EECS 16A Designing Information Devices and Systems I
Spring 2022 Homework 7

This homework is due March 11, 2022, at 23:59.
Self-grades are due March 14, 2022, at 23:59.

Submission Format
Your homework submission should consist of **one** file.

- `hw7.pdf`: A single PDF file that contains all of your answers (any handwritten answers should be scanned)

Submit the file to the appropriate assignment on Gradescope.

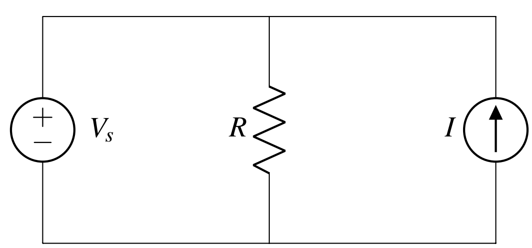
1. **Reading Assignment**

For this homework, please read Notes 13 and 14. Note 13 will refresh you on how simple 1-D resistive touchscreens work, as well as the notion of power in electric circuits. Note 14 will cover a slightly more complicated 2-D resistive touchscreens and how to analyze them from a circuits perspective.

(a) Describe the key ideas behind how the 1D touchscreen works. In general, why is it useful to be able to convert a “physical" quantity like the position of your finger to an electronic signal (i.e. voltage)?

2. **Power Analysis**

Learning Goal: *This problem aims to help you practice calculating power dissipation in different circuit elements. It will also give you insights into how power is conserved in a circuit.*



(a) Find the expressions of power dissipated by each element in the circuit above. Remember to label voltage-current pairs using passive sign convention.

(b) Use $R = 5\text{k}\Omega$, $V_s = 5\text{V}$, and $I = 5\text{mA}$. Calculate the power dissipated by the voltage source (P_{V_s}), the current source (P_I), and the resistor (P_R).

(c) Once again, let $R = 5\text{k}\Omega$, $V_s = 5\text{V}$. What does the value I of the current source have to be such that the current source **dissipates** 40mW? Note that it is possible for a current source to *dissipate* power, i.e. under passive sign convention, $P_I = 40\text{mW}$. For this value of I, compute P_{V_s}, P_I, and P_R as well.

As an aside: If the current source were delivering power *it would have been* $P_I = -40\text{mW}$*, under passive sign convention, but this is NOT what the question is asking about.*

3. Volt and ammeter

Learning Goal: *This problem helps you explore what happens to voltages and currents in a circuit when you connect voltmeters and ammeters in different configurations.*

Use the following numerical values in your calculations: $R_1 = 1\,\mathrm{k}\Omega$, $R_2 = 2\,\mathrm{k}\Omega$, $R_3 = 3\,\mathrm{k}\Omega$, $R_4 = 4\,\mathrm{k}\Omega$, $R_5 = 5\,\mathrm{k}\Omega$, $V_s = 10V$.

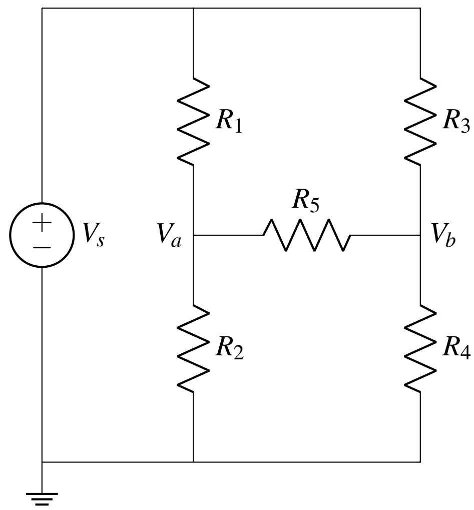


Figure 1: Circuit consisting of a voltage source V_s and five resistors R_1 to R_5

(a) Redraw the circuit diagram shown in Figure 1 by adding a voltmeter (letter V in a circle and plus and minus signs indicating direction) to measure voltage V_{ab} from node V_a (positive) to node V_b (negative). Calculate the value of V_{ab}. You may use a numerical tool such as IPython to solve the final system of linear equations.

