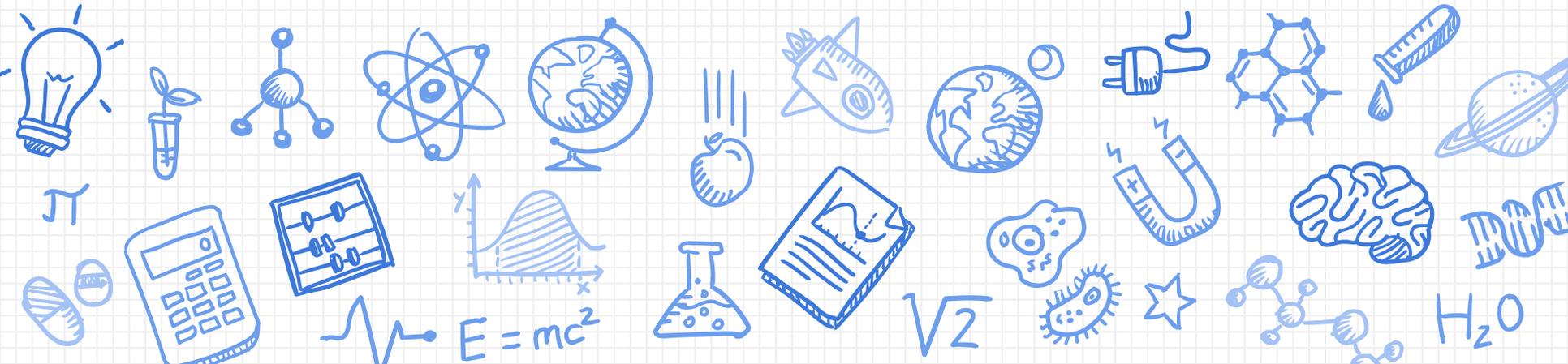


EECS16A

Acoustic Positioning System 1

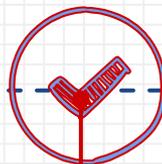
TA, ASE, ASE, ASE



Where Are We Now?



Imaging
Module



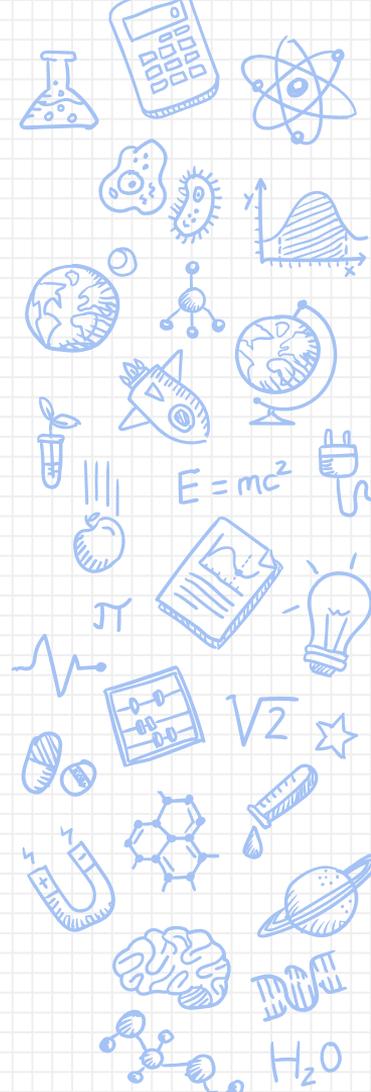
Touchscreen
Module



APS
Module

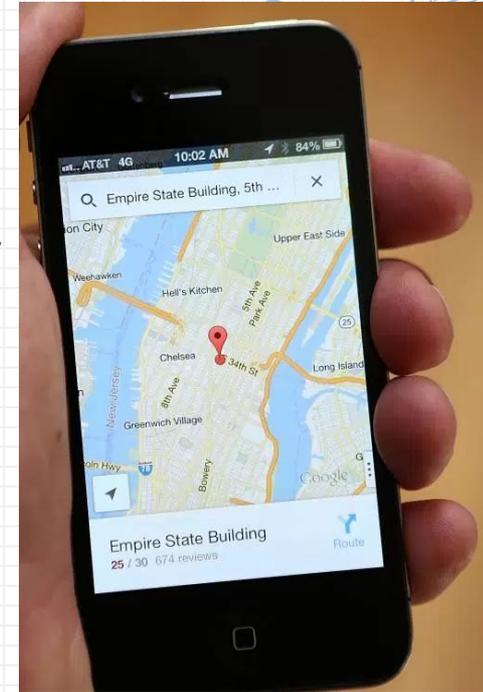
Announcements

- All software
- Submit PDF of completed lab + checkoff quiz on Gradescope
 - due on Friday 4/24 at 11:59 PM PT



