

# Welcome to EECS 16A!

## Designing Information Devices and Systems I

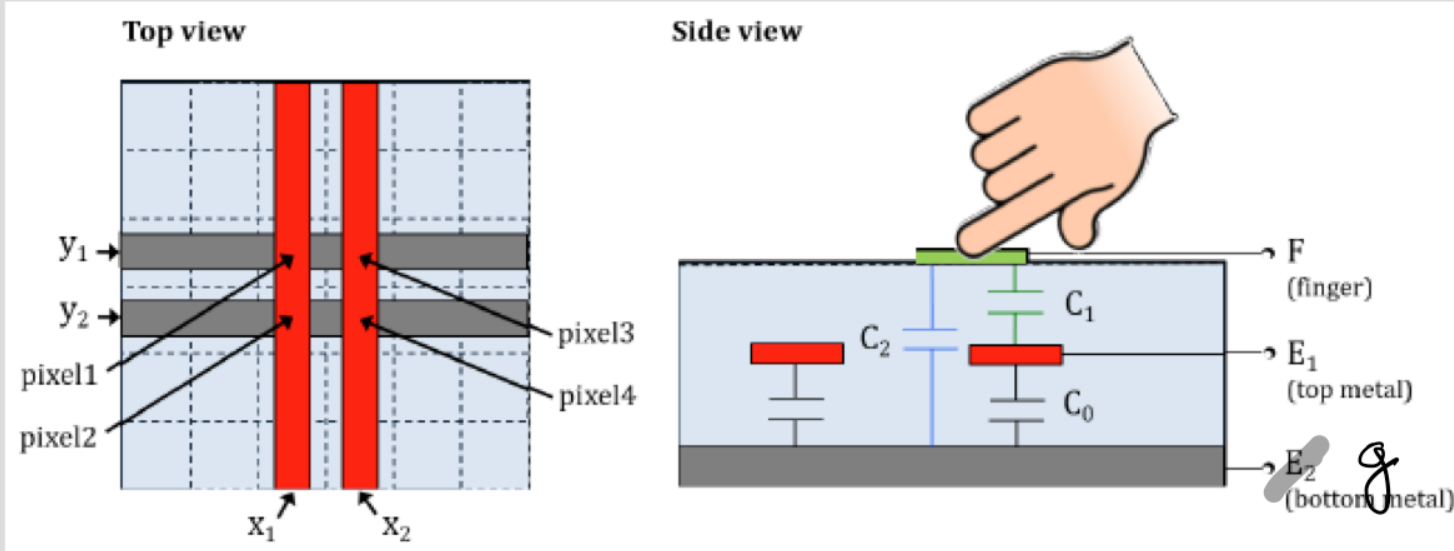
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Fall 2022

Module 2  
Lecture 9

Capacitance Modeling and Comparator  
(Note 18)

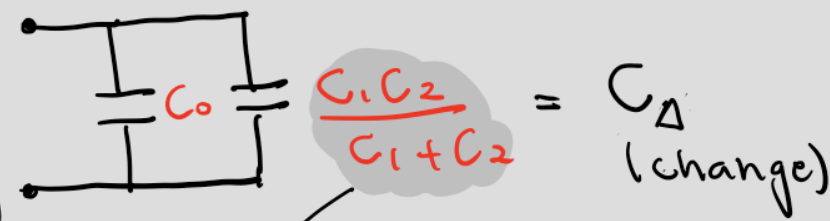


# Last Class...



Problem: We don't have a capacitance meter!

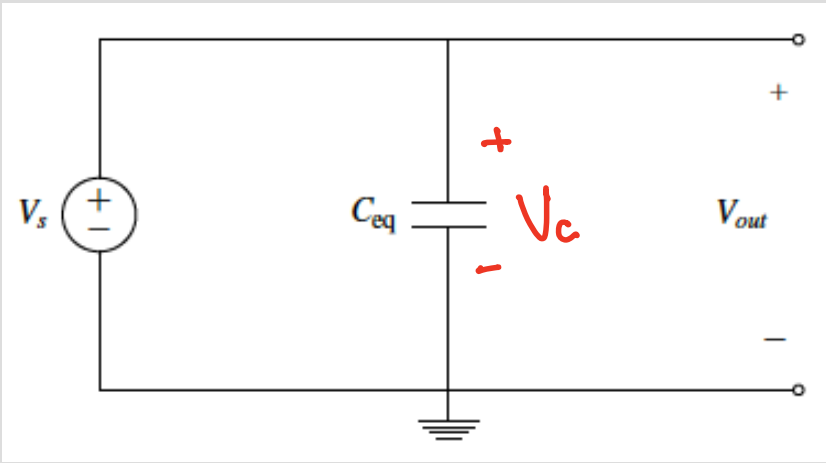
We want to measure capacitance here



This capacitor goes away with no touch

We will try ideas to get to a final model.

