

#### **EECS 16B**

# Designing Information Devices and Systems II Lecture 2

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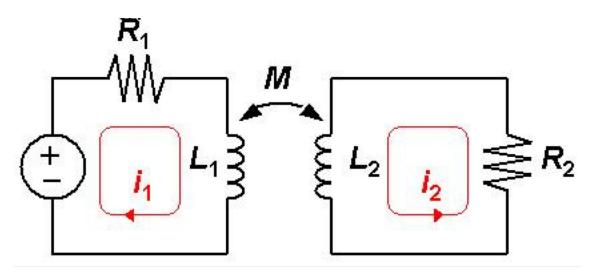
#### **Transient Response**

- Outline
  - Mutual Inductance
  - DAC and ADC
  - R-C circuits
  - R-L circuits
  - Steady State

#### • Reading: Section 3.6, 4.1-4.4, Slides

#### **Mutual Inductance**

- Mutual inductance occurs when two windings are arranged so that they have a mutual flux linkage
- The change in current in one winding causes a voltage drop to be induced in the other



Transformers (adapters), motors, generators (electric cars)

## **The Dot Convention**

- If a current enters the dotted terminal of a coil, the reference polarity of the voltage induced in the other coil is positive at its dotted terminal.
- If a current leaves the dotted terminal of a coil, the reference polarity of the voltage induced in the other coil is negative at its dotted terminal.
- Total voltage induced in a coil is a summation of its own induced voltage and the mutually induced voltage

$$i_{1} \qquad M \qquad i_{2} \qquad + \circ \qquad i_{1} \qquad M \qquad i_{2} \qquad + \circ \qquad i_{1} \qquad M \qquad i_{2} \qquad + \circ \qquad + \circ$$

## Summary

#### **Capacitors:**

$$i = C \frac{dv}{dt}$$
$$w = \frac{1}{2}Cv^2$$

- v cannot charge instantaneously
- *i* **can** charge instantaneously (do not short circuit a charged capacitor)
- *N* capacitors in series

$$\frac{1}{C_{eq}} = \sum_{i=1}^{N} \frac{1}{C_{eq}}$$

• *N* capacitors in parallel  $C_{eq} = \sum C_i$ 

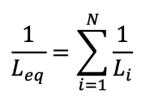
#### Inductors:

$$v = L\frac{di}{dt}$$
$$w = \frac{1}{2}Li^2$$

- *i* cannot charge instantaneously
- v can charge instantaneously (do not open an inductor with current)
- *N* inductors in series

