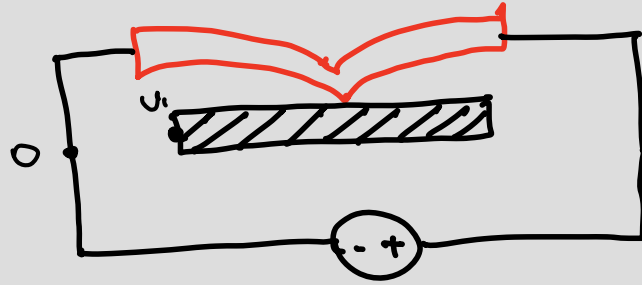
# 2D Touch Screen

Top View



(wire)  
good conductor

poor conductor (R)

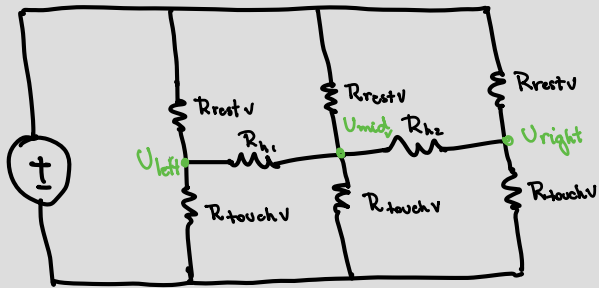


This is our interesting circuit

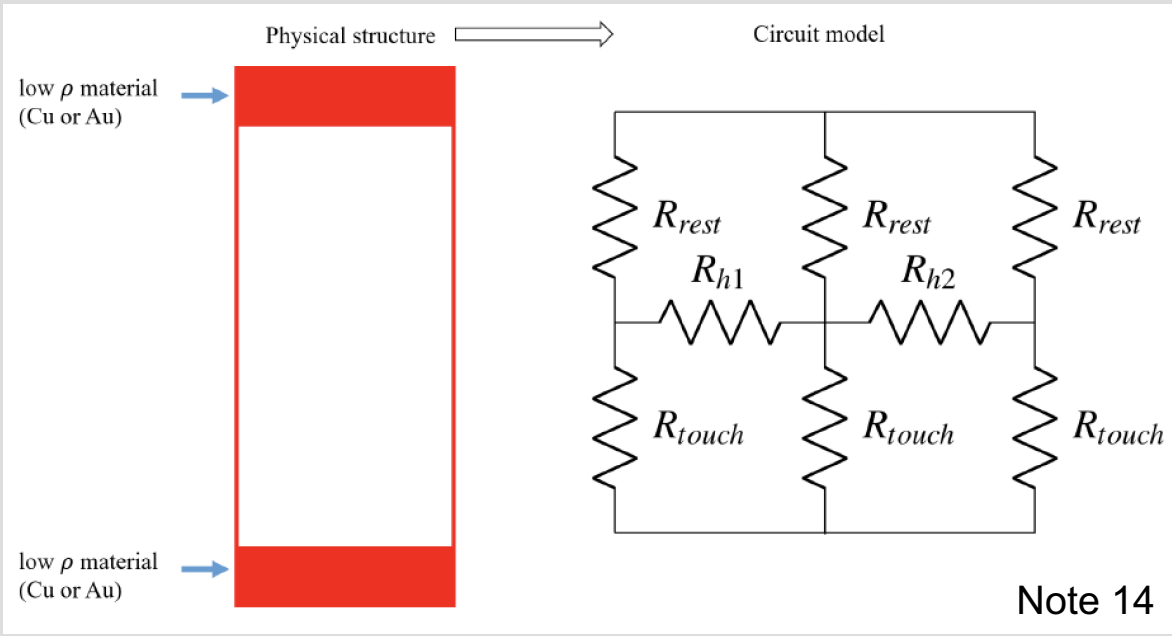
$$U_{mid} = U_{left} = U_{right}$$

$$U_{mid} = \frac{R_{touch}}{R_{rest} + R_{touch}} \cdot V_s$$

$$U_{mid} = \frac{\rho \frac{l_{touch}}{A}}{\rho \frac{l_{rest}}{A} + \rho \frac{l_{touch}}{A}} \cdot V_s$$