(b) Suppose you accidentally connect an ammeter in part (a) instead of a voltmeter. Calculate the value of V_{ab} with the ammeter connected.

(c) Redraw the circuit diagram shown in Figure 1 by adding an ammeter (letter A in a circle and plus and minus signs indicating direction) in series with resistor R_5. This will measure the current I_{R_5} through R_5. Calculate the value of I_{R_5}.

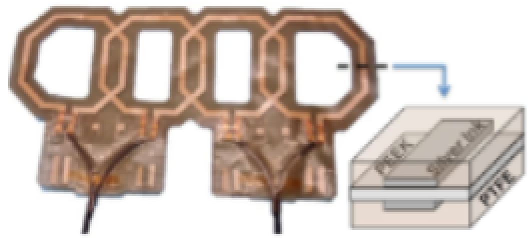
(d) Your friend accidentally connects a voltmeter in part (c) above, rather than an ammeter. Calculate the value of I_{R_5} with the voltmeter connected.

4. Printed electronics

Learning Goal: *This problem will help you practice thinking about electronic materials and their properties.*

All electronic devices require connections to conduct signals. These connections, or traces, are manufactured through different deposition methods such as physical vapor deposition and chemical vapor deposition. Another less traditional technique is printing. Inks can be made from metallic nanoparticles and deposited using inkjet printing, screen printing, and spray coating. A commonly printed metal ink is silver.

Here's an example of a printed MRI antenna coil from research conducted in Prof. Ana Arias's lab.



(a) Say we screenprinted a trace of silver 20 mm in length and 4 µm in width. Given the resistivity should be 0.001 Ω mm, and we measure the resistance of the trace to be 250 Ω, what is the trace thickness?

(b) Nanoparticle inks often require a drying step called *sintering*, during which the nanoparticles coalesce and form condcutive pathways. The manufacturer of our silver paste lists 100 °C and 175 °C as two possible sintering temperatures resulting in resistivities of 0.001 Ω mm and 0.5 Ω µm. Given that we need a trace 20 mm in length, 4 µm in width, and 20 µm in thickness, what is the smallest resistance trace we can obtain and with which sintering temperature?

(c) Say the maximum resistance we can tolerate is 125 Ω. What would the cross sectional areas required be from both sintering temperatures to achieve the specified resistance for our 20 mm long trace?

(d) Continuing with the design specifications from part (c), if our printing technique has a resolution limit of one micron (meaning the minimum width and minimum length achieveable is one micron) and we want to aim for a trace thickness of at least one hundred micron for good film uniformity, then at which temperature should we sinter our printed silver?

(e) One unique advantage of using printing as a deposition technique is that electronic devices can be fabricated on plastic flexible substrates rather than brittle silicon wafers, allowing for applications where lightweight, conformable electronics are needed. However, when heated, plastic substrates can begin to soften and deform. Using your answer from part (c) and part (d) what is one drawback from the lower sintering temperature, and what is one drawback from the higher sintering temperature?

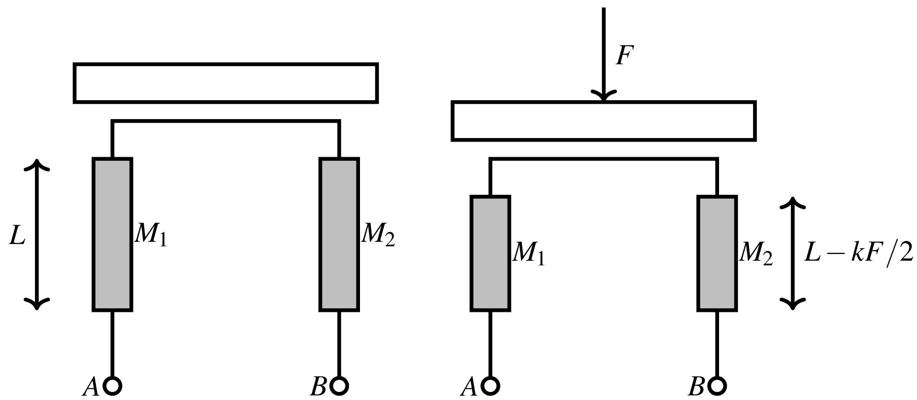
5. Fruity Fred

Learning Goal: *This problem will introduce the process of designing a sensing circuit for the purpose of measuring a physical quantity. This will also help to build your intuition for modeling physical elements.*

Fruity Fred just got back from Berkeley Bowl with a bunch of mangoes, pineapples, and coconuts. He wants to sort his mangoes in order of weight, so he decides to use his knowledge from EECS16A to build a scale.