# Measuring Capacitance Models – Attempt #1: Add power sources

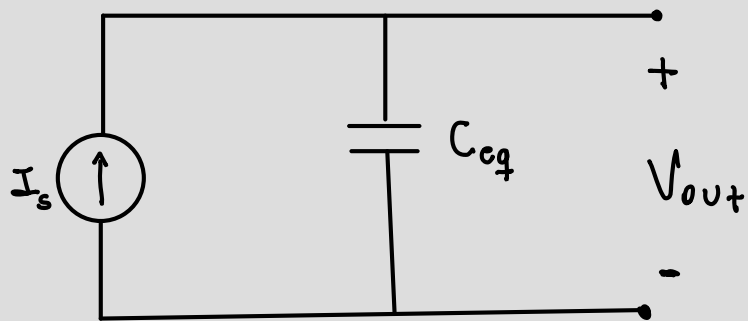


If there is touch:  $V_c = V_s$

If there is no-touch:  $V_c = V_s$

$V_{out}$  does not change!

Need a better idea...



Assume  $C_{eq}$  starts out discharged

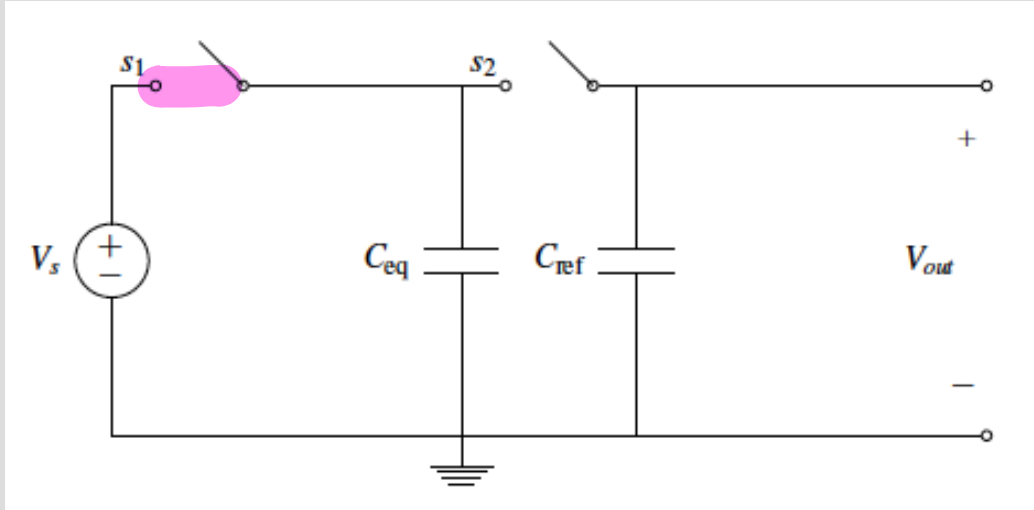
$$V_{out}(t=0) = 0$$

$$I_s = C_{eq} \frac{dV_{out}(t)}{dt} \rightarrow V_{out}(t) = \int_0^t \frac{I_s}{C_{eq}} dt$$

$$V_{out} = \frac{I_s \cdot t}{C_{eq}} \Rightarrow C_{eq} = \frac{I_s \cdot t}{V_{out}}$$

We will learn how to design current sources in EE140

# Measuring Capacitance Models – Attempt #2 – add switches and a reference capacitor



If  $S_1$  and  $S_2$  are both closed – we have attempt #1

We want to charge  $C_{ref}$  and measure  $V_{out}$  as  $C_{ref}$  discharges.

## Phase 1

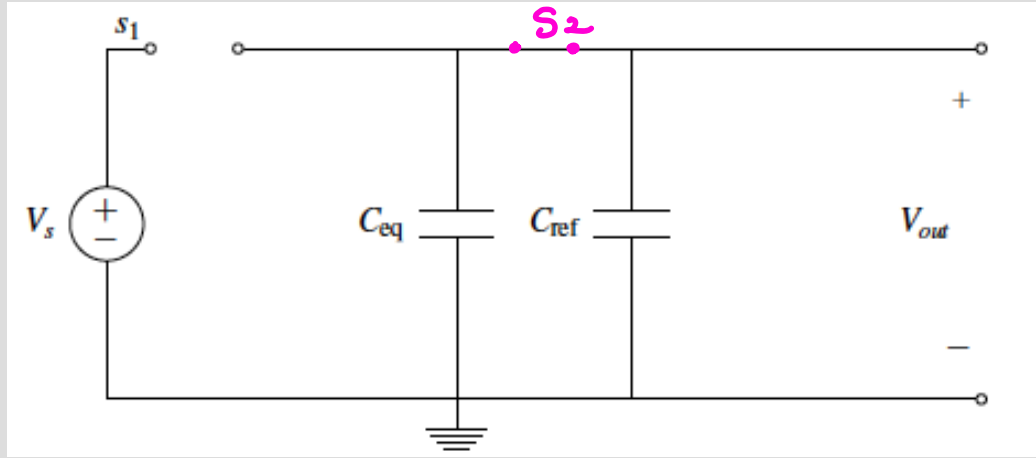
Close  $S_1$  ; Open  $S_2$

$C_{eq}$  charges

$$q = C_{eq} \cdot V_s$$

(charge accumulates on capacitor plates)

# Measuring Capacitance Models – Attempt #2 – add switches and a reference capacitor



Charge will be shared between  $C_{eq}$  and  $C_{ref}$  ∴ charge sharing

Very close!