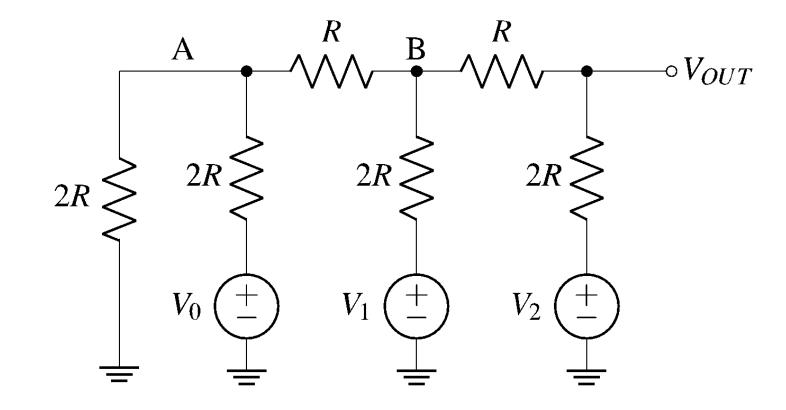
$$L_{eq} = \sum_{i=1}^{N} L_i$$

• *N* inductors in parallel

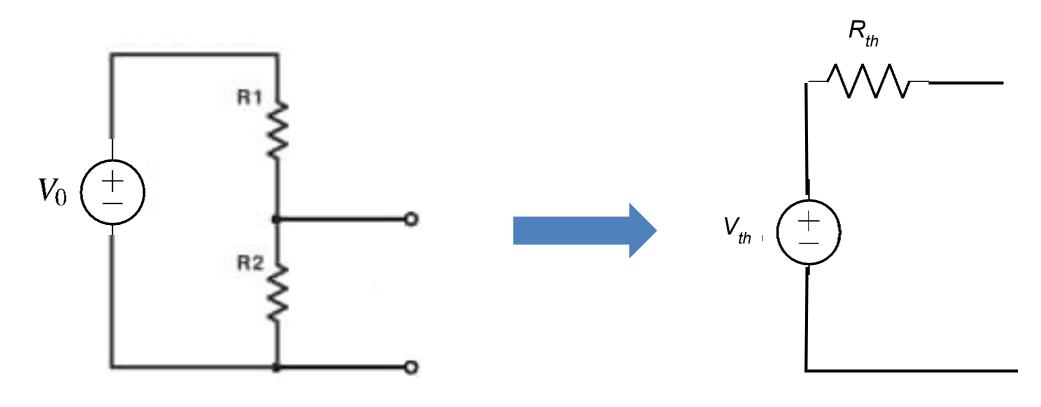


Lecture 2, Slide 5

#### **Simple Circuits**

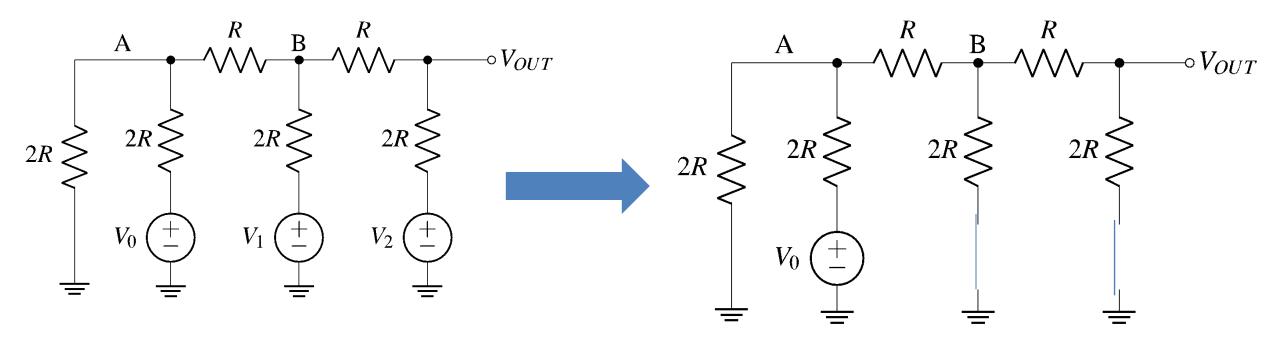


#### **Remember Superposition and Equivalence?