He finds two identical bars of material (let's call them M_1 and M_2) of length L (in meters) and a cross-sectional area (i.e. width $\times$ thickness) of A_c (in meters^2). The bars are made of a material with resistivity ρ. He knows that the **length of these bars decreases** by k meters per Newton of force applied, while the **cross-sectional area remains constant**.

He builds his scale as shown below, where the top of the vertical bars are connected with an ideal electrical wire. The left side of the diagram shows the scale at rest (with no object placed on it), and the right side shows it when the applied force is F (Newtons). The force F is equally distributed between two bars, causing the length of each bar to decrease by $kF/2$ meters.



(a) Let R_{AB} be the resistance between nodes A and B with the weights on the scale. Write an expression for R_{AB} as a function of A_c, L, ρ, F, and k. *Hint: You can start by representing each bar as a resistor, then find how they are connected.*

(b) Fred wants to measure a voltage that changes based on how much weight is placed on his scale. He knows that R_{AB} will change with the weight on the scale.

Design a circuit for Fred that outputs a voltage that is some function of the weight F. This function does *not* have to be linear. **Your circuit should include R_{AB}, and you may use any number of voltage sources and resistors in your design.** Be sure to **label** where the voltage should be measured in your circuit.

Also provide an **expression** relating the output voltage of your circuit to the force applied on the scale. This expression can contain any necessary parameters.

Hint: If you connected only a voltage source across A and B and measured the voltage (V_{AB}) between A and B, would V_{AB} change based on the value of R_{AB}? It turns out it wouldn't. Why?

Hint: Consider tools we have learned in this class such as voltage dividers. Can you build a circuit using R_{AB} and R_{fixed}, where R_{fixed} is a value you know and choose?

6. Resistive Touchscreen

Learning Goal: *The objective of this problem is to provide insight into modeling of resistive elements. This will also help to apply the concepts from resistive touchscreen.*

In this problem, we will investigate how a resistive touchscreen with a defined thickness, width, and length can actually be modeled as a series combination of resistors. As we know the value of a resistor depends on its length.

Figure 2 shows the top view of a resistive touchscreen consisting of a conductive layer with resistivity ρ_1, thickness t, width W, and length L. At the top and bottom it is connected through perfect conductors ($\rho = 0$) to the rest of the circuit. The touchscreen is wired to voltage source V_s.

Use the following numerical values in your calculations: $W = 50$ mm, $L = 80$ mm, $t = 1$ mm, $\rho_1 = 0.5\,\Omega$m, $V_s = 5$V, $x_1 = 20$ mm, $x_2 = 45$ mm, $y_1 = 30$ mm, $y_2 = 60$ mm.

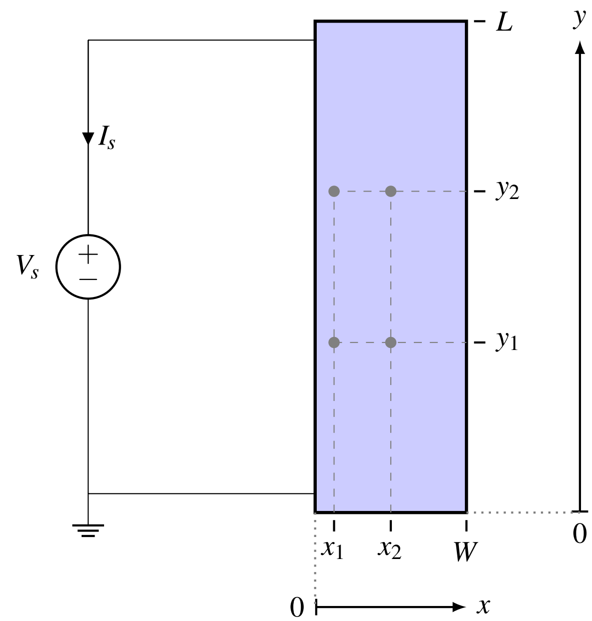


Figure 2: Top view of resistive touchscreen (not to scale). z axis i.e. the thickness not shown (into the page).