But... we don't know the initial value of  $C_{ref}$

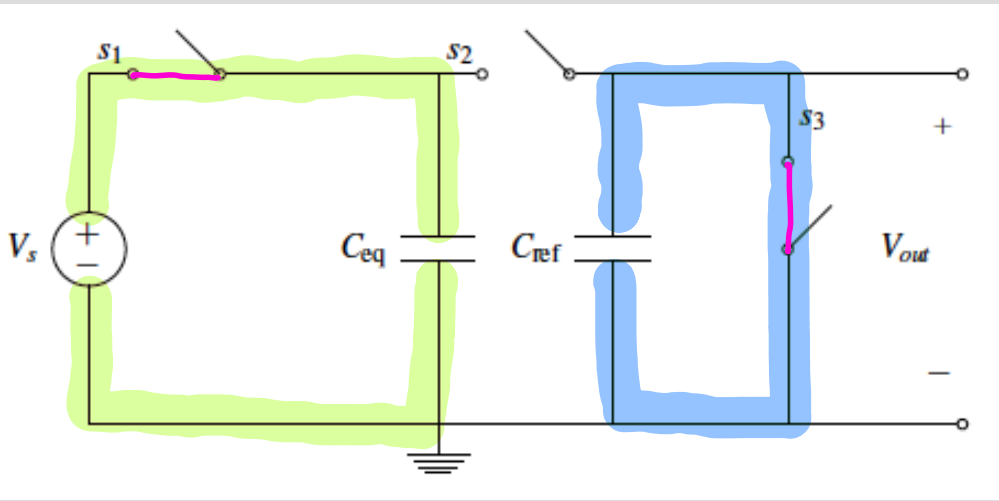
## Phase 2

Close  $S_2$  ; Open  $S_1$

- There is a path for charge to move.
- $C_{eq}$  provides the energy needed for current.

# Measuring Capacitance Models – Attempt #3 – known initial condition

Use  $S_3$  to discharge  $C_{ref}$  so we know  $C_{ref} = 0$



## Phase 1

$S_1$  closed,  $S_2$  open,  $S_3$  closed

$C_{ref}$  discharges  $V_{out} \rightarrow 0$

$$q = C_{ref} \cdot V_{out} = 0 \quad \checkmark$$

$C_{eq}$  charges

$$q = C_{eq} \cdot V_s$$

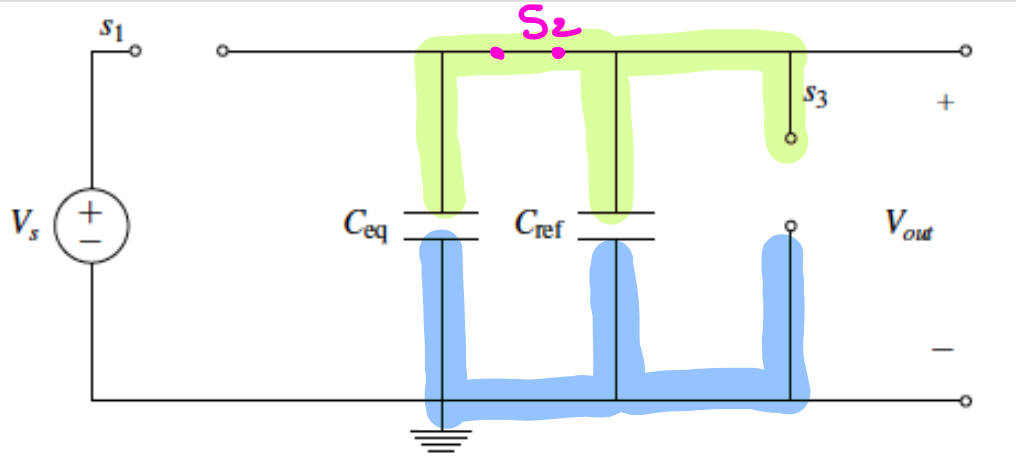
## Phase 2

$S_1$  open,  $S_2$  closed,  $S_3$  open

$C_{eq}$ : charged

$C_{ref}$ : discharged

# Measuring Capacitance Models – Attempt #3 – known initial condition



Voltage across  $C_{eq}$  :  $V_{out}$   
Voltage across  $C_{ref}$  :  $V_{out}$   
Charge in  $C_{eq}$  :  $q_1 = C_{eq} \cdot V_{out}$   
Charge in  $C_{ref}$  :  $q_2 = C_{ref} \cdot V_{out}$

Total charge is conserved!