# Top Plate Model



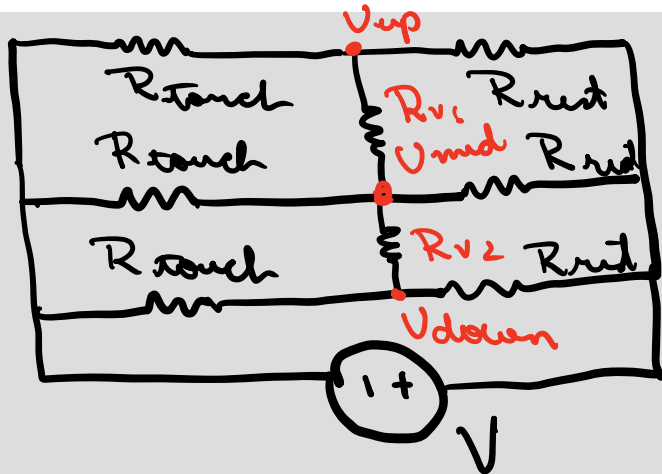
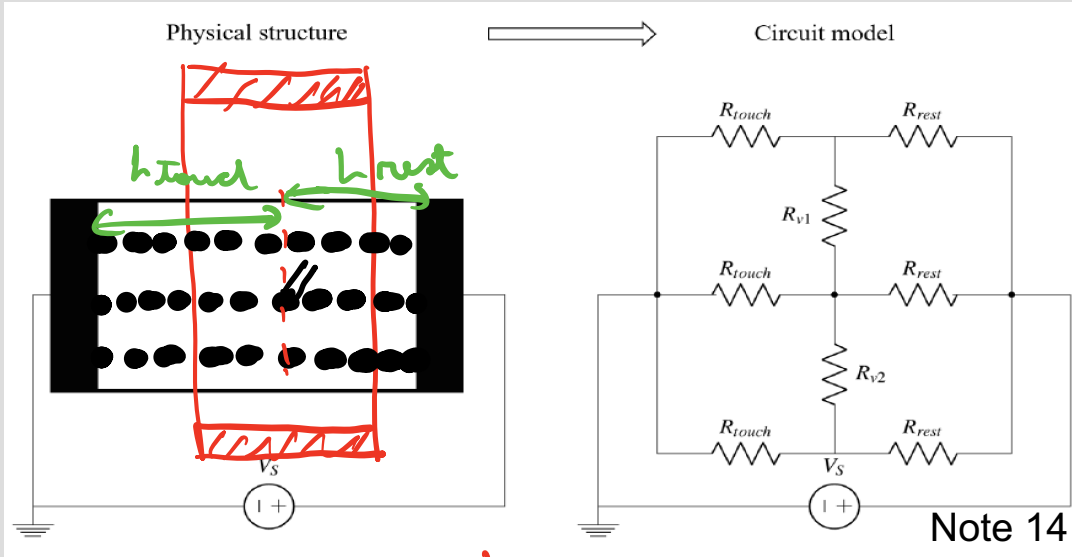
$$U_{midv} = \frac{l_{touch}}{L_{rest} + l_{touch}} \cdot V_s$$

\* This gives us the vertical position in the screen.

What is the next step in the model?