Today's lab: Acoustic positioning system

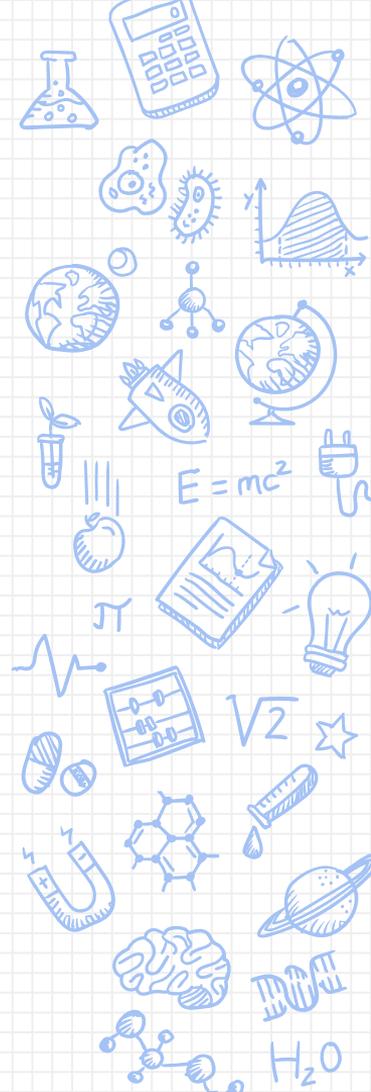
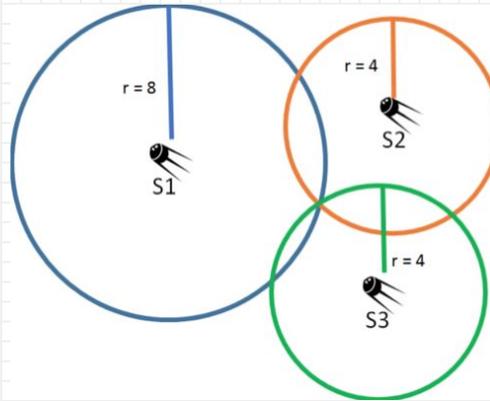
- Global Positioning System (GPS)
 - Very similar logic
 - Uses radio waves instead of sound waves
- Understand mathematical tools used for shifting and detecting signals
 - Think about cross correlation!



Let's go backwards

Assume we know the **distance** between the receiver and every beacon

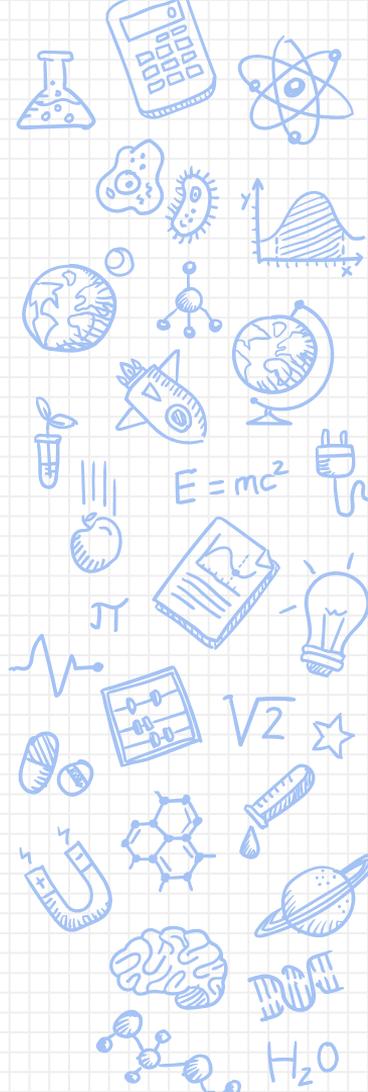
- Use **lateration** and the satellites' locations to locate the receiver!
- How many satellites do we need in a 2D world?