$$q(\text{phase1}) = q(\text{phase2})$$

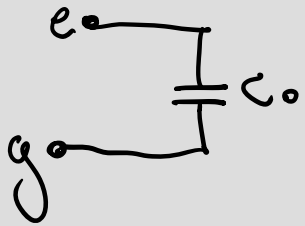
$$C_{eq} \cdot V_s = C_{eq} \cdot V_{out} + C_{ref} \cdot V_{out}$$

$$V_{out} = \frac{C_{eq} V_s}{C_{eq} + C_{ref}}$$

$\Rightarrow$   $V_{out}$  changes when  $C_{eq}$  changes!  
😊

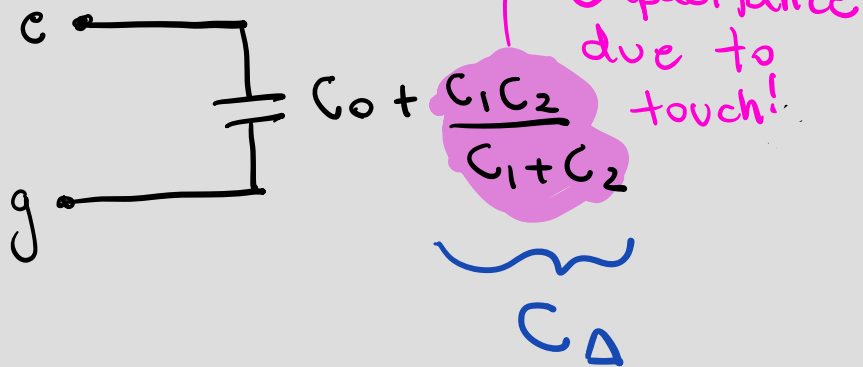
# Effect of touch on total capacitance

when no touch:



$$\Rightarrow V_{OUT} = \frac{C_0}{C_0 + C_{ref}} \cdot V_S$$

with touch:

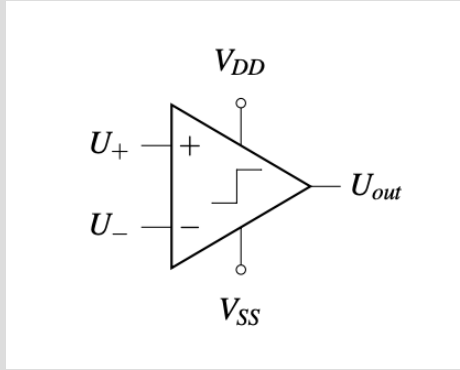


$$\Rightarrow V_{OUT} = \frac{(C_0 + C_\Delta)}{C_0 + C_\Delta + C_{ref}} \cdot V_S$$





# How can we go from voltage measurement to binary answer: touch or no touch?



- We need to choose a Voltage that we call : Threshold Voltage ( $V_{th}$ )

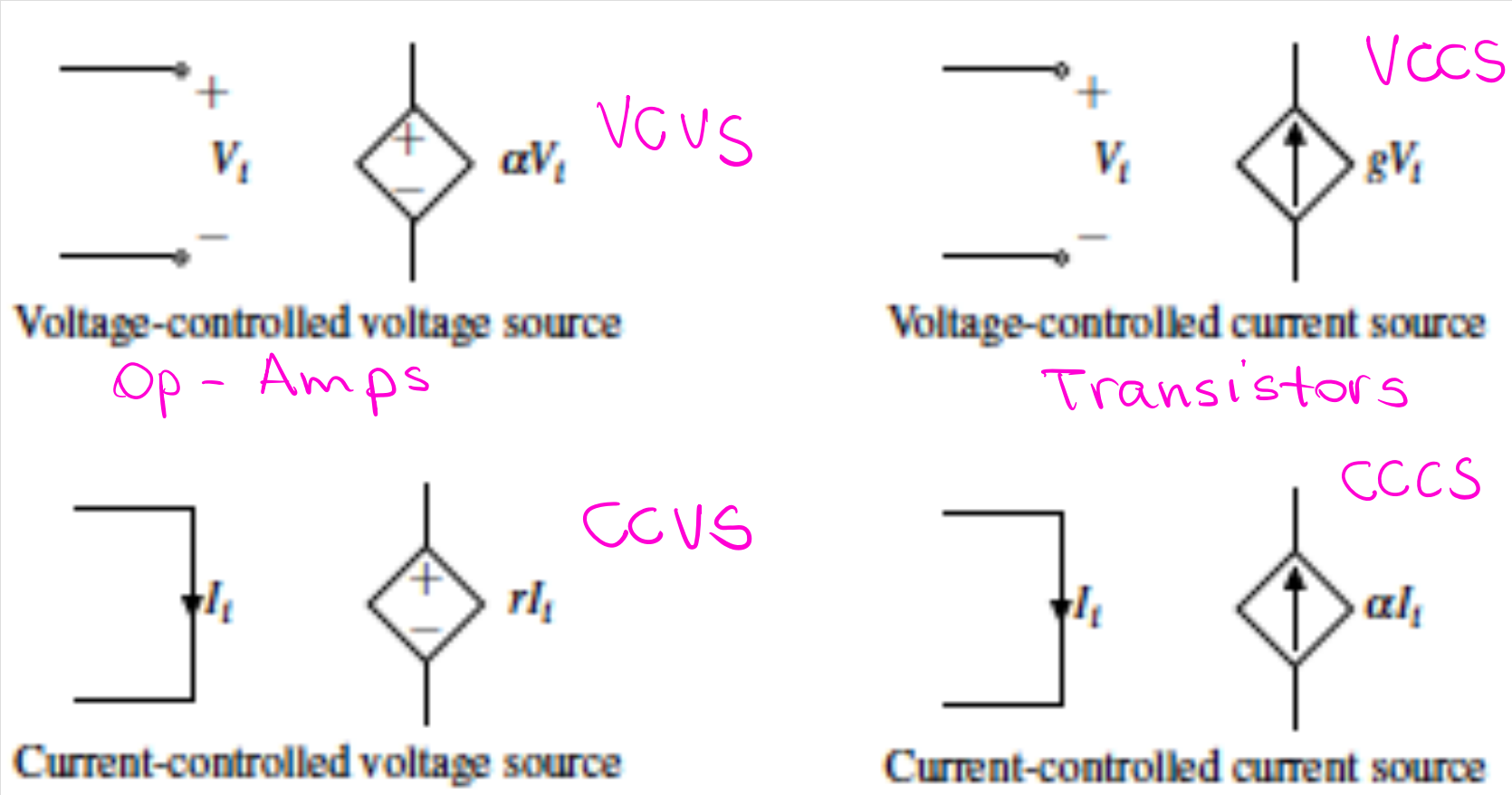
- Above  $V_{th}$  : 1 (touch)