# Bottom Plate Model



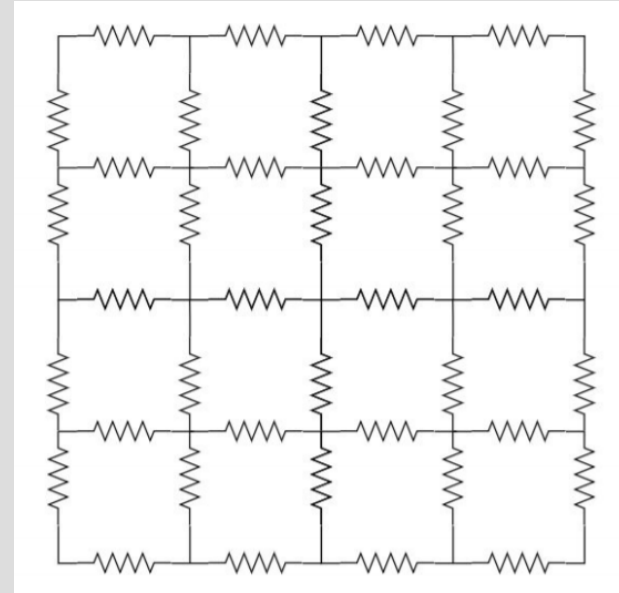
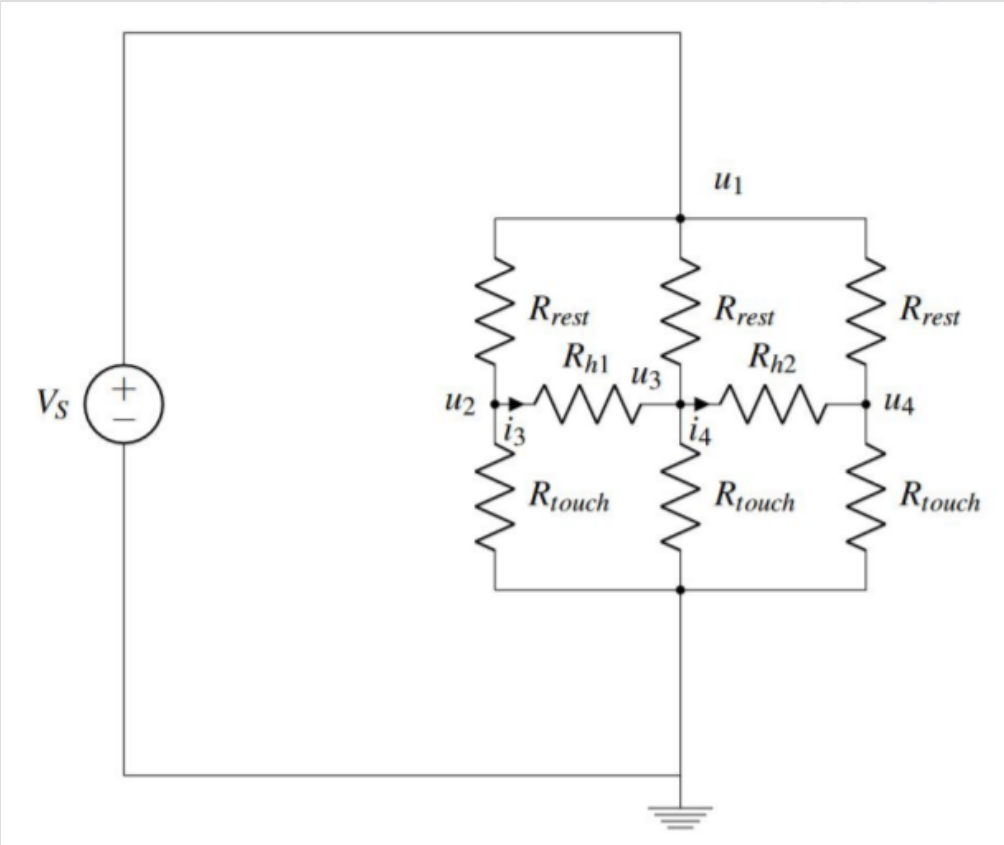
$$V_{up} = V_{mid} = V_{down}$$

$$V_{mid} \neq \frac{R_{touch_{t1}}}{R_{rest_{t1}} + R_{touch}} \cdot V_s$$

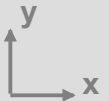
$$V_{mid} = \frac{h_{touch_{t1}}}{h_n} \cdot V_s$$