How do we get those distances?

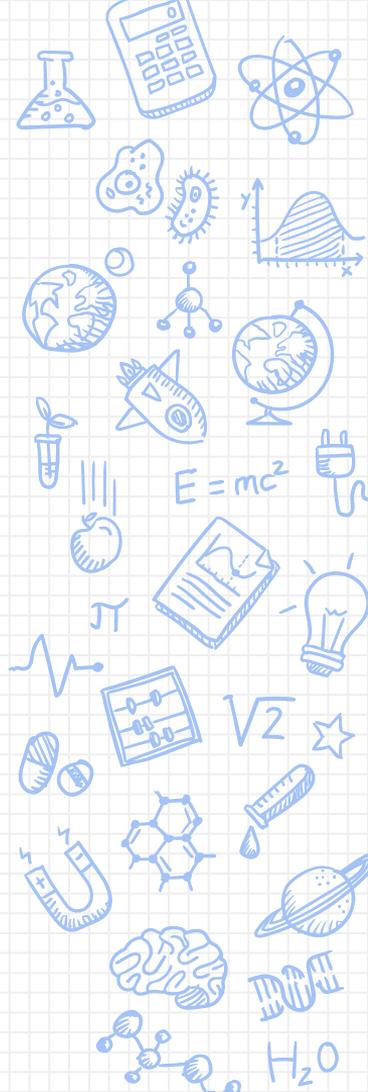
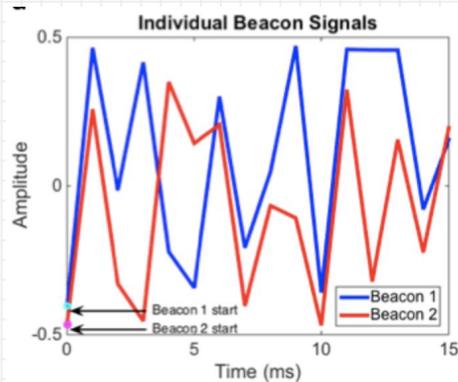
Assume we know the **time-delay** (in secs) of every beacon

- Use the **speed that sound travels** through air to get exactly how far our receiver is from every satellite
 - $d = v * t$



How do we get sample delays?

- Receiver's recorded signal is the sum of all the beacon signals
- Need to separate the recorded signal into the individual beacons to see how many samples each is delayed by



Overview



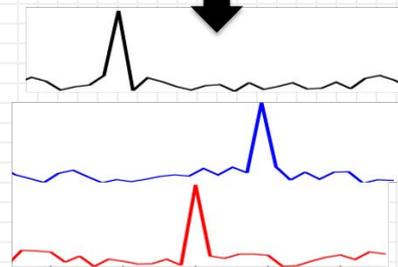
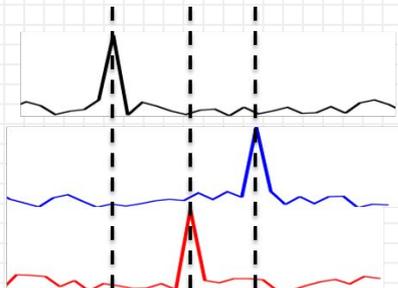
Broadcast beacons