- Below  $V_{th}$  : 0 (no-touch)

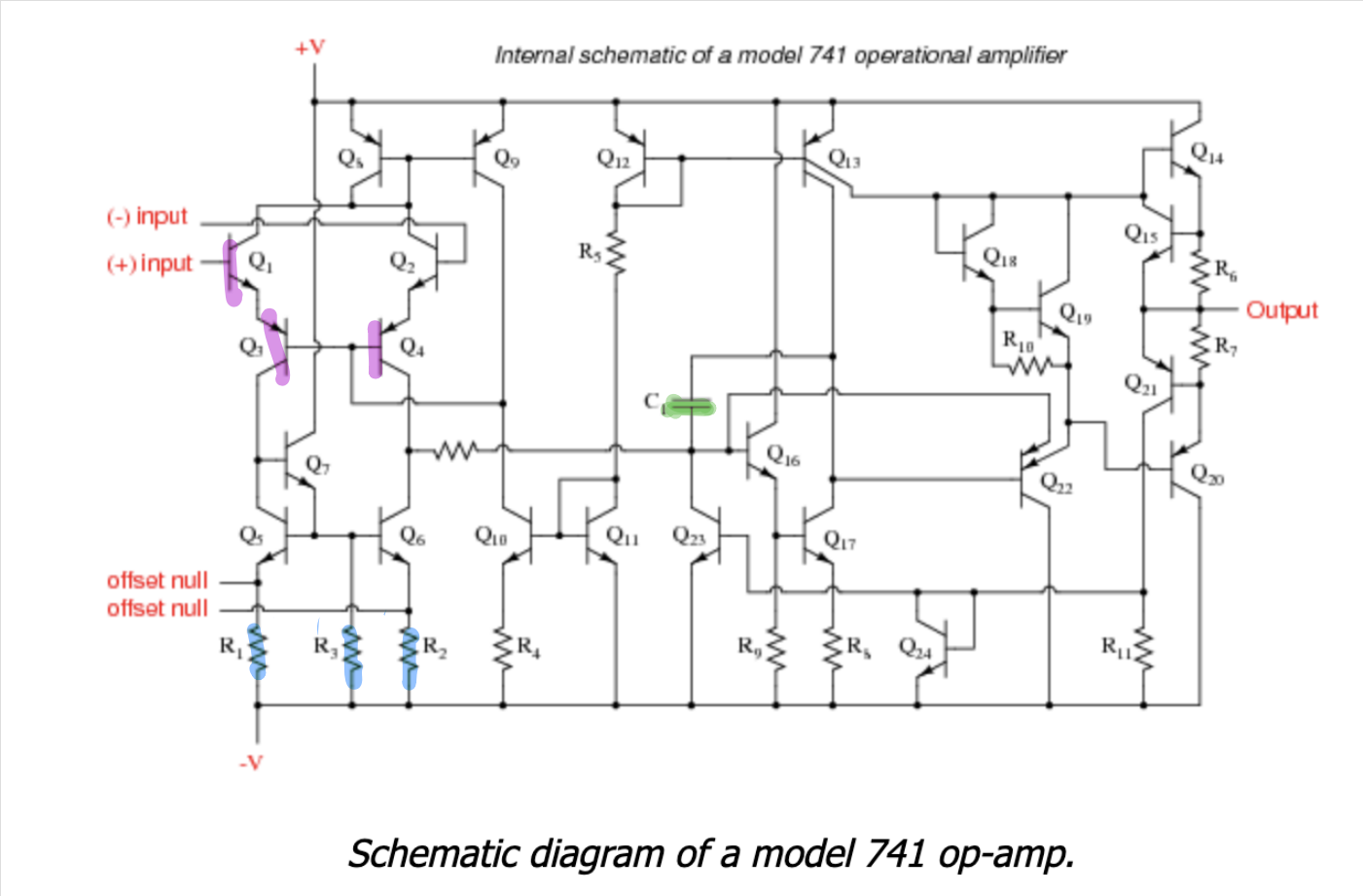
We need to compare Voltages to determine if 1 or 0