**

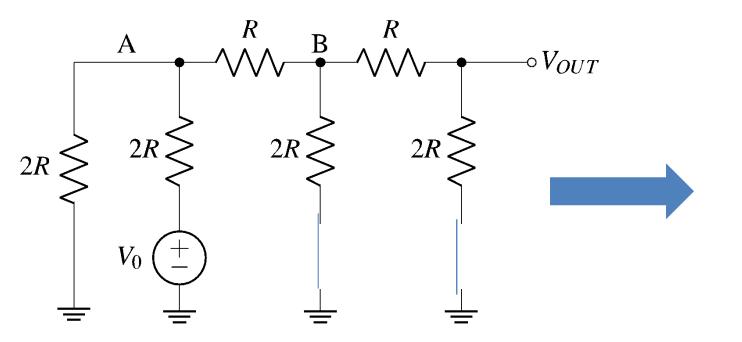


Thevenin Equivalent

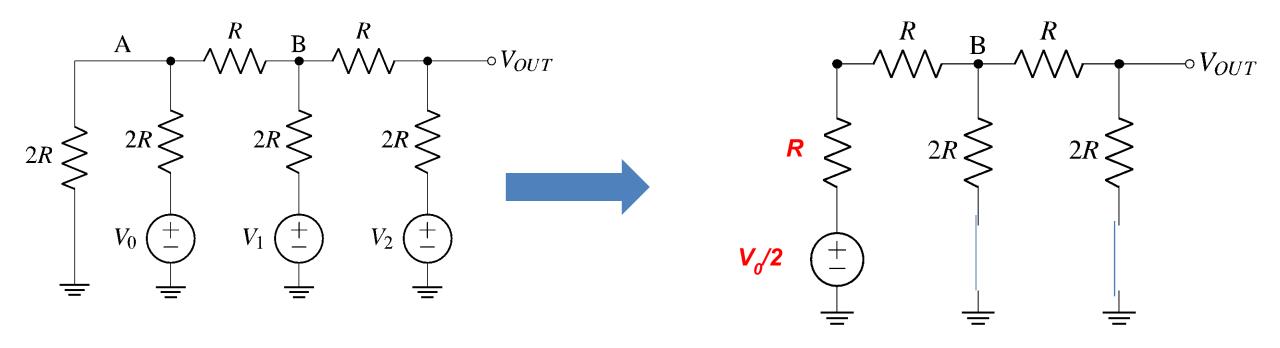
Use superposition: Start with  $V_0$ 



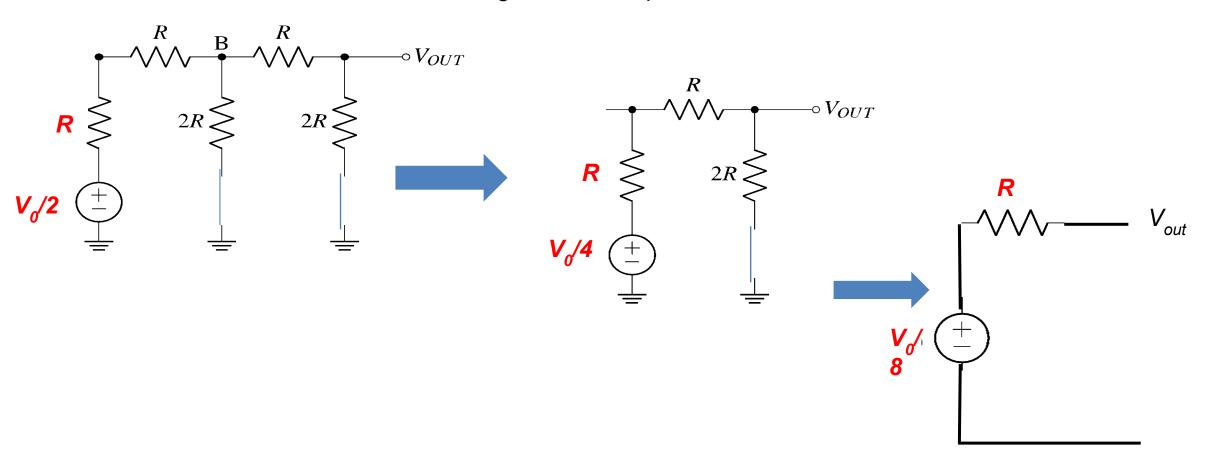
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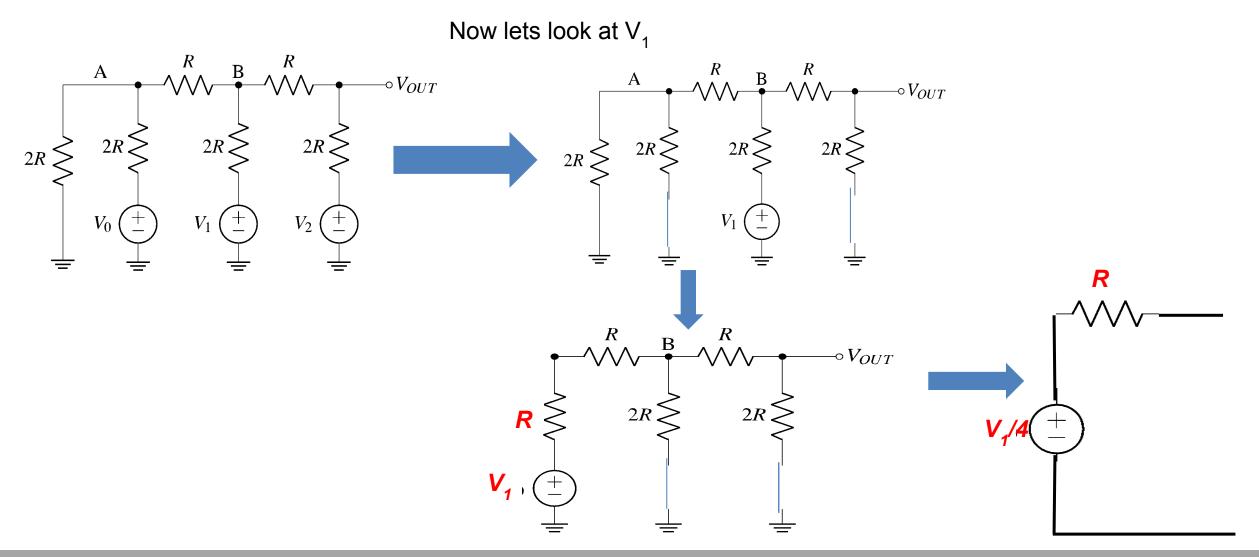