(a) Draw a circuit diagram representing Figure 2, where the entire touchscreen is represented as *a single resistor*. **Note that no touch is occurring in this scenario.** Remember that circuit diagrams in general consist of only circuit elements (resistors, sources, etc) represented by symbols, connecting wires, and the reference/ ground symbol. Calculate the value of current I_S based on the circuit diagram you drew. Do not forget to specify the correct unit as always.

(b) Let us assume u_{12} is the node voltage at the node represented by coordinates (x_1, y_2) of the touchscreen, as shown in Figure 3. What is the value of u_{12}? You should first draw a circuit diagram representing Figure 3, which includes node u_{12}. Specify all resistance values in the diagram. Does the value of u_{12} change based on the value of the x-coordinate x_1?

Hint: You will need more than one resistor to represent this scenario.

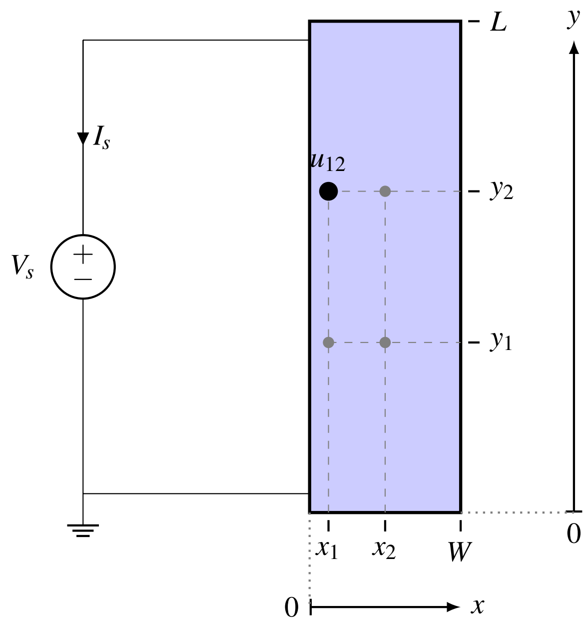


Figure 3: Top view of resistive touchscreen showing node u_{12}.

(c) Assume V_{ab} is the voltage measured between the nodes represented by touchscreen coordinates (x_1, y_1) and coordinates (x_1, y_2), as shown in Figure 4. Calculate the absolute value of V_{ab}. As with the previous part, you should first draw the circuit diagram representing Figure 4, which includes V_{ab}. Calculate all resistor values in the circuit. *Hint: Try representing the segment of the touchscreen between these two coordinates as a separate resistor itself.*

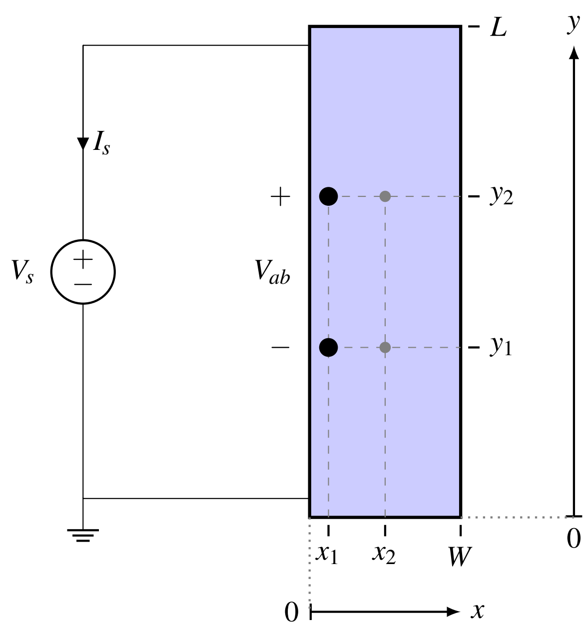


Figure 4: Top view of resistive touchscreen showing voltage V_{ab}.