# How can we go from voltage measurement to binary answer: touch or no touch?

- New tools are needed – new circuit elements



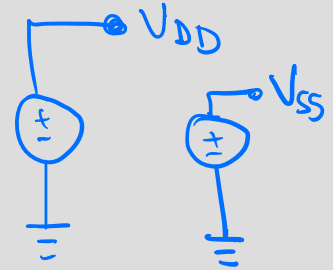
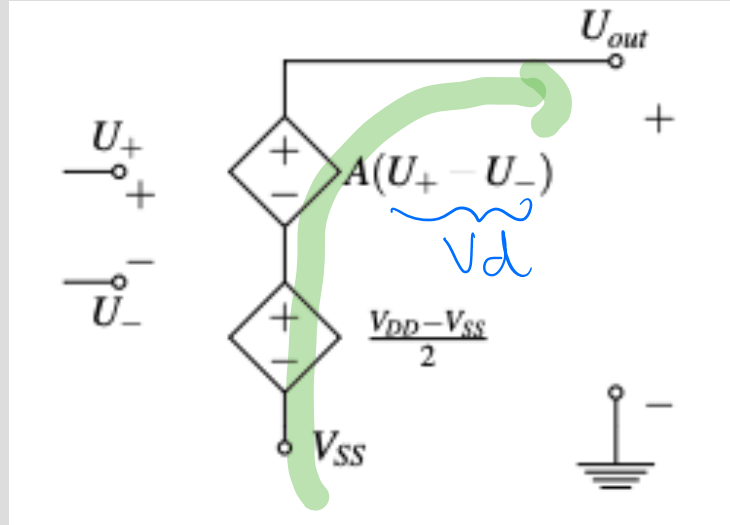
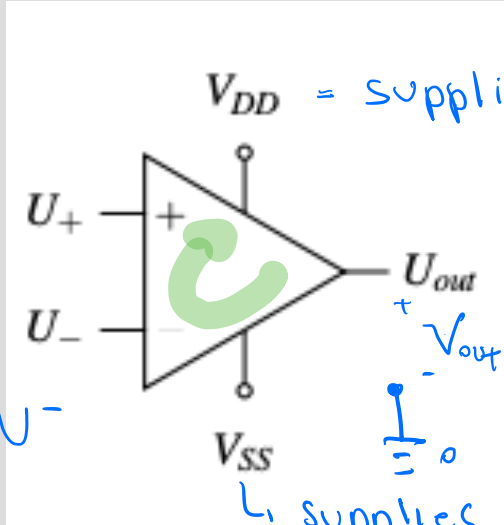
# An example of an Op-amp circuit diagram



# Operational Amplifier

An op-amp (operational amplifier) is a device that transforms a small voltage difference into a very large voltage difference.

Model



An op-amp has two input terminals marked (+) and (-) with potentials  $U_+$  and  $U_-$ , two power supply terminals called  $V_{DD}$  and  $V_{SS}$ , and one output terminal with potential  $U_{out}$ .

$$V_{out} = V_{SS} + \frac{V_{DD} - V_{SS}}{2} + A \cdot V_d$$

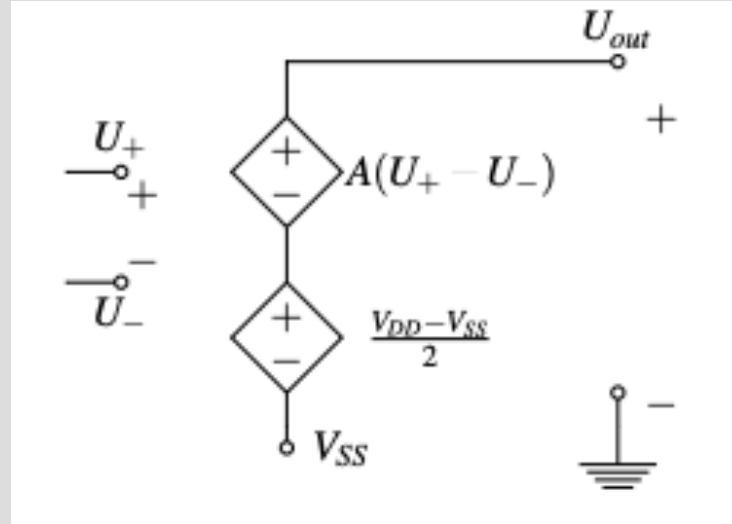
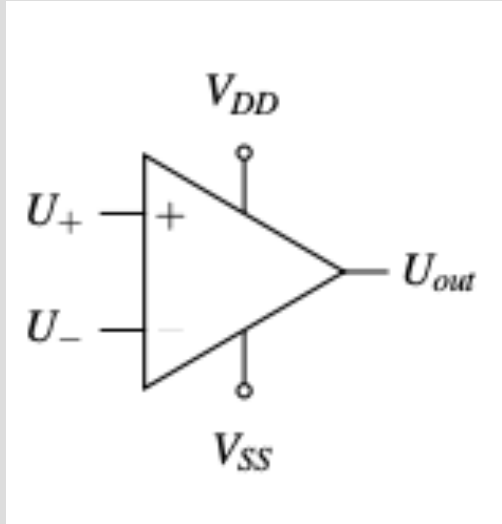
when

$$V_{SS} \leq \frac{V_{DD} - V_{SS}}{2} + A V_d \leq V_{DD}$$

# Operational Amplifier

An op-amp (operational amplifier) is a device that transforms a small voltage difference into a very large voltage difference.