Using Thevenin Equivalent



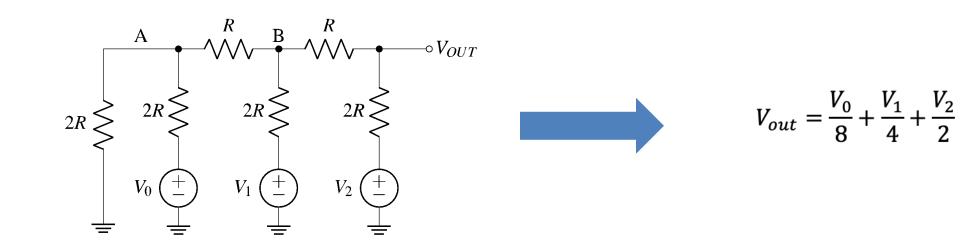
Using Thevenin Equivalent





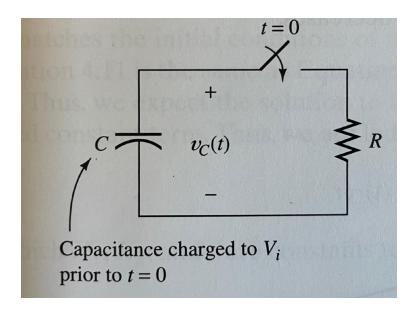
Lecture 2, Slide 13

Adding all contributions from the sources



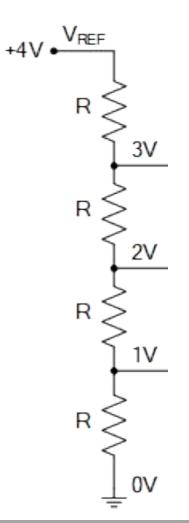
## **R-C circuits: Response in time**

Say a capacitor C had a stored charge of Q so that it held a voltage of  $V_i$  across it. At *t*=0 a switch connects it to a resistor completing the circuit.