Received signal



Cross Correlation with Each Beacon



Recall: Inner (Dot) product

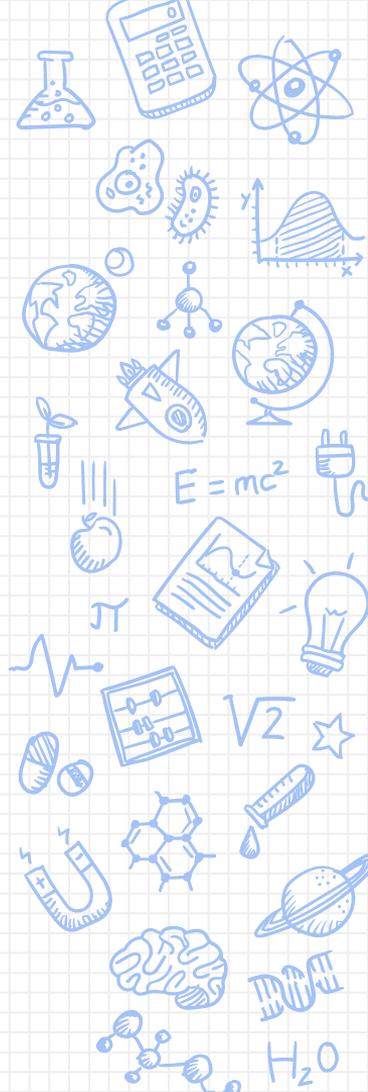
- A mathematical operation for vectors
- Computes how similar two vectors are

$$\langle \vec{x}, \vec{y} \rangle \equiv \vec{x} \cdot \vec{y} \equiv \vec{x}^T \vec{y}$$

$$= \begin{bmatrix} x_1 & x_2 & \cdots & x_n \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

$$= x_1 y_1 + x_2 y_2 + \cdots + x_n y_n$$

$$= \sum_{i=1}^n x_i y_i$$



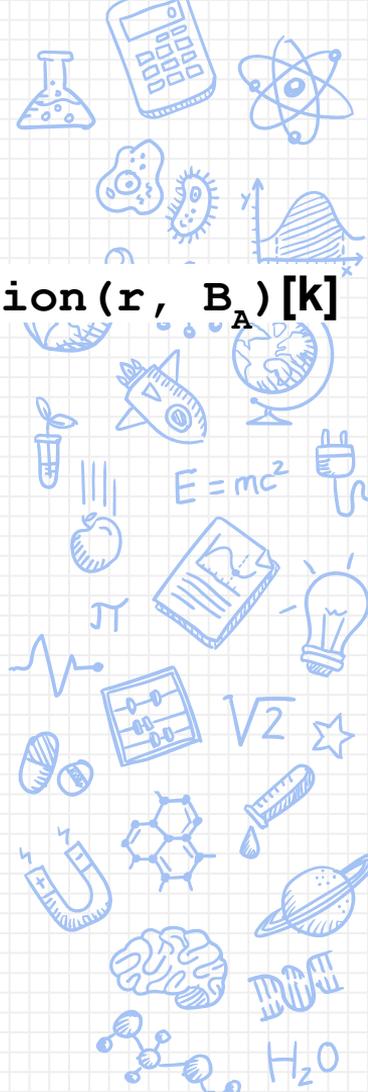
Tool: Cross-correlation

$$\text{corr}_r(B_A)[k] = \sum_{i=-\infty}^{\infty} r[i]B_A[i - k] \Leftrightarrow \text{cross_correlation}(r, B_A)[k]$$

In Python:

`cross_correlation(r, B_A)[k]`

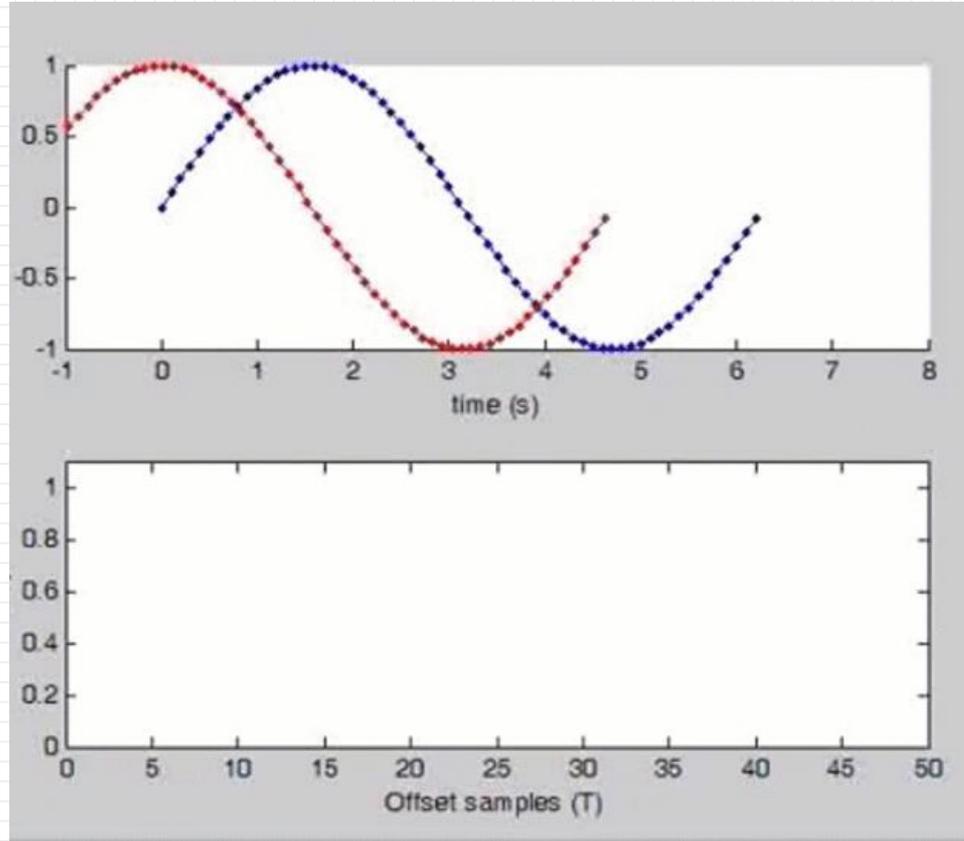
- Mathematical tool for finding similarities between signals
- **Idea:** Computes dot product between r and signal B_A shifted by k samples
- From the previous slide, the peak of the cross-correlation vector tells us which shift amount makes B_A “most similar” to r



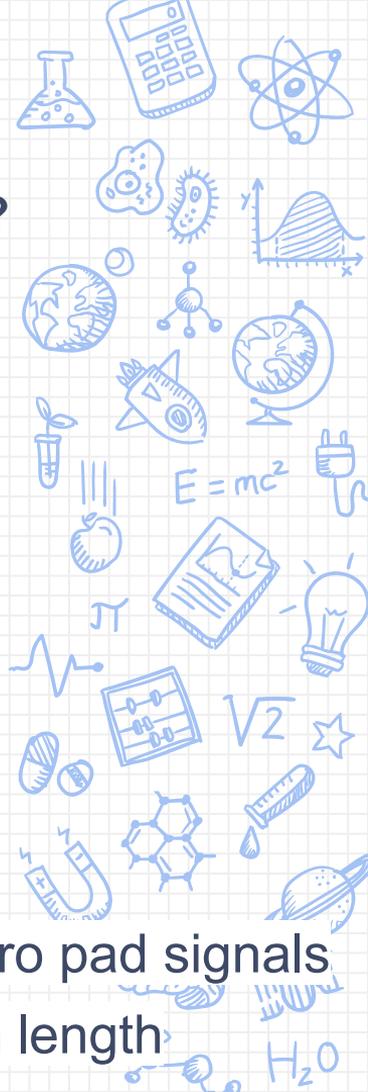
Tool: Cross-correlation

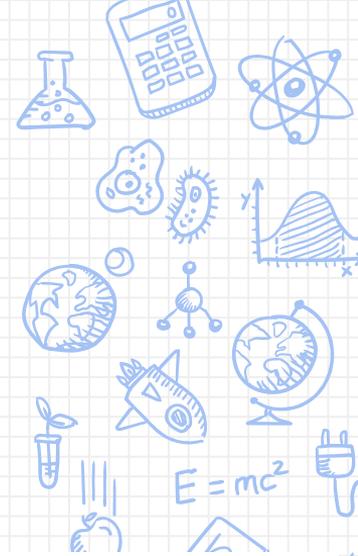
- At ~ how many offset samples are the signals most similar?