(d) Calculate (the absolute value of) the voltage between the nodes represented by touchscreen coordinates (x_1, y_1) and coordinates (x_2, y_1) in figure 4.

(e) Calculate (the absolute value of) the voltage between the nodes represented by touchscreen coordinates (x_1, y_1) and coordinates (x_2, y_2) in figure 4.

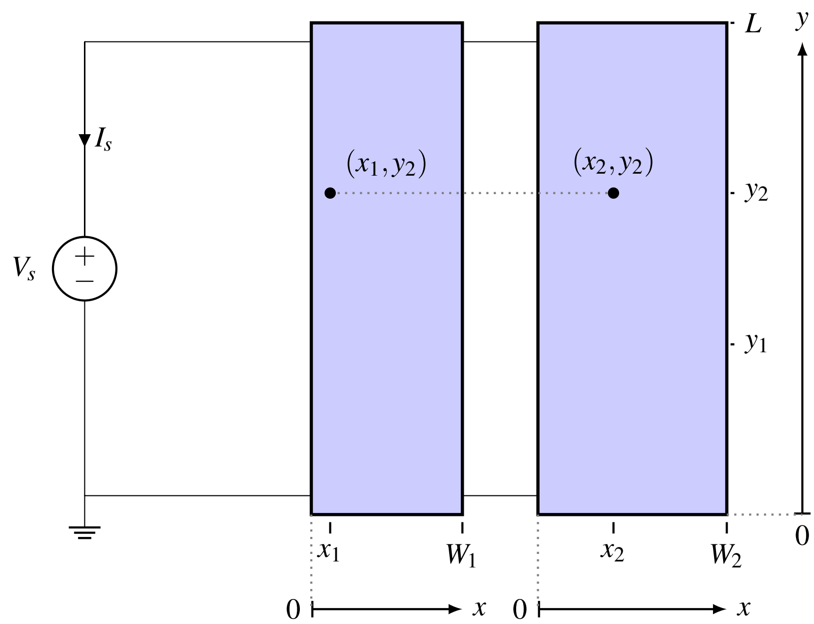


Figure 5: Top view of two touchscreens wired in parallel (not to scale). z axis not shown (into the page).

(f) Figure 5 shows a new arrangement with two touchscreens. The two touchscreens are next to each other and are connected to the voltage source in the same way. The second touchscreen (the one on the right) is identical to the one shown in Figure 2, except for different width, W_2, and resistivity, ρ_2.

Use the following numerical values in your calculations: $W_1 = 50$ mm, $L = 80$ mm, $t = 1$ mm, $\rho_1 = 0.5\,\Omega\,\text{m}$, $V_s = 5\text{V}$, $x_1 = 20$ mm, $x_2 = 45$ mm, $y_1 = 30$ mm, $y_2 = 60$ mm, which are the same values as before. The new touchscreen has the following numerical values which are different: $W_2 = 85$ mm, $\rho_2 = 0.6\,\Omega\,\text{m}$.

Draw a circuit diagram representing Figure 5, where the two touchscreens are represented as *two separate resistors*. **Note that no touch is occurring in this scenario.**

(g) Calculate the value of current I_s for the two touchscreen arrangement based on the circuit diagram you drew in the last part.

(h) Consider the two points: (x_1, y_2) in the touchscreen on the left, and (x_2, y_2) in the touchscreen on the right in Figure 5. Show that the node voltage at (x_1, y_2) is the same that at (x_2, y_2), i.e. the potential difference between the two points is 0. You can show this without explicitly calculating the node voltages at the two points.

If you were to connect a wire between the two coordinates (x_1, y_2) in the touchscreen on the left, and (x_2, y_2) in the touchscreen on the right, would any current flow through this wire?

7. Homework Process and Study Group

Who did you work with on this homework? List names and student ID's. (In case you met people at homework party or in office hours, you can also just describe the group.) How did you work on this homework? If you worked in your study group, explain what role each student played for the meetings this week.