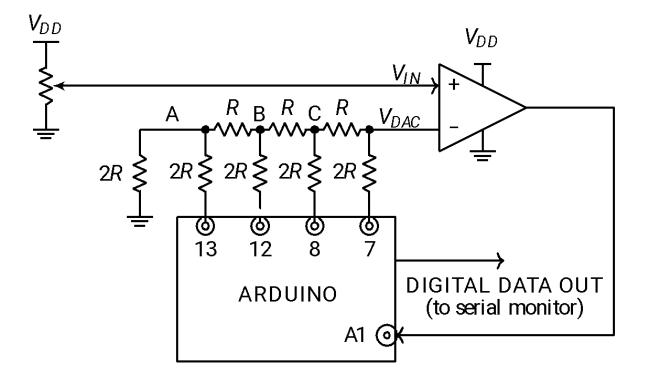


## **Analog to Digital Conversion**

Say we want to convert an analog signal to a 2 bit digital signal  $\Box$  4 levels

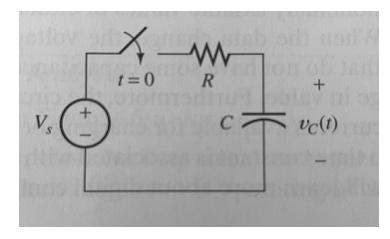


## Lab 2: SAR (Successive Approximation Resistor) ADC



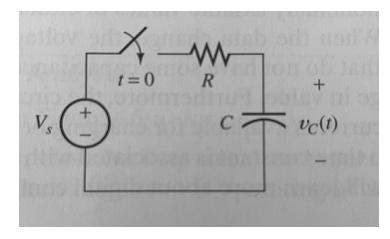
## **R-C circuits: Response in time**

We now ask a slightly different question. What happens if a capacitor that had initially no charge is connected to a constant voltage at t=0



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## **General Solution of the Differential Equation**

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For a first order, linear differential equation of the form

 $\frac{dy}{dt} + ay(t) = b(t)$  where we assume a to be a constant

Homogeneous/Compl ementary solution

$$\frac{dy}{dt} + ay(t) = 0$$
  

$$\Rightarrow \frac{dy}{y} = -a$$
  

$$\Rightarrow \ln(y) = -at + C$$
  

$$\Rightarrow y(t) = Ke^{-at}$$

**Particular Solution (Integrating Factor Method):** 

 $\frac{dy}{dt} + ay(t) = b(t)$ 

We want to find a multiplier function f(t) such that

 $f(t)\frac{dy}{dt} + af(t)y(t) = b(t)f(t)$ can be written as  $\frac{d}{dt}[y(t)f(t)] = b(t)f(t) \quad --(A)$  For equation (A) to hold

$$\frac{df(t)}{dt} = af(t)$$
  

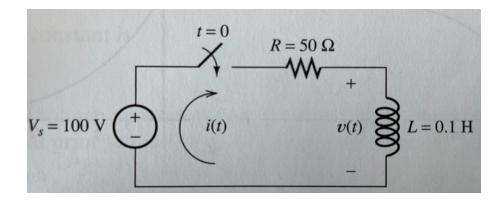
$$\Rightarrow f(t) = e^{at}$$

Then from (A)

$$\begin{split} y(t) &= \frac{1}{f(t)} \int b(t) f(t) dt \\ \Rightarrow y_p(t) &= e^{-at} \int e^{at} b(t) dt \end{split}$$

 $y(t) = Ke^{-at} + e^{-at} \int e^{at} b(t) dt$  K is determined using initial condition

#### **R-L Circuits**



#### **Steady State**

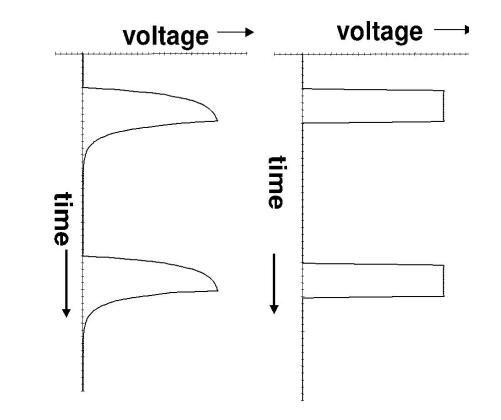
Capacitors:

Inductors:

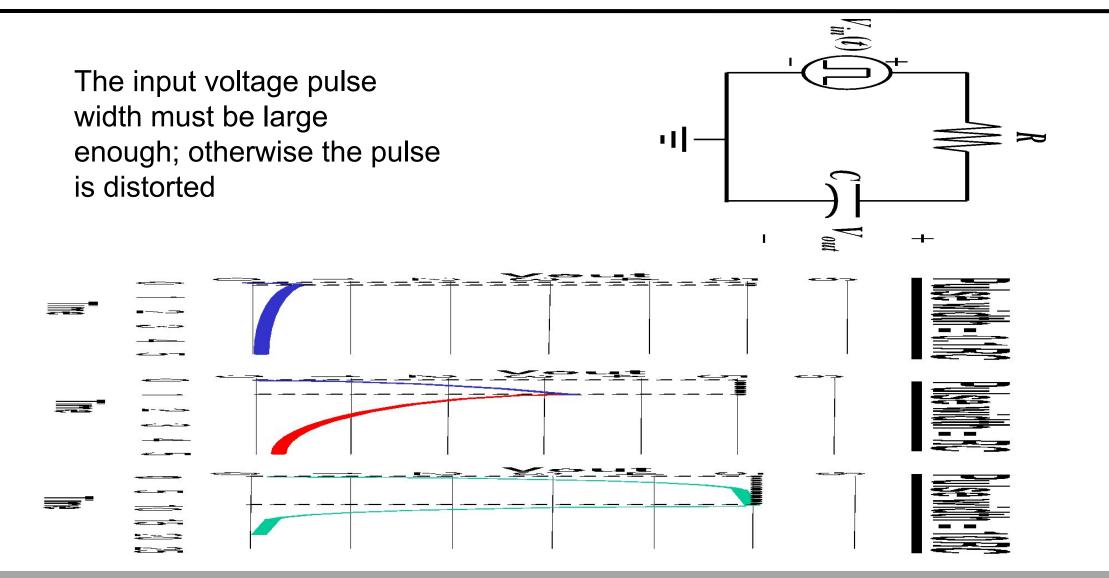
## **Digital Signals to a RC circuit**

• Every node in a real circuit has capacitances

 Even if we send in very 'pure' square looking pulses what we actually get is how it looks in the right due to capacitor charging and discharging <u>unless we go very</u> <u>very slow</u>

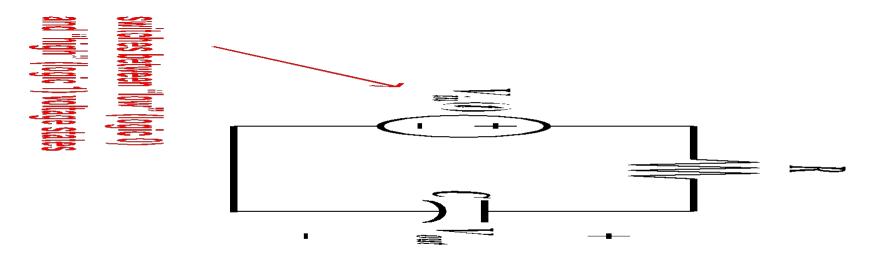


#### **Pulse Distortion**



## **Computers are RC circuits (almost)**

- Digital circuits are predominantly RC circuits (other than the communication part)
- Simplistically a logic gate can be model as a RC circuit
- The speed of the computer is limited by the RC time constant



#### **Complex Numbers**

• 
$$e^{i\theta} = \cos(\theta) + i\sin(\theta)$$

• Read the note j