$r = \text{blue}$
 $B_A = \text{red}$



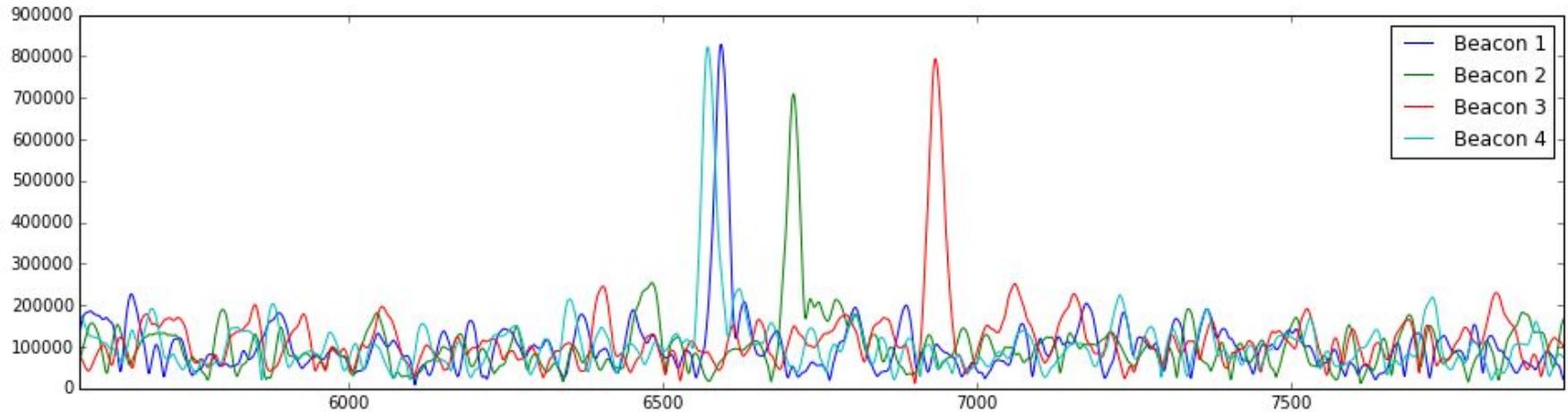
Note: zero pad signals
to match length





How to use?

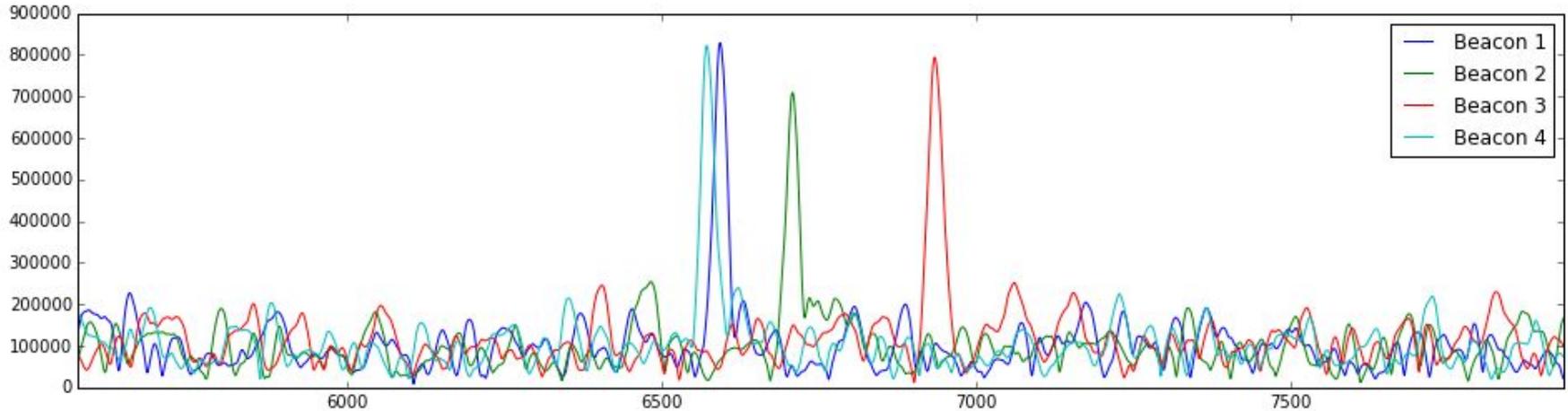
- Cross correlating should tell us where each beacon arrived in our recorded signal
- Let's cross-correlate each of the known beacon signals with what we recorded and plot the result





Absolute or relative sample delays?