$$\frac{V_{DD} - V_{SS}}{2} + A V_d \quad V^*$$



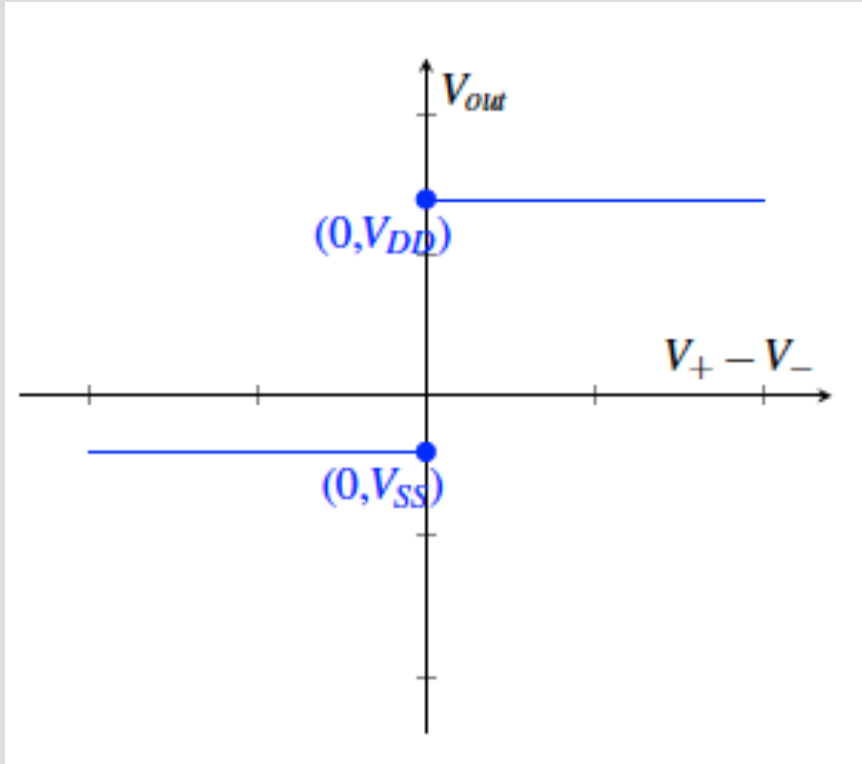
An op-amp has two input terminals marked (+) and (-) with potentials  $U_+$  and  $U_-$ , two power supply terminals called  $V_{DD}$  and  $V_{SS}$ , and one output terminal with potential  $U_{out}$ .

$$V_{out} = V_{DD} \quad \text{if} \quad V^* > V_{DD}$$

$$V_{out} = V_{SS} \quad \text{if} \quad V^* < V_{SS}$$

Can be used to compare Voltage

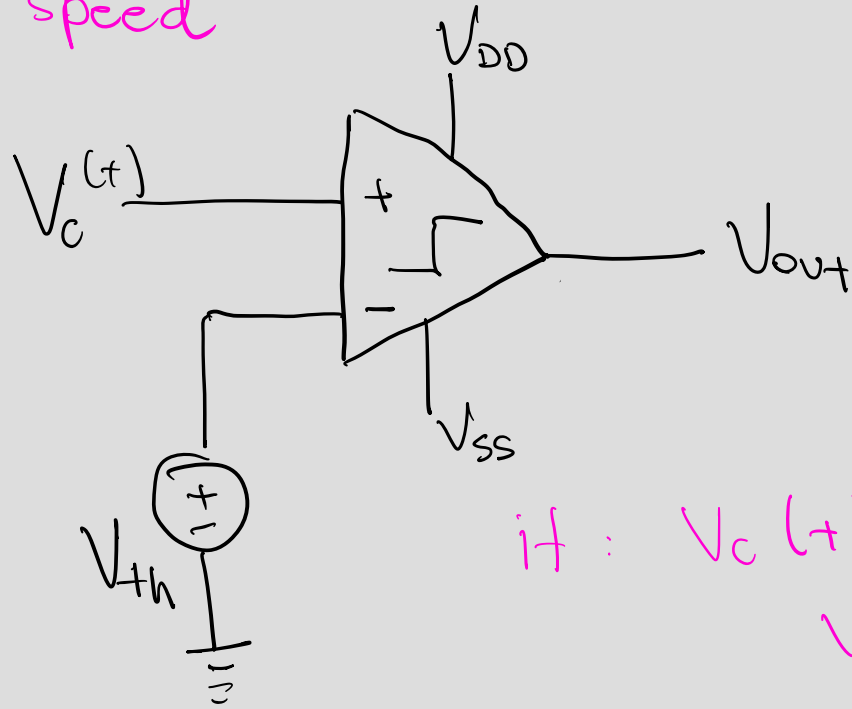
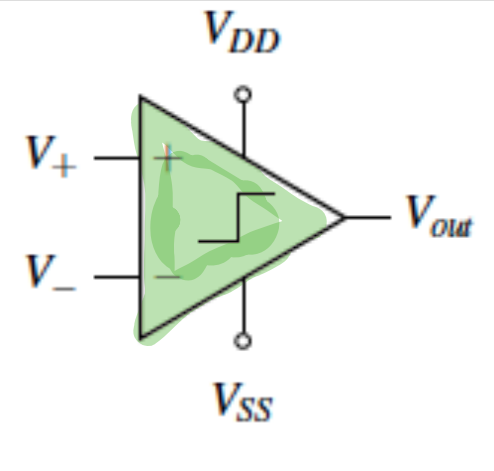
# Comparator – optimized for binary output



$V_{DD}$  can be much  
higher than  $V_{SS}$   
∴  
it amplifies the  
signal.

