## 1. KVL/KCL Review

Use Kirchhoff's Laws on the circuit below to find $V_{x}$ in terms of $V_{\text {in }}, R_{1}, R_{2}, R_{3}$.


Figure 1: Example Circuit
(a) Recall Node Voltage Analysis (NVA). Determine $V_{x}$ by labeling the circuit and writing equations to solve a system of equations in node voltages.
(b) In EECS16A, you learned you can simplify analysis by replacing series or parallel resistors with equivalents and memorizing common circuit design blocks. Determine $V_{x}$ by leveraging resistor equivalence and recognition of a design block.
(c) As a check, as $R_{3} \rightarrow \infty$, what is $V_{x}$ for what you found in (a) and (b)? The $V_{x}$ 's of each part should approach the same value. What is the name we used for this type of circuit?

## 2. Current Sources And Capacitors

(Adapted from EECS16A Fall 20 Disc 9A.)
(HINT: Recall charge has units of Coulombs. (C), and capacitance is measured in Farads. (F). Also, 1F $=\frac{1 \mathrm{C}}{1 \mathrm{~V}}$. It may also help to note metric prefix examples: $3 \mu \mathrm{~F}=3 \times 10^{-6} \mathrm{~F}$.)

Given the circuit in fig. 2, find an expression for $v_{\text {out }}(t)$ in terms of $I_{S}, C, V_{0}$, and $t$, where $V_{0}$ is the initial capacitor voltage at $t=0$.


Figure 2: A current source attached to a capacitor.

Then plot the function $v_{\text {out }}(t)$ over time on the graph below for each set of conditions, detailed below.

Use the values $I_{S}=1 \mathrm{~mA}$ and $C=2 \mu \mathrm{~F}$.
(1) Capacitor is initially uncharged $V_{0}=0$ at $t=0$.
(2) Capacitor has been charged with $V_{0}=1.5 \mathrm{~V}$ at $t=0$.
(3) (PRACTICE) Swap this capacitor for one with half the capacitance $C=1 \mu \mathrm{~F}$, which is initially uncharged $V_{0}=0$ at $t=0$.
(HINT: Recall the calculus identity $\int_{a}^{b} f^{\prime}(x) \mathrm{d} x=f(b)-f(a)$, where $f^{\prime}(x)=\frac{\mathrm{d} f}{\mathrm{~d} t}$.)


## 3. Op-Amp Summer

Consider the following circuit (assume the op-amp is ideal):


Figure 3: Op-amp Summer

What is the output $V_{o}$ in terms of $V_{1}$ and $V_{2}$ ? You may assume that $R_{1}, R_{2}$, and $R_{f}$ are known.