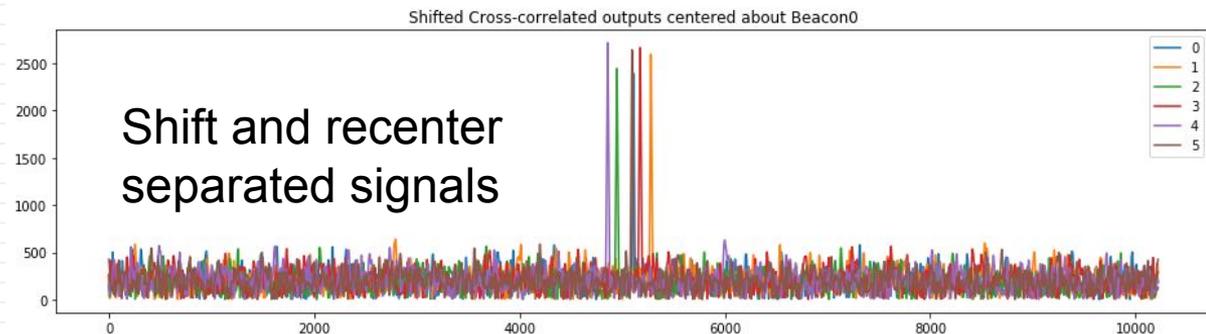
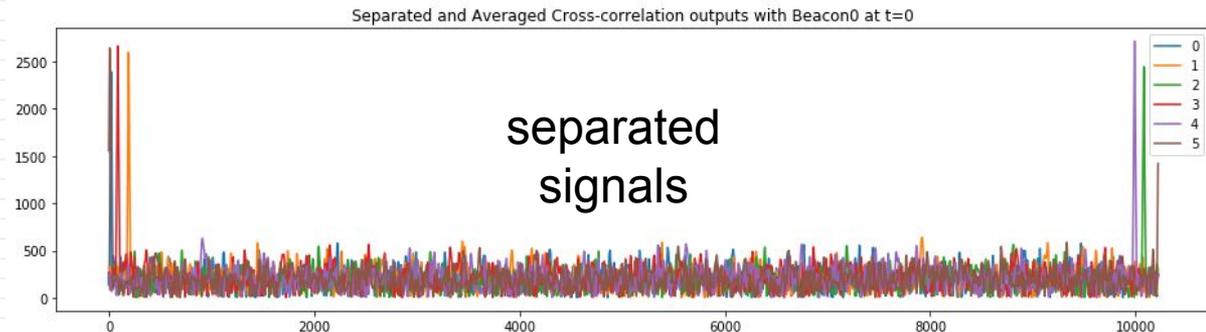
- We can see peaks where each beacon arrived!
- But notice it only gives us **relative** sample delays
 - Still can't tell how many absolute samples each beacon is delayed, we don't know when it was supposed to arrive
- Arbitrarily pick a beacon to be the reference point

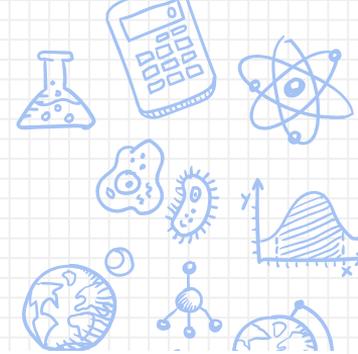




New axis

- Let's shift our axis so beacon 0 has a delay of 0
- We could pick any beacon to be the center
 - 0 is arbitrary