Horizontal information

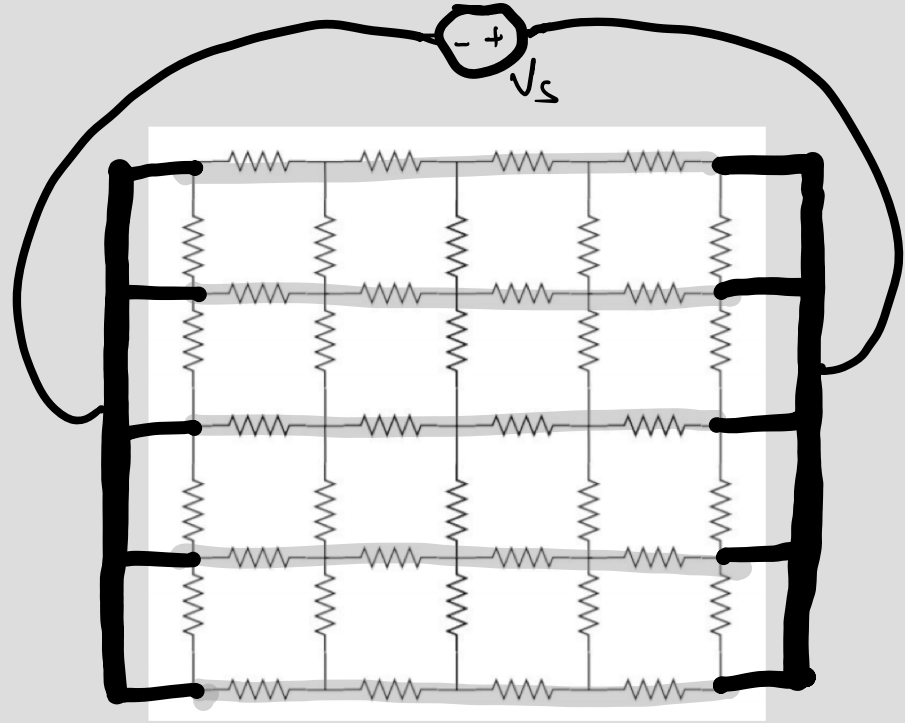
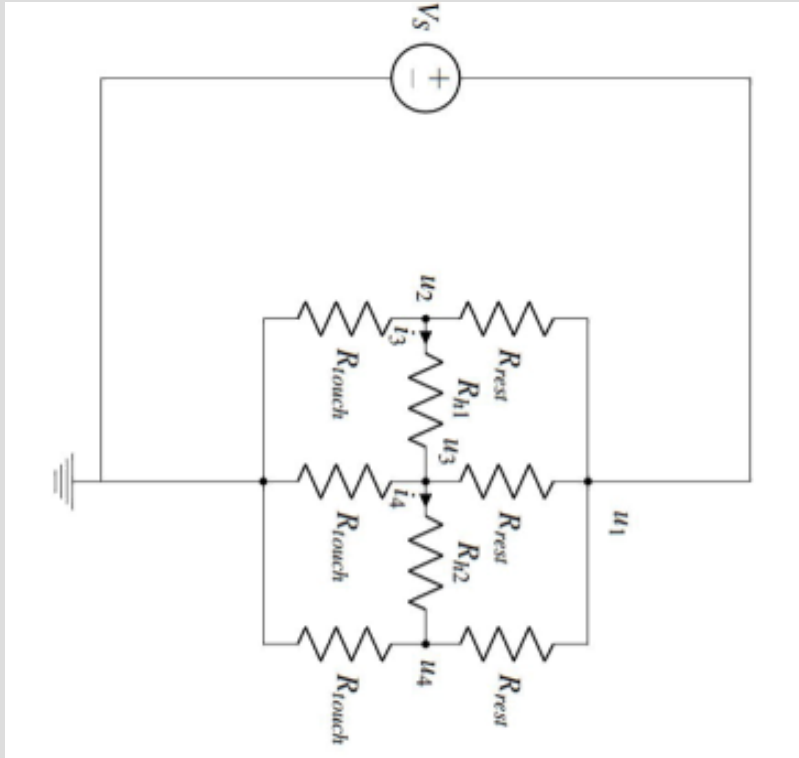
Connecting voltage source to top sheet gives *y-touch* position



$$U_{mid} = \frac{h_{touch}}{h_v} \cdot V_S$$



# Connecting voltage source to bottom sheet gives *x-touch* position



$$V_{mid} = \frac{h_{touch}}{h_H} \cdot V_S$$