# Comparator – optimized for binary output

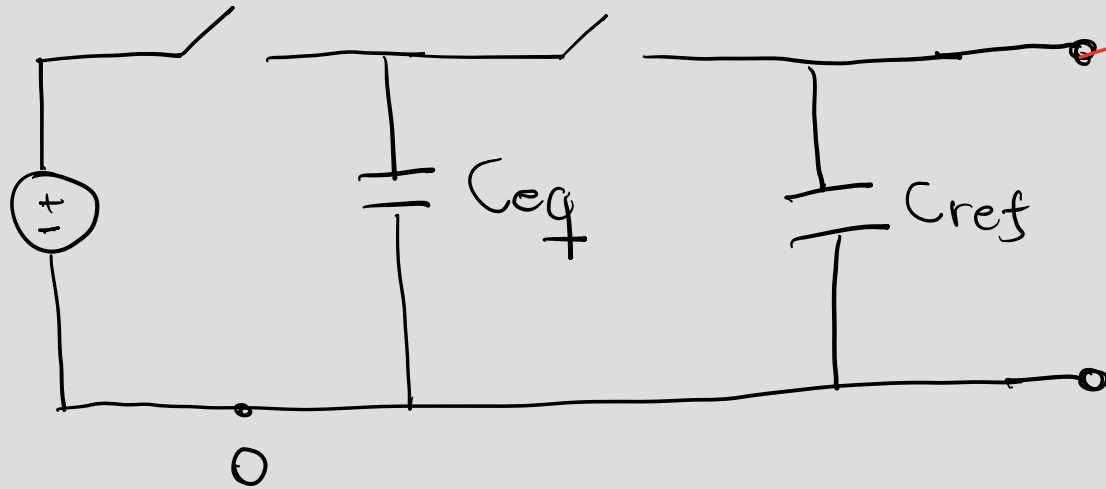
Also optimized for speed



if :  $V_C(t) > V_{th}$   
 $V_{out} = V_{DD}$

if :  $V_C(t) \leq V_{Th}$   
 $V_{out} = V_{SS}$

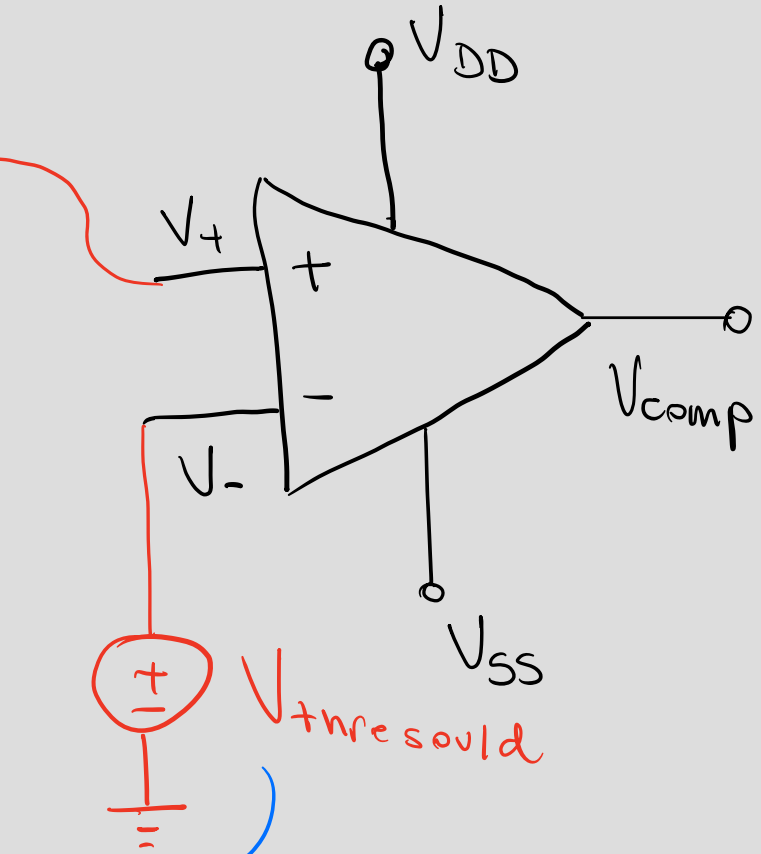
# Back to our Capacitive Touchscreen



$C_{eq} \Rightarrow C_0 + C_{\Delta}$  - touch  
 $C_0$  - no touch

$V_{DD}$  touch

no touch  $V_{SS}$



Should be half way between  $V_{touch}$  and  $V_{notouch}$