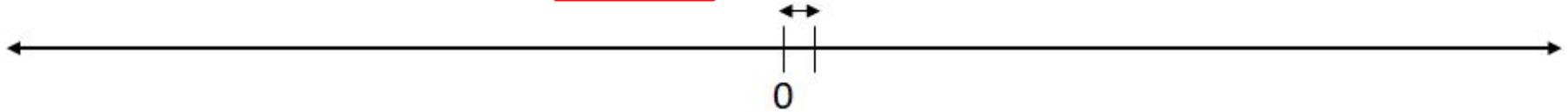




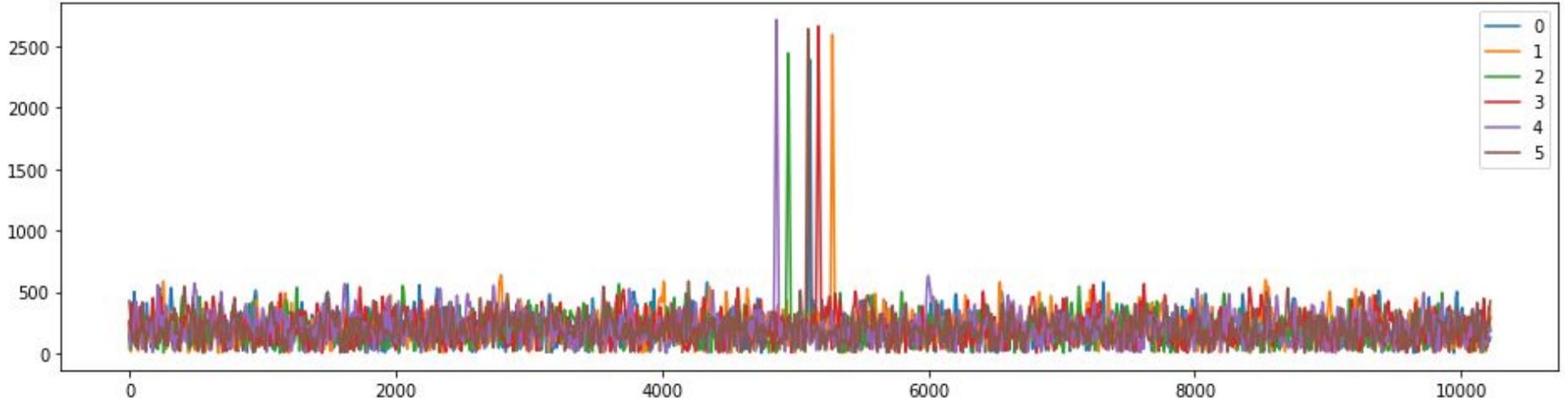
New axis

Now beacon 0 is our new “origin” and all computations are relative to the new “0”

Relative offset of beacon 1

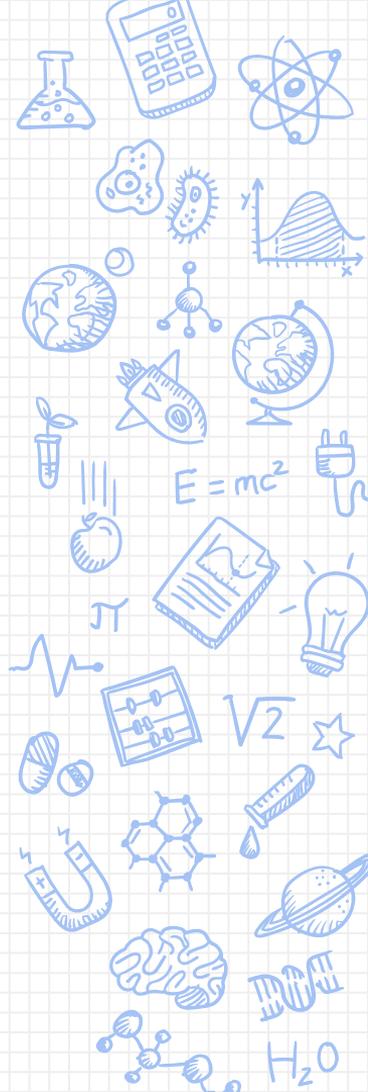


Shifted Cross-correlated outputs centered about Beacon0



Additional assumption for APS1

- What if we knew the absolute sample delay of beacon 0?
 - Now we can adjust all our relative measurements to absolute ones!
 - Assume delay_0 is given, then
$$\text{delay}_i = \text{delay}_i \text{ relative to } 0 + \text{delay}_0$$
- Then we can use absolute time-delays to get distances then location!



Notes + next lab:

- If we know the absolute sample delay of beacon 0, we can locate the receiver
 - Note that this is the same as telling you exactly how far the receiver is from satellite 0
- This week, this value will be given to you
- Find out how to get around this assumption in APS 2!
- **Don't forget to turn in PDF and complete checkoff quiz on Gradescope**

